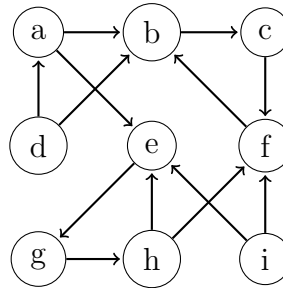


# Problem Set 5

CS 331H

Due Thursday, March 25

1. Solve the graph reduction exercises in the Jupyter notebook on the website.
2. Consider running DFSALL on the following graph, where every iteration (the outer one over all vertices, and the inner ones over edges) is in alphabetical order by vertex name:



- (a) What is the preorder of the vertices? What is the postorder?
  - (b) Shade in the “tree” edges.
  - (c) Circle the strongly connected components.
  - (d) Give a topological ordering of the strong component graph.
3. (Problem 21 of book chapter 6) Kris is a professional rock climber who is competing in the U.S. climbing nationals. The competition requires Kris to use as many holds on the climbing wall as possible, using only transitions that have been explicitly allowed by the route-setter. The climbing wall has  $n$  holds. Kris is given a list of  $m$  pairs  $(x, y)$  of holds, each indicating that moving directly from hold  $x$  to hold  $y$  is allowed; however, moving directly from  $y$  to  $x$  is not allowed unless the list also includes the pair  $(y, x)$ . Kris needs to figure out a sequence of allowed transitions that uses as many holds as possible, since each new hold increases his score by one point. The rules allow Kris to choose the first and last hold in his climbing route. The rules also allow him to use each hold as many times as he likes; however, only the first use of each hold increases Kris’s score.

- (a) Define the natural graph representing the input. Describe and analyze an algorithm to solve Kris's climbing problem if you are guaranteed that the input graph is a dag.
- (b) Describe and analyze an algorithm to solve Kris's climbing problem with no restrictions on the input graph. Both of your algorithms should output the maximum possible score that Kris can earn.