

Neural nets

$$f(\vec{x}) = [g \ b \ n]$$

good

1 0 0

-

+

bad

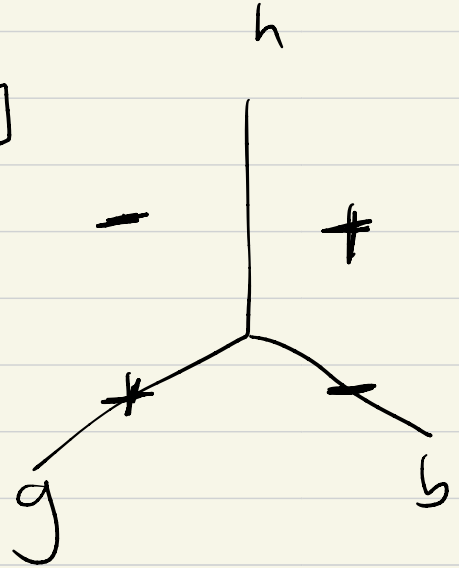
0 1 0

not good

1 0 1

not bad

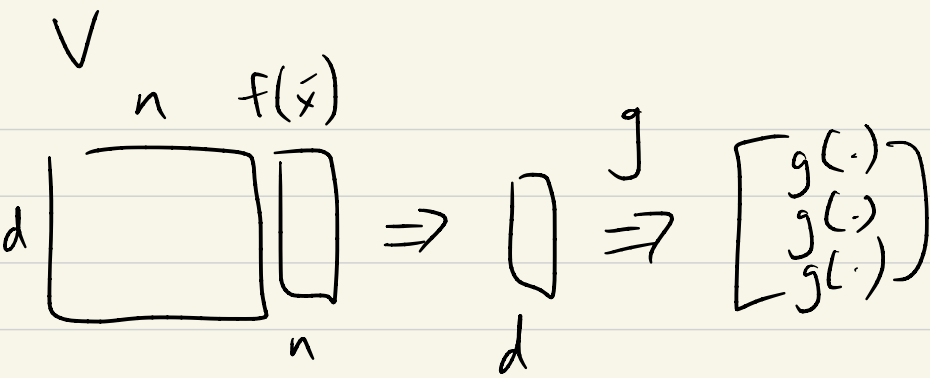
0 1 1



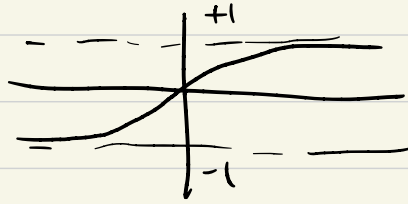
~~$\vec{w}^T f(\vec{x})$~~
 $\vec{w}^T \vec{z}$ → make this not just a simple feature vector
intermediate features

$$\vec{z} = g(\underbrace{V f(\vec{x})}_{\text{BoW, } n \text{ features}})$$

↑ nonlinearity applied to each coordinate
↑ $d \times n$ matrix



$g: \tanh$

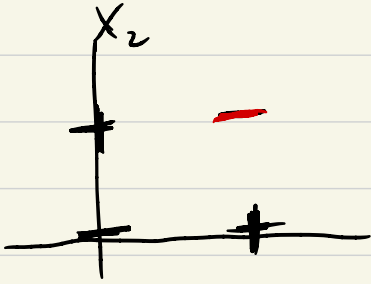


ReLU



V : trainable weights
 g : nonlinearity

XOR:



x_1 I made this up

$f(\vec{x})$	0	0	-
	0	1	+
	1	0	+

$$V = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \end{bmatrix}$$

$$\boxed{\begin{bmatrix} 1 & 1 & - \end{bmatrix}}$$

$$g = \tanh$$

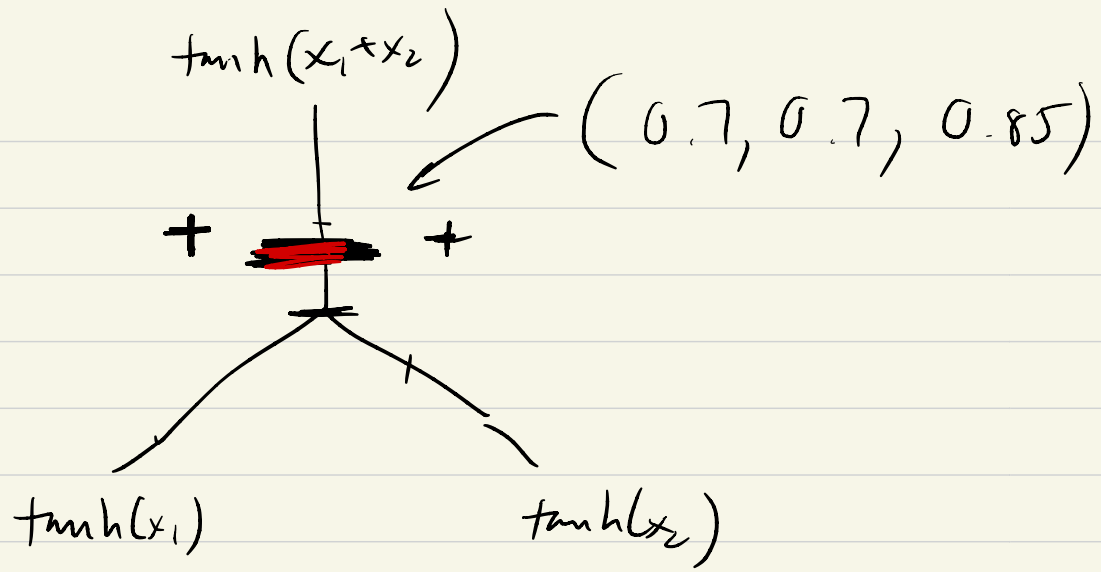
$$V f(\vec{x}) = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \end{bmatrix}_{3 \times 2} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}_2 = \begin{bmatrix} x_1 \\ x_2 \\ x_1 + x_2 \end{bmatrix}$$

$$\begin{bmatrix} \tanh(x_1) \\ \tanh(x_2) \\ \tanh(x_1 + x_2) \end{bmatrix}$$

$$\tanh(0) = 0$$

$$\tanh(1) = 0.7$$

$$\tanh(2) \approx 0.85$$



Classification:

$$\bar{w}^T \bar{z} = \bar{w}^T g(vf(\bar{x}))$$

data is separable in
new space