

# CS388: Natural Language Processing

## Lecture 5: Word Embeddings

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# Administrivia

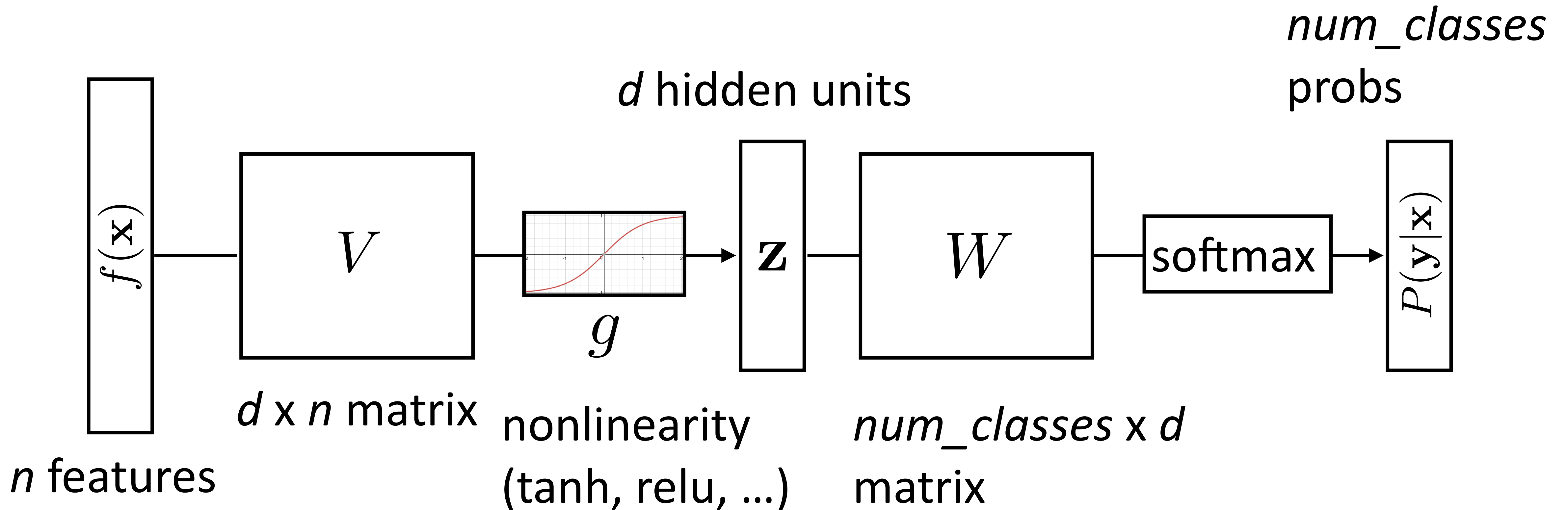
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- ▶ Project 1 due today
- ▶ Project 2 released today; material for it covered Thursday and finished next Tuesday



# Recall: Feedforward NNs

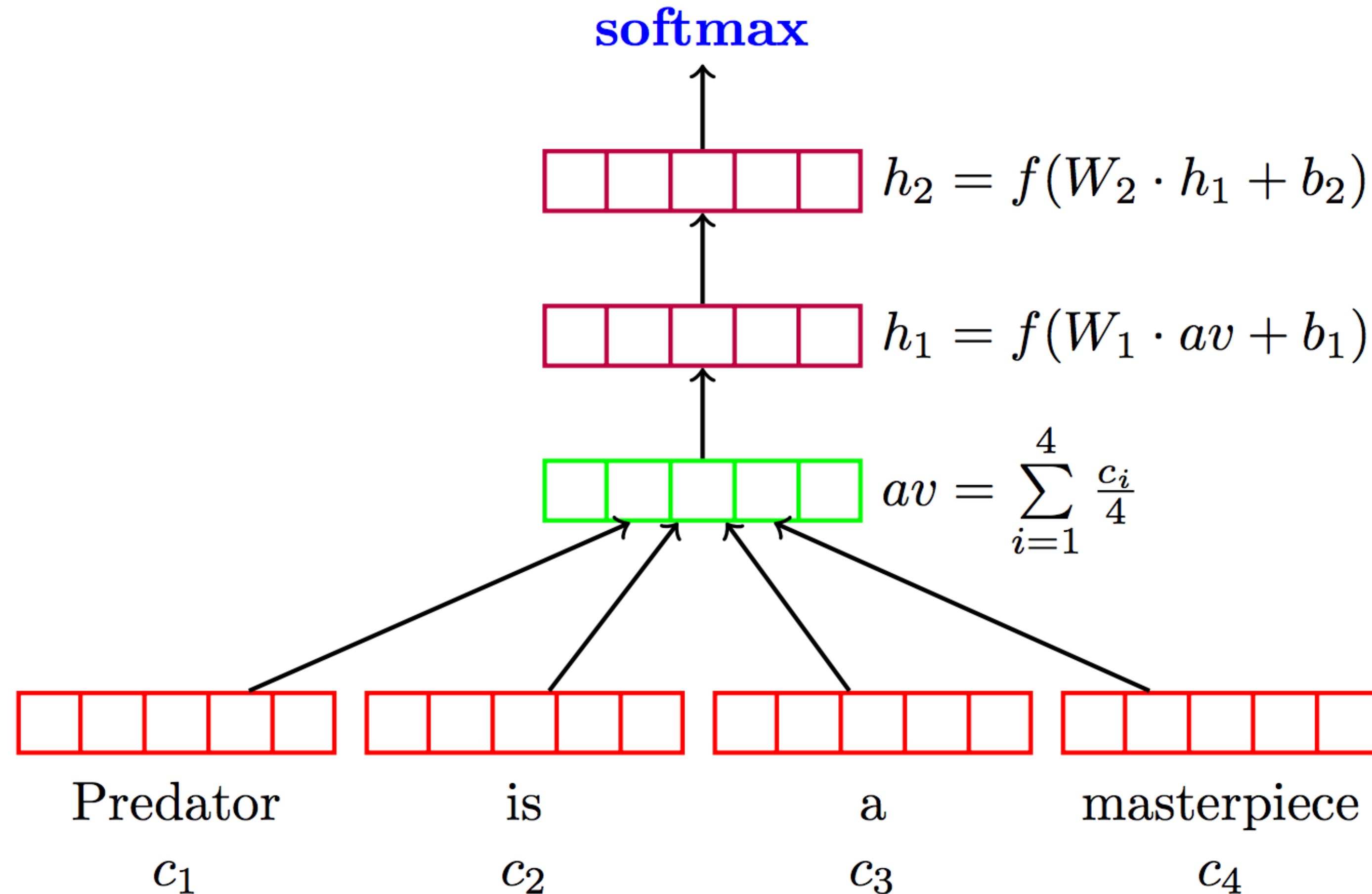
$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$





# Recall: Deep Averaging Networks

- ▶ Deep Averaging Networks: feedforward neural network on average of word embeddings from input





# This Lecture

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- ▶ Word representations
- ▶ Skip-gram
- ▶ GloVe
- ▶ Other word embedding methods
- ▶ Evaluating word embeddings

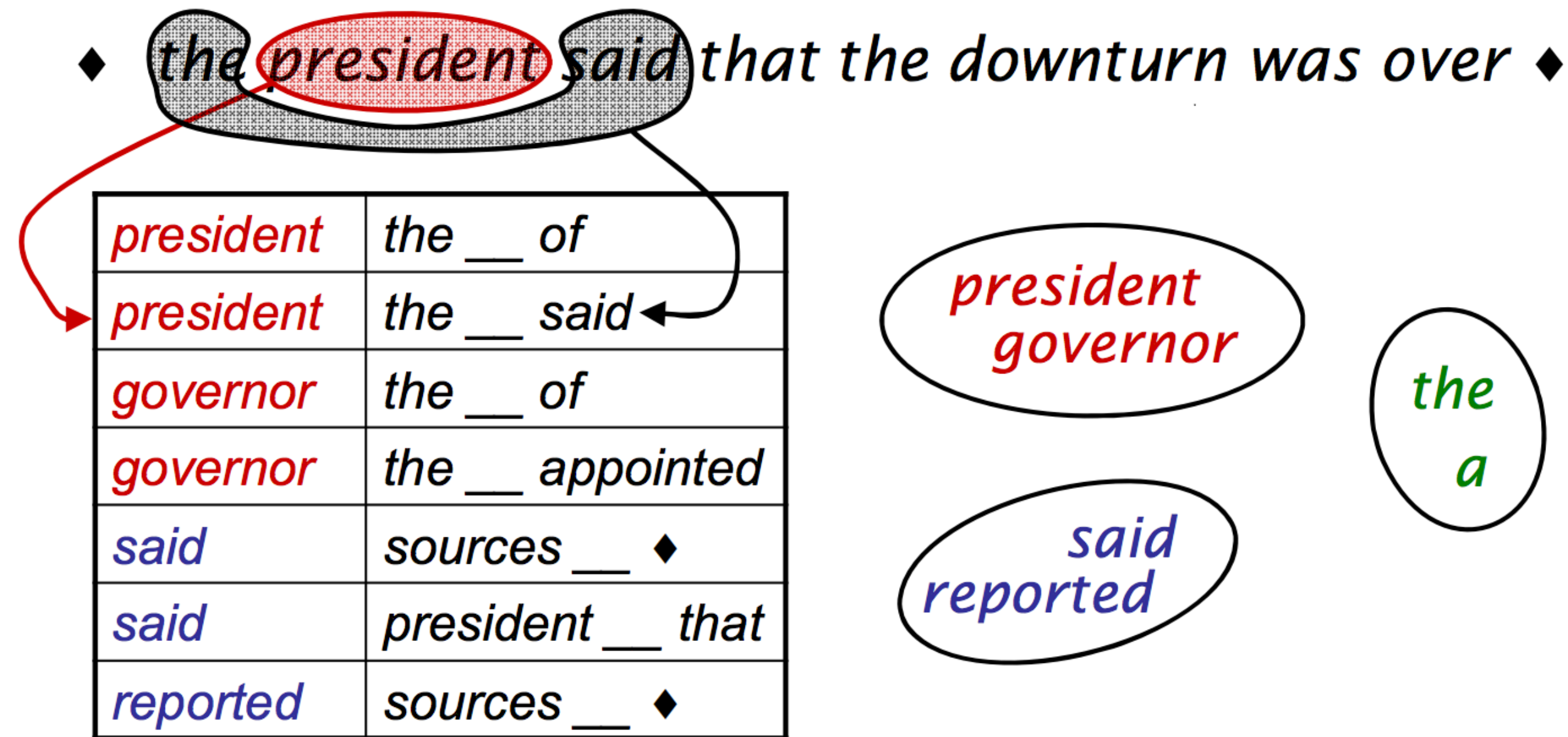
# Word Representations





# Word Representations

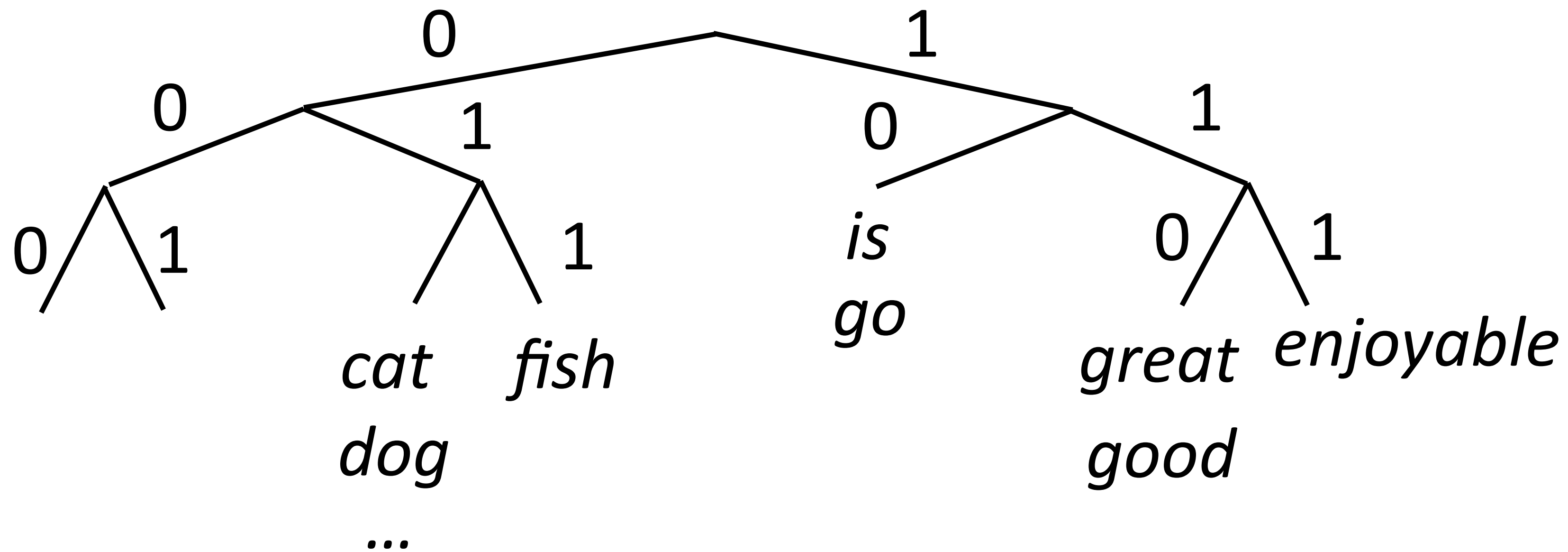
- ▶ Neural networks work very well at continuous data, but words are discrete
- ▶ Continuous model  $\leftrightarrow$  expects continuous semantics from input
- ▶ “You shall know a word by the company it keeps” Firth (1957)





# Discrete Word Representations

- ▶ Brown clusters: hierarchical agglomerative *hard* clustering (each word has one cluster, not some posterior distribution like in mixture models)



- ▶ Maximize  $P(w_i|w_{i-1}) = P(c_i|c_{i-1})P(w_i|c_i)$
  - ▶ Useful features for tasks like NER, not suitable for NNs
- Brown et al. (1992)





# Word Embeddings

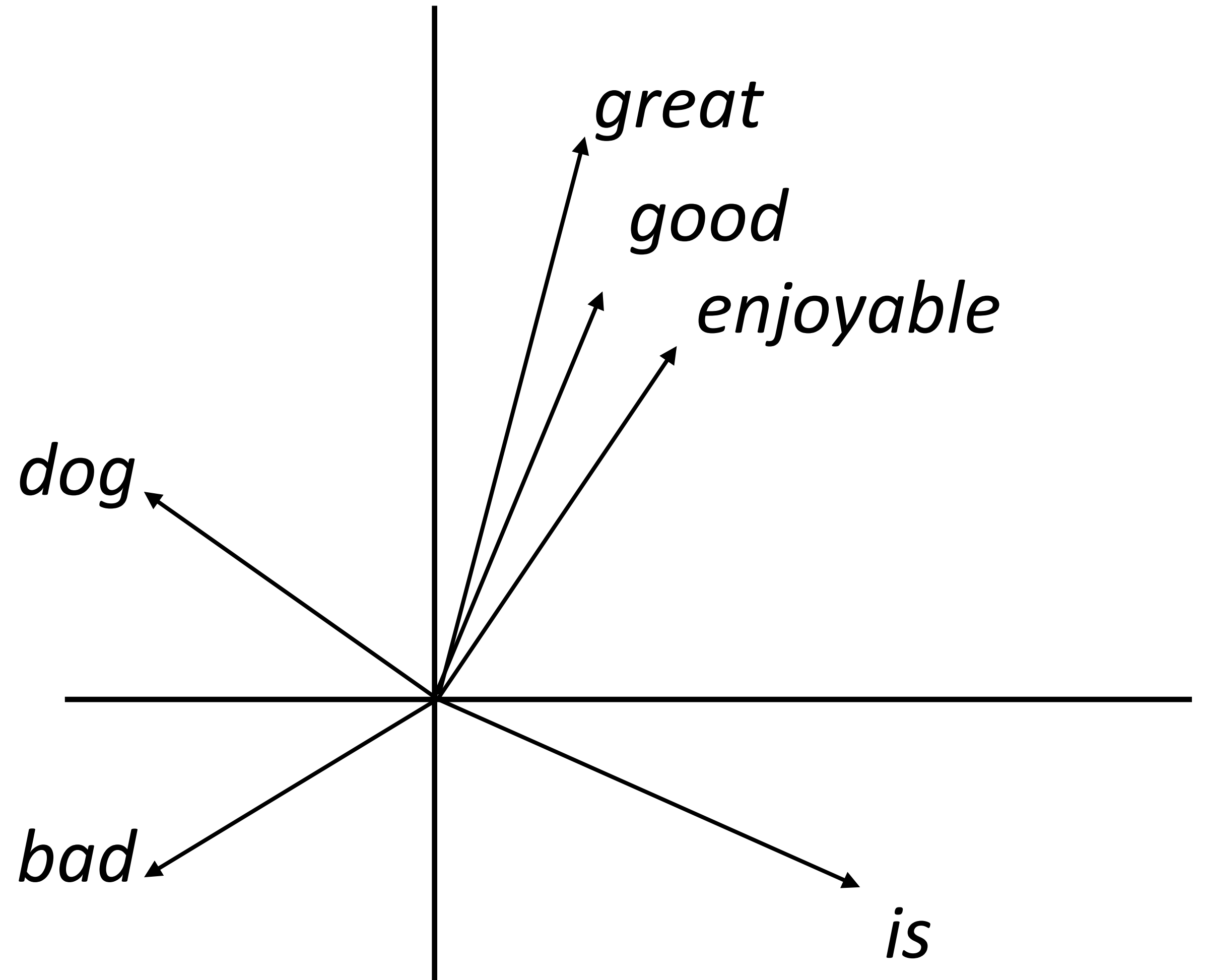
- ▶ Want a vector space where similar words have similar embeddings

*the movie was great*

≈

*the movie was good*

- ▶ Goal: come up with a way to produce these embeddings
- ▶ For each word, want “medium” dimensional vector (50-300 dims) representing it



Skip-gram



# Skip-Gram

- ▶ Input: a corpus of raw text. (Same as the input to “real” language modeling)
- ▶ Output: a set of *embeddings*: a real-valued vector for each word in the vocabulary
- ▶ We are going to learn these by setting up a fake prediction problem: predict a word’s context from that word



*the dog bit the man*

(word = *bit*, context = *dog*)

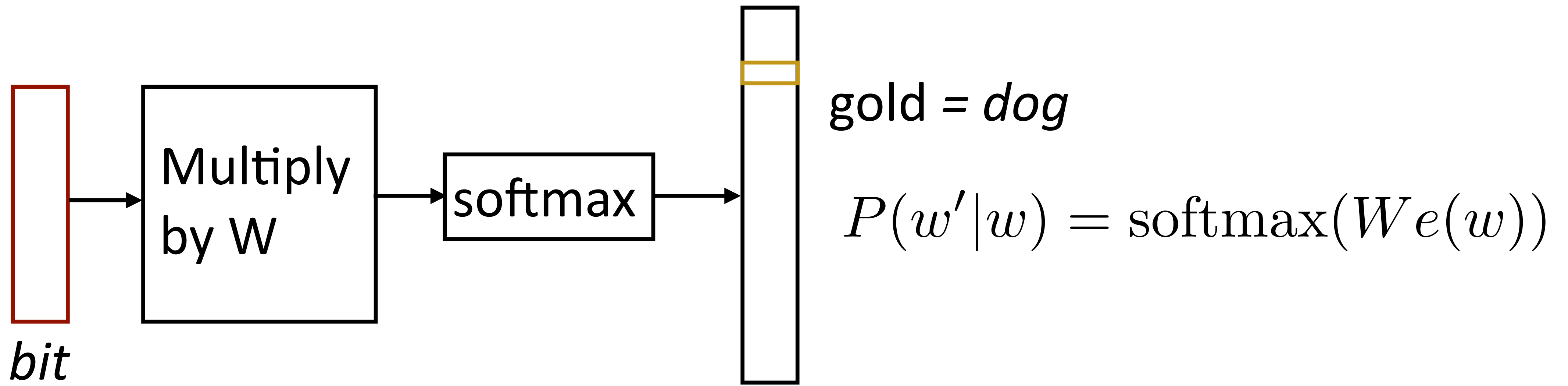
(word = *bit*, context = *the*)



# Skip-Gram

- ▶ Predict one word of context from word

*the dog bit the man*



- ▶ Another training example: *bit* -> *the*
- ▶ Parameters:  $d \times |V|$  **vectors**,  $|V| \times d$  output parameters ( $W$ ) (also usable as vectors!).  $d$  is a hyperparameter



# Using Skip-Gram

- ▶ Context window size: how many words around the “center” word do we look?



$k=1$ : two words of context

$k=2$ : four words of context

- ▶ Advantages/disadvantages of different sizes of  $k$ ?
- ▶ Training: maximize log likelihood of the examples derived given  $k$ , summed over a corpus (but we'll never use the model as is, only its embeddings)
- ▶ Initialization: need to randomly initialize in a reasonable way
- ▶ Vector size: controls capacity of model

Mikolov et al. (2013)

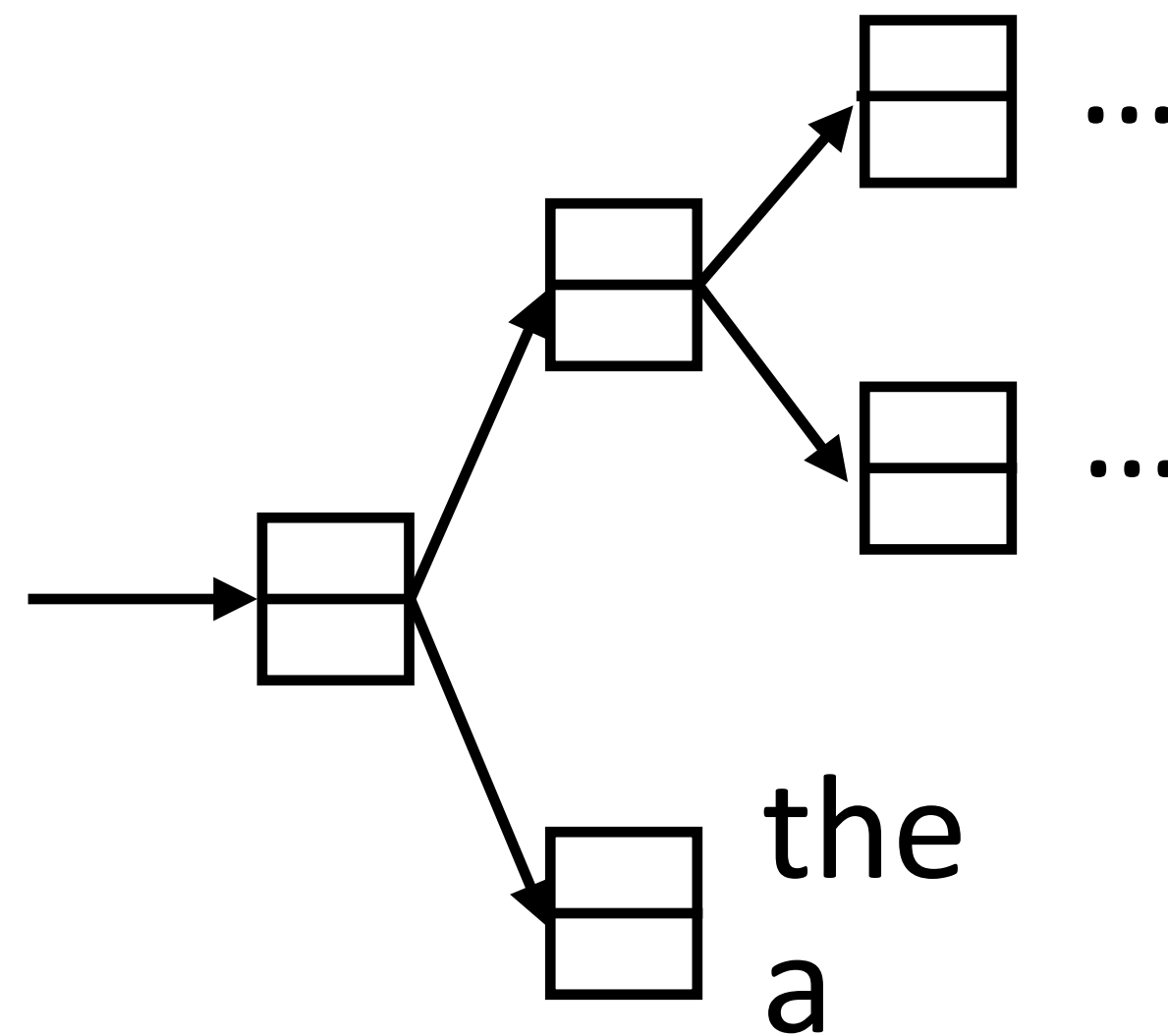
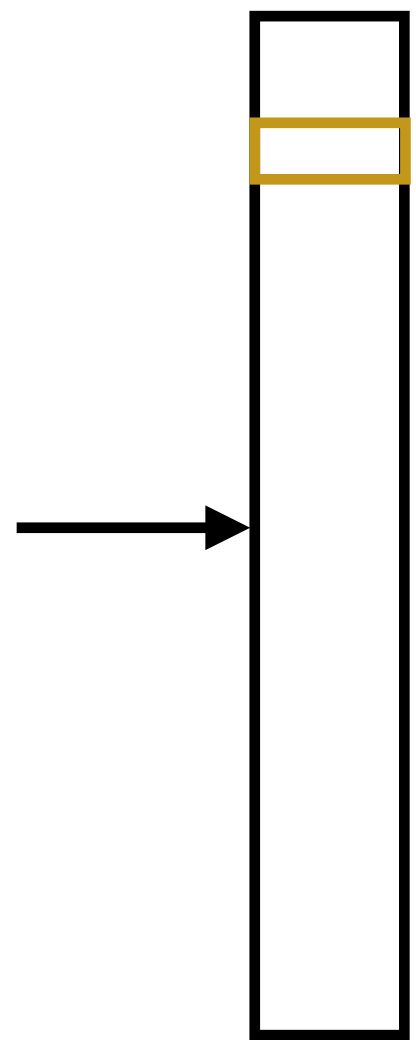




# Hierarchical Softmax

$$P(w'|w) = \text{softmax}(We(w))$$

- ▶ Matmul + softmax over  $|V|$  is very slow to compute for skip-gram



- ▶ Huffman encode vocabulary, use binary classifiers to decide which branch to take
- ▶  $\log(|V|)$  binary decisions

- ▶ Standard softmax:  
 $|V|$  dot products  
of size  $d$

- ▶ Hierarchical softmax:  
 $\log(|V|)$  dot products of size  $d$ ,  
 $|V| \times d$  parameters



# Skip-Gram with Negative Sampling

- ▶ Take (word, context) pairs and classify them as “real” or not. Create random negative examples by sampling from unigram distribution

$(bit, the) \Rightarrow +1$

$(bit, cat) \Rightarrow -1$

$(bit, a) \Rightarrow -1$

$(bit, fish) \Rightarrow -1$

$$P(y = 1|w, c) = \frac{e^{w \cdot c}}{e^{w \cdot c} + 1}$$

words in similar contexts select for similar  $c$  vectors

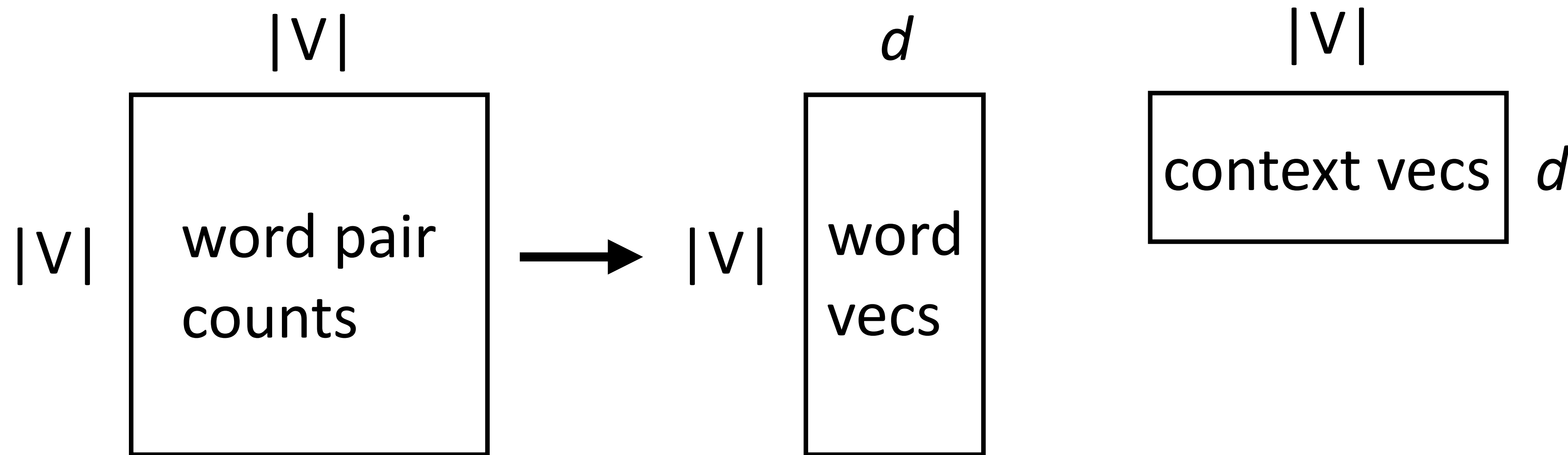
- ▶  $d \times |V|$  vectors,  $d \times |V|$  context vectors (same # of params as before)

- ▶ Objective =  $\log P(y = 1|w, c) + \frac{1}{k} \sum_{i=1}^n \log P(y = 0|w_i, c)$  ↙ sampled



# Connections with Matrix Factorization

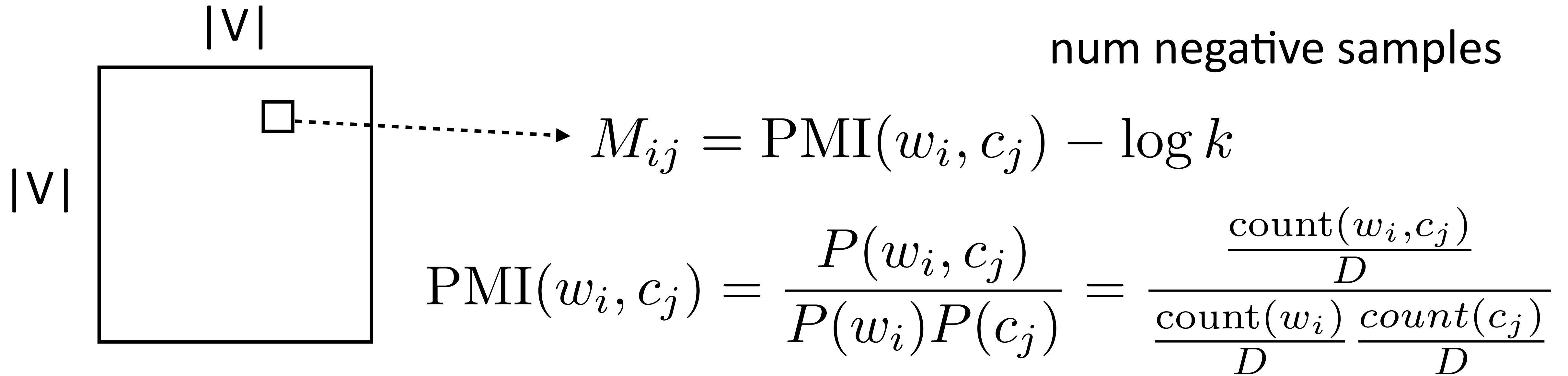
- ▶ Skip-gram model looks at word-word co-occurrences and produces two types of vectors



- ▶ Looks almost like a matrix factorization...



# Skip-Gram as Matrix Factorization



Skip-gram objective *exactly* corresponds to factoring this matrix:

- ▶ *If* we sample negative examples from the unigram distribution over words
- ▶ ...and it's a *weighted* factorization problem (weighted by word freq)

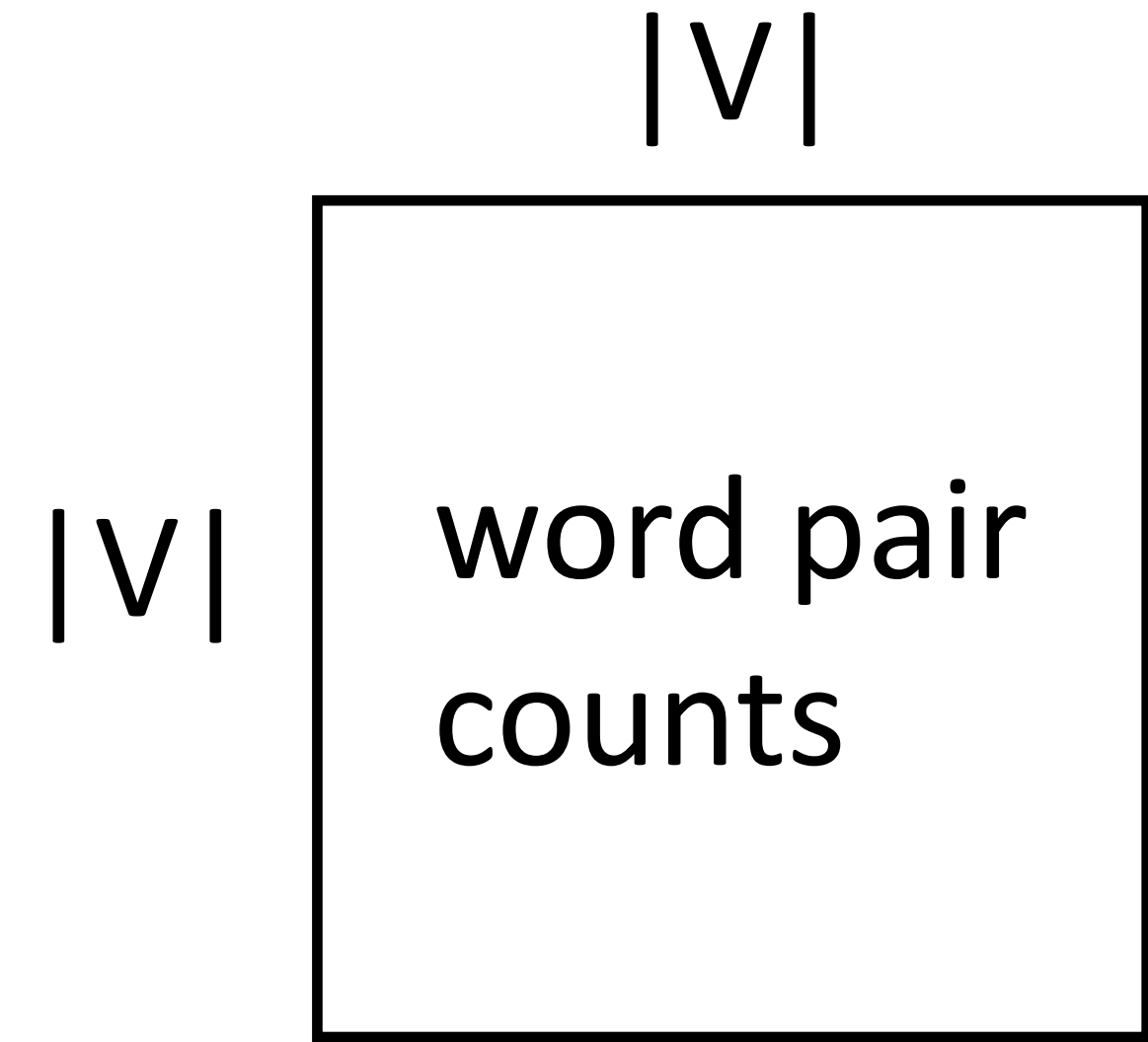
GloVe





# GloVe (Global Vectors)

- ▶ Also operates on counts matrix, weighted regression on the log co-occurrence matrix



- ▶ Objective =  $\sum_{i,j} f(\text{count}(w_i, c_j)) (w_i^\top c_j + a_i + b_j - \log \text{count}(w_i, c_j))^2$
- ▶ Constant in the dataset size (just need counts), quadratic in voc size
- ▶ By far the most common word vectors used today (30000+ citations)



# GloVe (Global Vectors): Example

► Objective =  $\sum_{i,j} f(\text{count}(w_i, c_j)) (w_i^\top c_j + a_i + b_j - \log \text{count}(w_i, c_j))^2$

■ ■ ■ ■  
*the dog cat ran*

<span style="color: black;">■</span> <i>the</i>	0	200	200	0
<span style="color: black;">■</span> <i>dog</i>	200	0	0	15
<span style="color: black;">■</span> <i>cat</i>	200	0	0	15
<span style="color: black;">■</span> <i>ran</i>	0	15	15	0

Linear regression with 6 pairs:  
each element is plugged into the above equation

■ ■ + constant = log count of pair

(made up values — matrix will generally be symmetric, though)

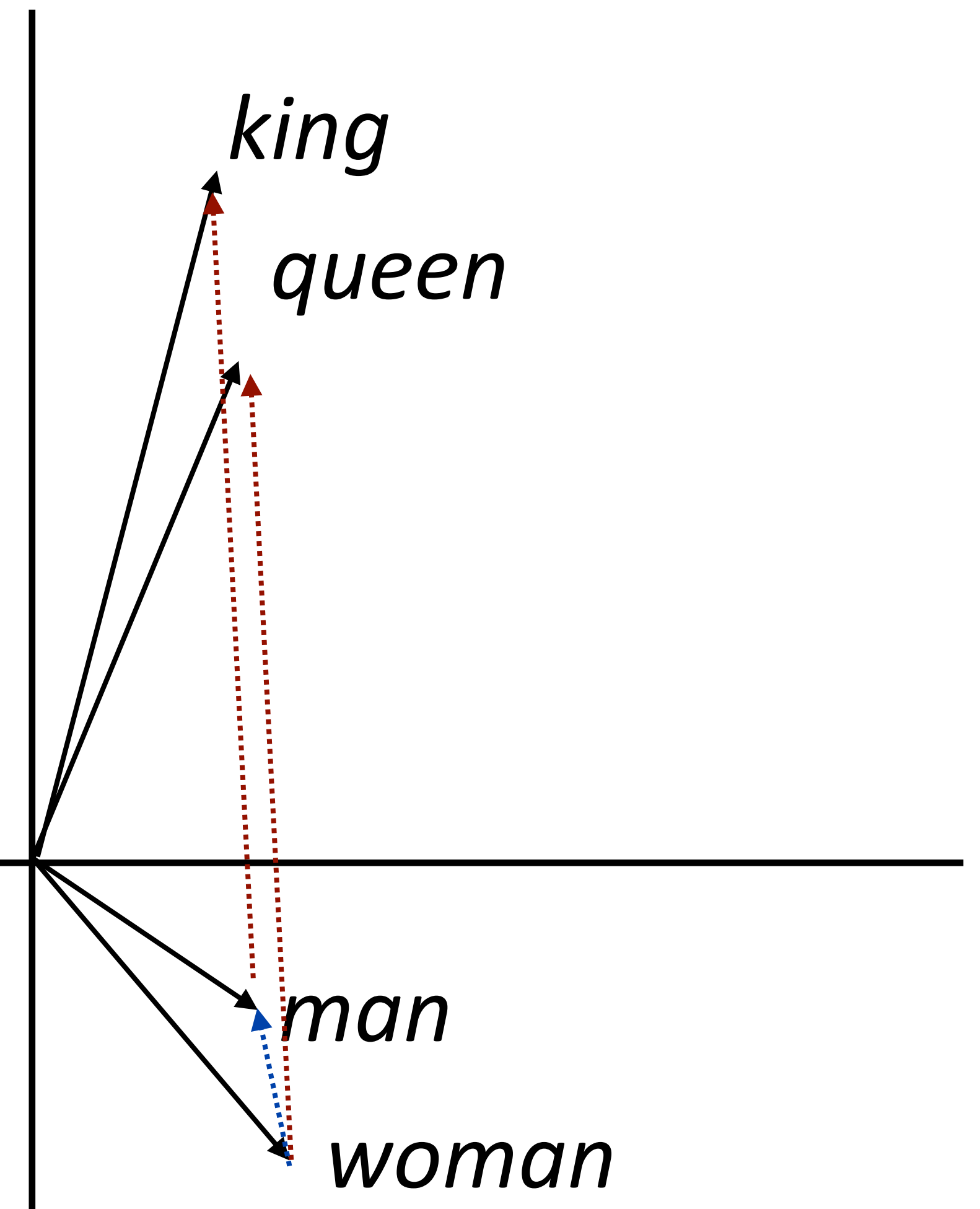


# Analogies

$(king - man) + woman = queen$

$king + (woman - man) = queen$

- ▶ Why would this be?
- ▶ woman - man captures the difference in the contexts that these occur in
- ▶ Dominant change: more “he” with man and “she” with woman — similar to difference between king and queen
- ▶ Can evaluate on this as well





# GloVe Motivation

Table 1: Co-occurrence probabilities for target words *ice* and *steam* with selected context words from a 6 billion token corpus. Only in the ratio does noise from non-discriminative words like *water* and *fashion* cancel out, so that large values (much greater than 1) correlate well with properties specific to ice, and small values (much less than 1) correlate well with properties specific of steam.

Probability and Ratio	$k = solid$	$k = gas$	$k = water$	$k = fashion$
$P(k ice)$	$1.9 \times 10^{-4}$	$6.6 \times 10^{-5}$	$3.0 \times 10^{-3}$	$1.7 \times 10^{-5}$
$P(k steam)$	$2.2 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.2 \times 10^{-3}$	$1.8 \times 10^{-5}$
$P(k ice)/P(k steam)$	8.9	$8.5 \times 10^{-2}$	1.36	0.96

- GloVe objective is derived to preserve regularities in cooccurrence of words with other words

$$F \left( (w_i - w_j)^T \tilde{w}_k \right) = \frac{P_{ik}}{P_{jk}}$$

# Other Methods





# fastText: Sub-word Embeddings

- ▶ Same as SGNS, but break words down into n-grams with  $n = 3$  to  $6$

where:

3-grams: <wh, whe, her, ere, re>

4-grams: <whe, wher, here, ere> ,

5-grams: <wher, where, here> ,

6-grams: <where, where>

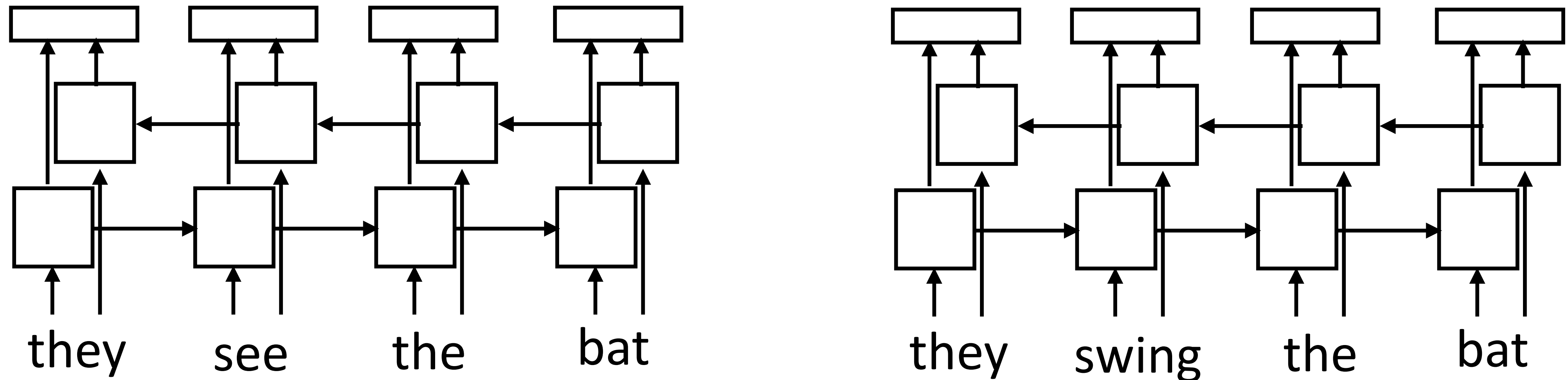
- ▶ Replace  $w \cdot c$  in skip-gram computation with  $\left( \sum_{g \in \text{ngrams}} w_g \cdot c \right)$

- ▶ Advantages?



# Preview: Context-dependent Embeddings

- ▶ How to handle different word senses? One vector for *bat*



- ▶ Train a neural language model to predict the next word given previous words in the sentence, use its internal representations as word vectors
- ▶ *Context-sensitive* word embeddings: depend on rest of the sentence
- ▶ *Huge* improvements across nearly all NLP tasks over GloVe

Peters et al. (2018)



# Compositional Semantics

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- ▶ What if we want embedding representations for whole sentences?
- ▶ *Skip-thought* vectors (Kiros et al., 2015), similar to skip-gram generalized to a sentence level (more later)
- ▶ Is there a way we can compose vectors to make sentence representations?  
Summing?
- ▶ Will return to this in a few weeks as we move on to syntax and semantics



# Using Word Embeddings

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- ▶ Approach 1: learn embeddings as parameters from your data
  - ▶ Often works pretty well
- ▶ Approach 2: initialize using GloVe, keep fixed
  - ▶ Faster because no need to update these parameters
- ▶ Approach 3: initialize using GloVe, fine-tune
  - ▶ Works best for some tasks

# Evaluating Word Embeddings



# Evaluating Word Embeddings

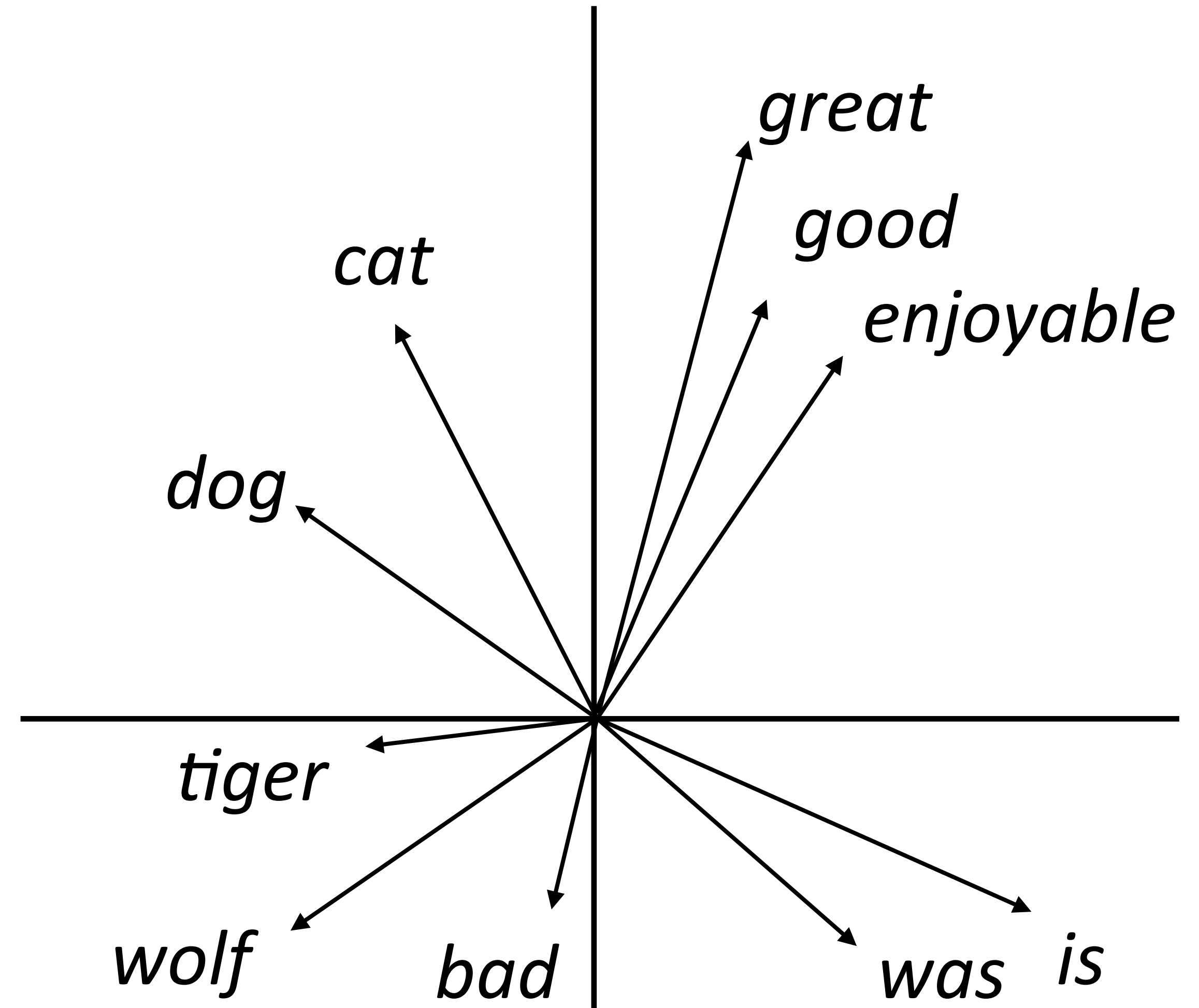
▶ What properties of language should word embeddings capture?

▶ Similarity: similar words are close to each other

▶ Analogy:

good is to best as smart is to ???

Paris is to France as Tokyo is to ???







# Similarity

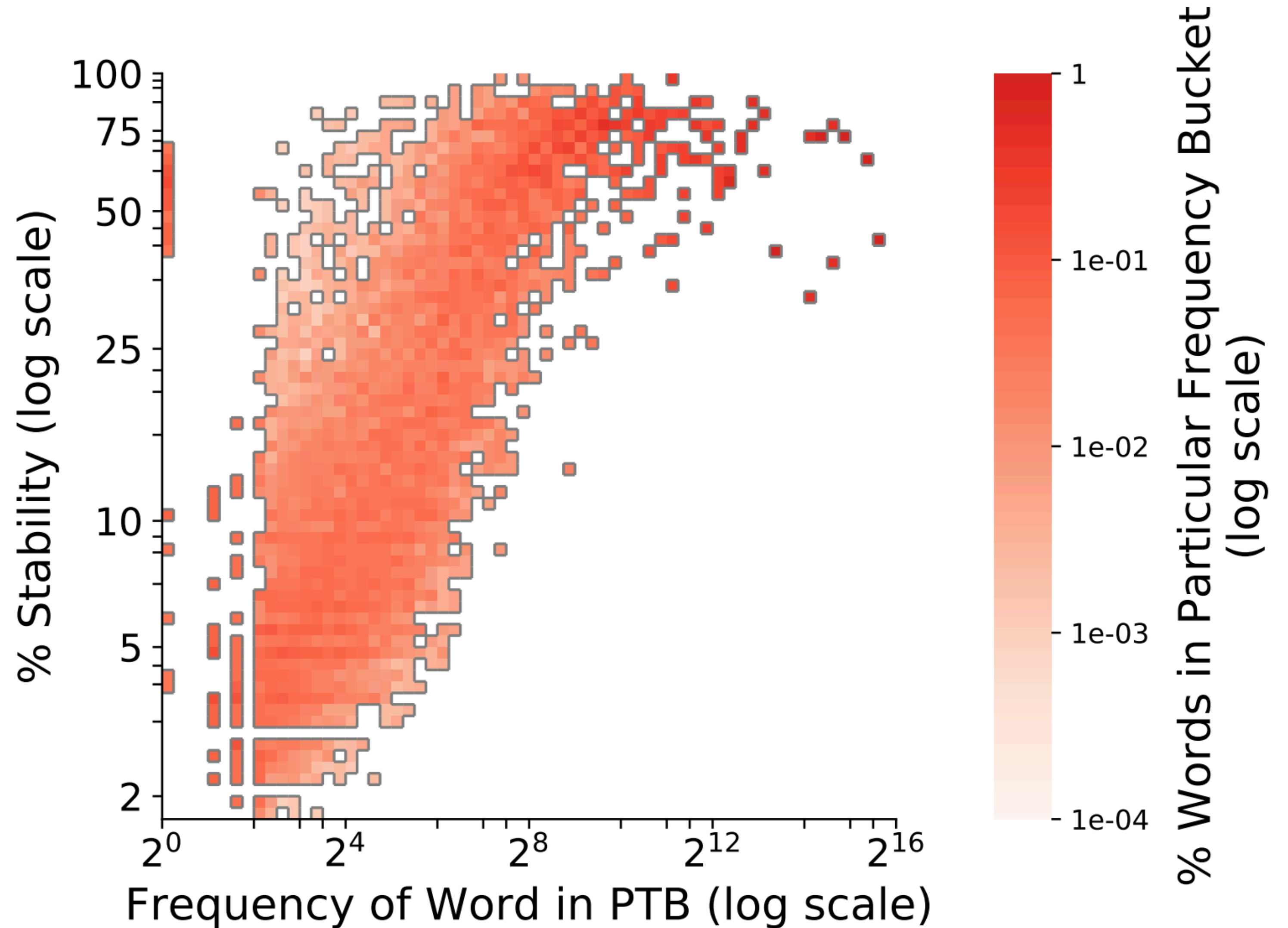
Method	WordSim Similarity	WordSim Relatedness	Bruni et al. MEN	Radinsky et al. M. Turk	Luong et al. Rare Words	Hill et al. SimLex
PPMI	.755	<b>.697</b>	.745	.686	.462	.393
SVD	<b>.793</b>	.691	<b>.778</b>	.666	<b>.514</b>	.432
SGNS	<b>.793</b>	.685	.774	<b>.693</b>	.470	<b>.438</b>
GloVe	.725	.604	.729	.632	.403	.398

- ▶ SVD = singular value decomposition on PMI matrix
- ▶ GloVe does not appear to be the best when experiments are carefully controlled, but it depends on hyperparameters + these distinctions don't matter in practice



# Stability

- ▶ To what extent are the relationships captured by word embeddings consistent?
- ▶ Stability: percent overlap between nearest neighbors in embedding space if you retrain embeddings from different initialization

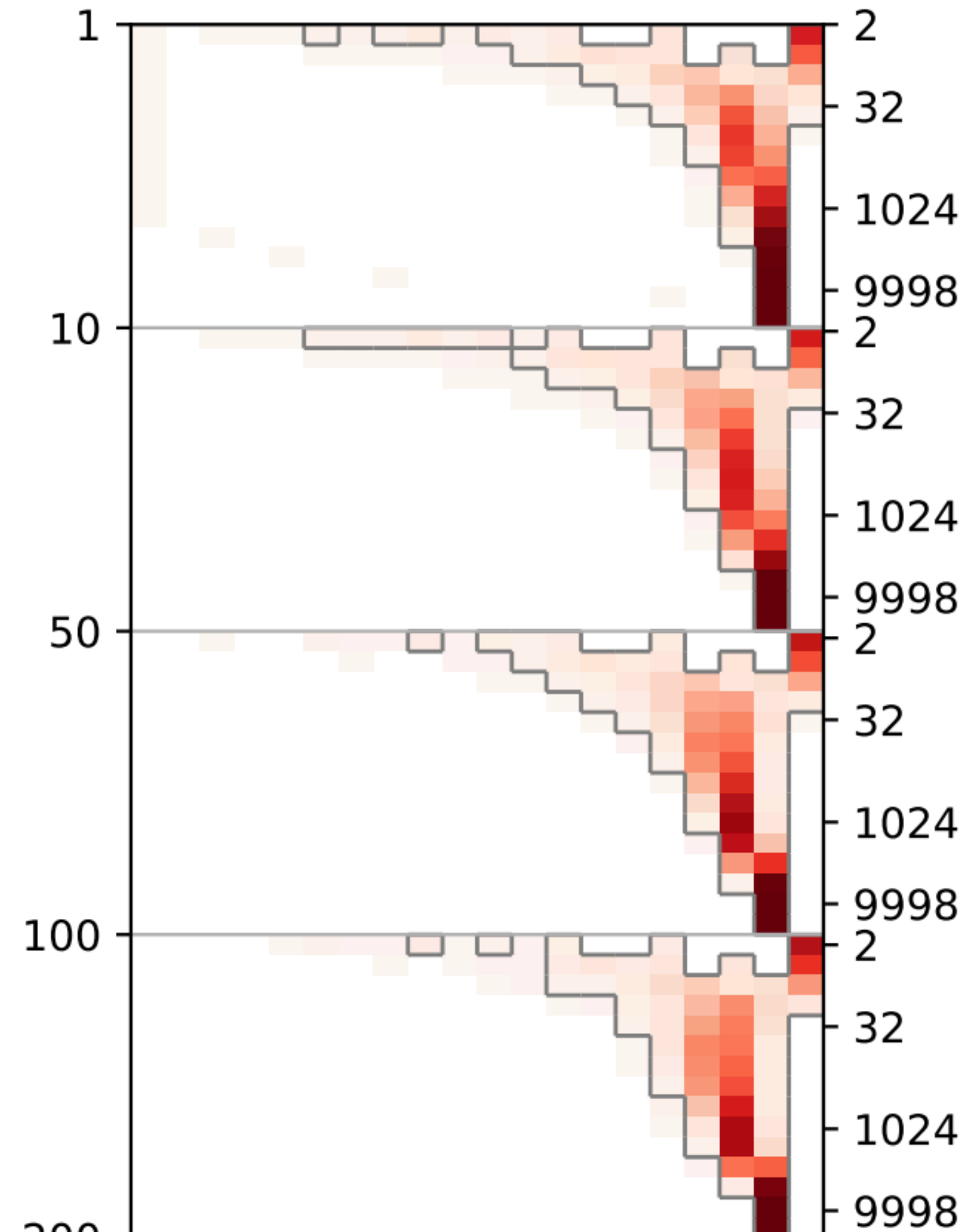


Burdick et al. (2018)



# Stability: GloVe

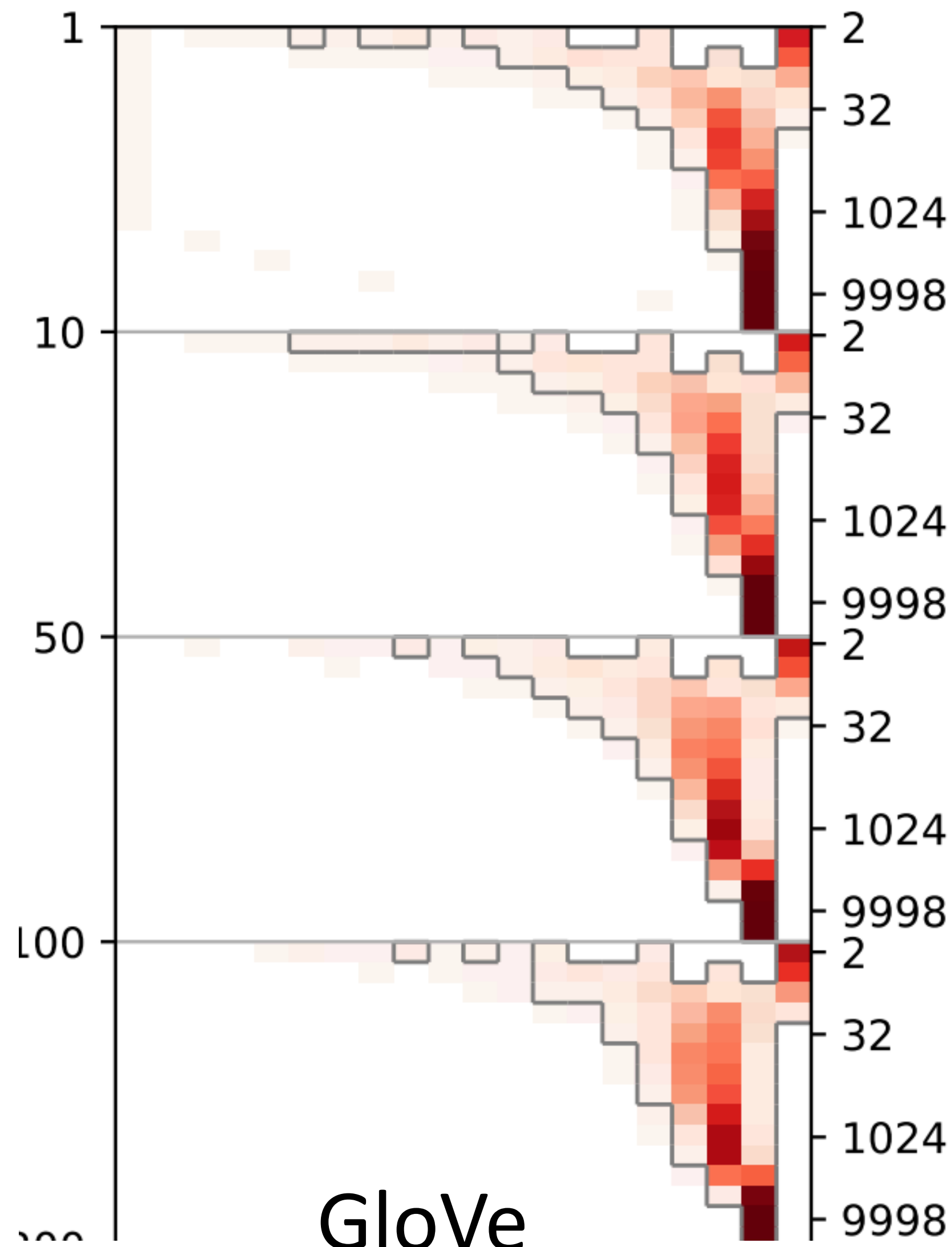
- ▶ Left y-axis: bucketed corpus frequency
- ▶ Right y-axis: number of neighbors
- ▶ x-axis: percent of neighbors stable across samples
- ▶ Being all the way to the right is better (most neighbors are stable)



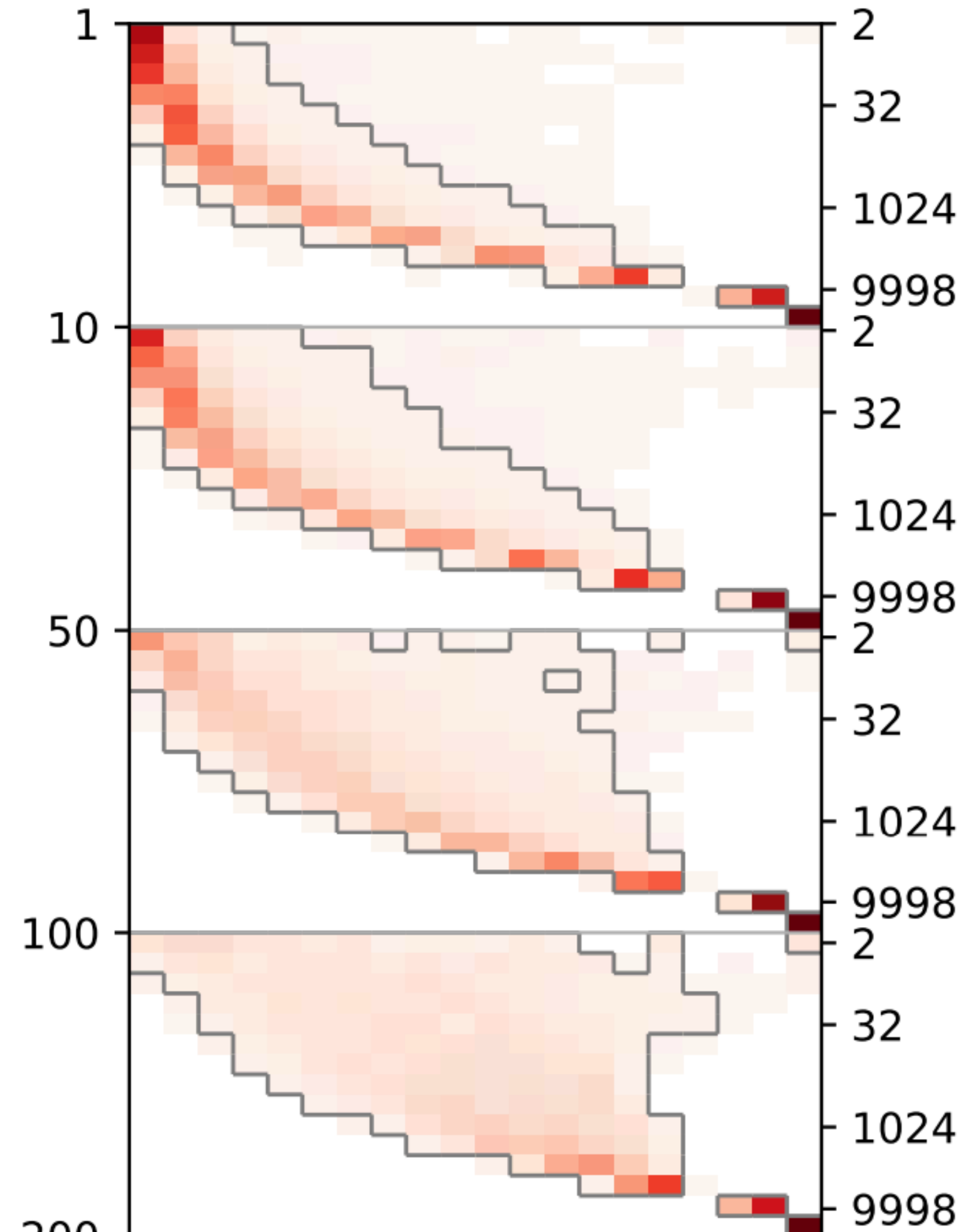
Burdick et al. (2018)



# GloVe vs. word2vec: w2v much less stable!



GloVe



word2vec

Burdick et al. (2018)





# What can go wrong with word embeddings?

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- ▶ What's wrong with learning a word's "meaning" from its usage?

*Ukraine's deputy defense minister resigns amid corruption allegations*

*From 2015 through 2020, there were at least 2,070 unintentional shootings by children under 18 in the US, according to a report from Everytown. Those shootings resulted in 765 deaths and 1,366 injuries.*

*Convicted child sex trafficker Ghislaine Maxwell has said a decades-old photograph of Prince Andrew with his sexual abuse accuser Virginia Giuffre is "fake," in a series of interviews from prison.*



# What do we mean by bias?

- ▶ Identify *she* - *he* axis in word vector space, project words onto this axis

- Extreme *she* occupations**
- |                 |                       |                        |
|-----------------|-----------------------|------------------------|
| 1. homemaker    | 2. nurse              | 3. receptionist        |
| 4. librarian    | 5. socialite          | 6. hairdresser         |
| 7. nanny        | 8. bookkeeper         | 9. stylist             |
| 10. housekeeper | 11. interior designer | 12. guidance counselor |

- Extreme *he* occupations**
- |                |                   |                |
|----------------|-------------------|----------------|
| 1. maestro     | 2. skipper        | 3. protege     |
| 4. philosopher | 5. captain        | 6. architect   |
| 7. financier   | 8. warrior        | 9. broadcaster |
| 10. magician   | 11. fighter pilot | 12. boss       |

## Bolukbasi et al. (2016)

- ▶ Nearest neighbor of  $(b - a + c)$

<b>Racial Analogies</b>	
black → homeless	caucasian → servicemen
caucasian → hillbilly	asian → suburban
asian → laborer	black → landowner
<b>Religious Analogies</b>	
jew → greedy	muslim → powerless
christian → familial	muslim → warzone
muslim → uneducated	christian → intellectually

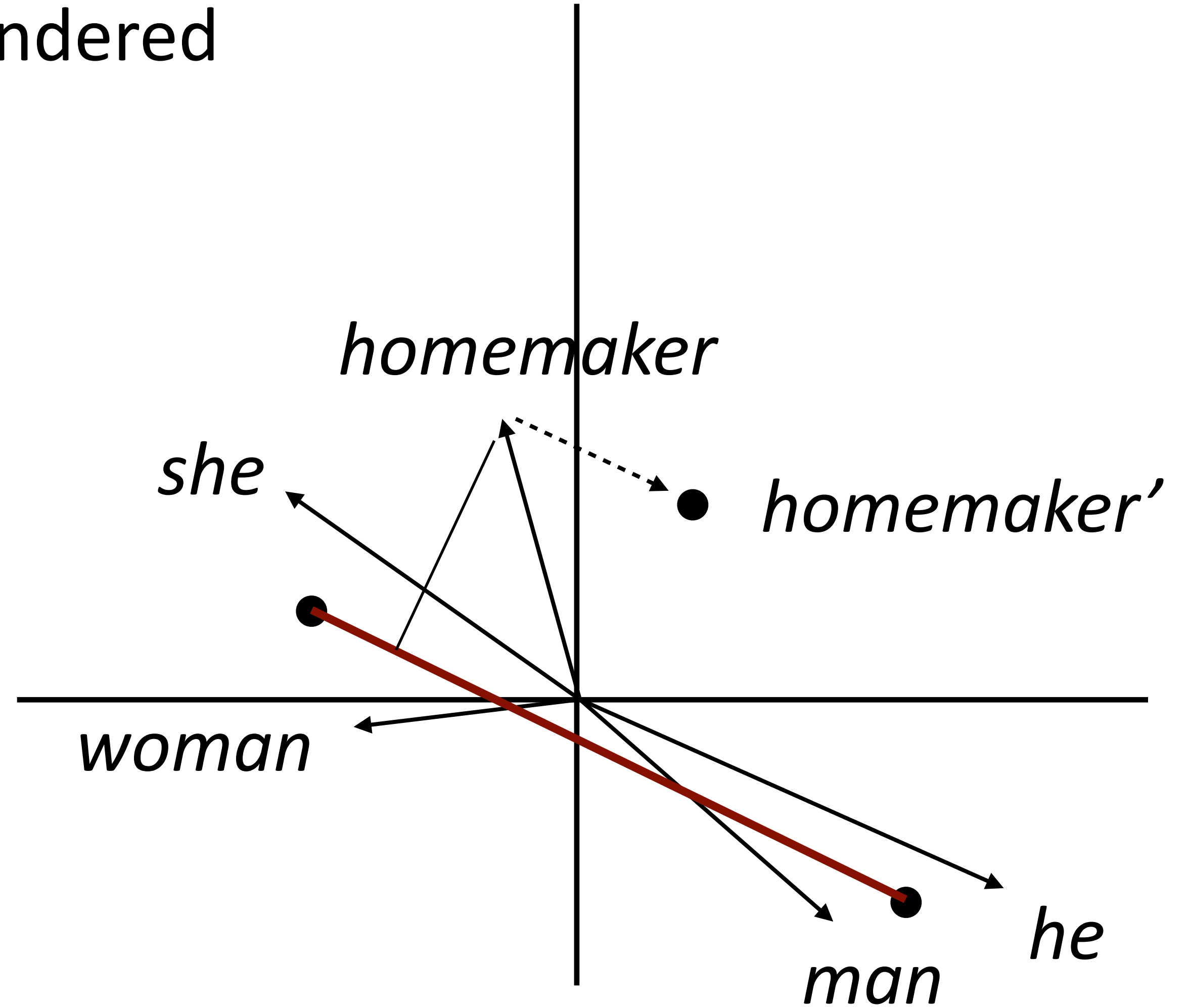
## Manzini et al. (2019)





# Debiasing

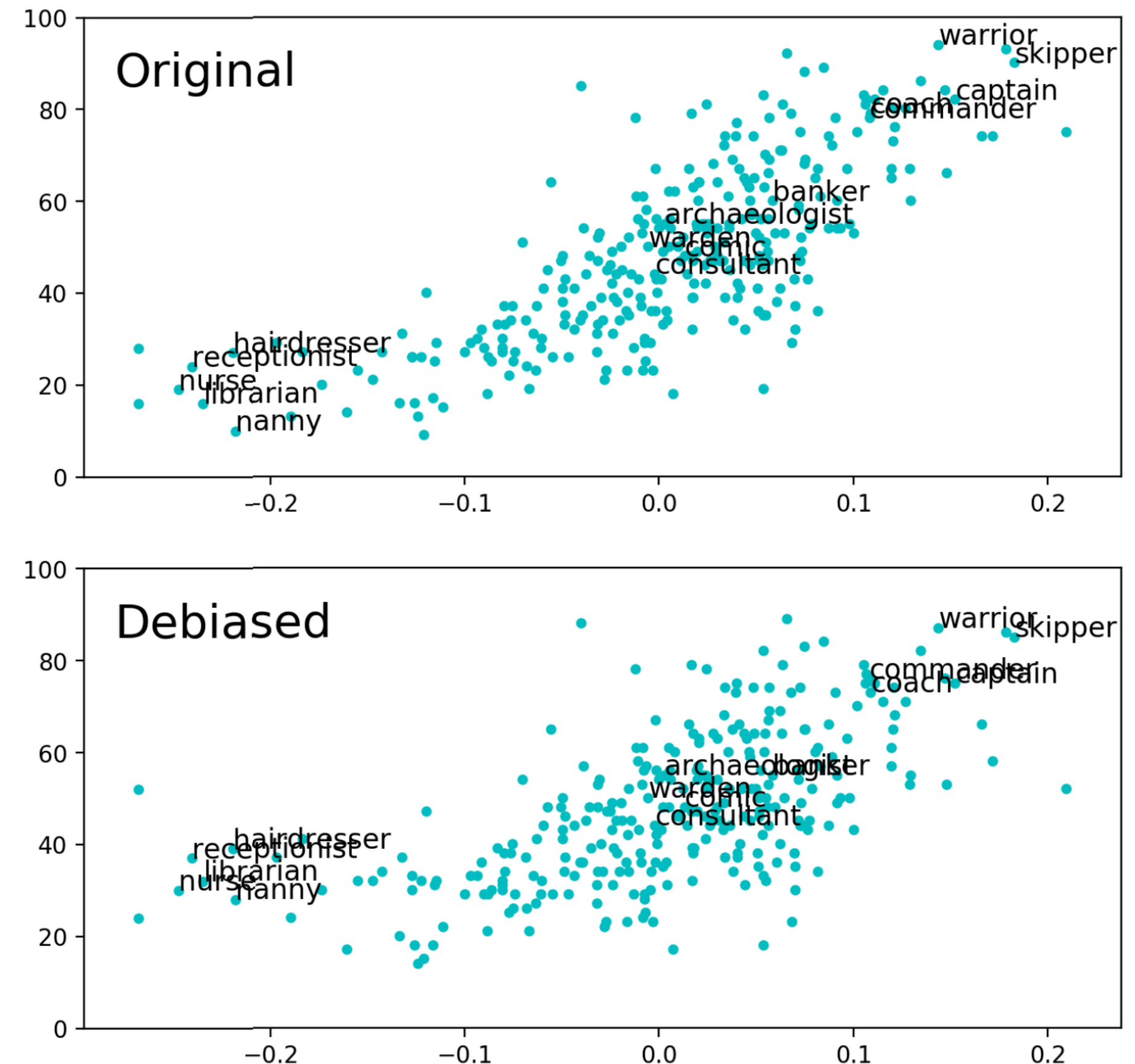
- ▶ Identify gender subspace with gendered words
- ▶ Project words onto this subspace
- ▶ Subtract those projections from the original word





# Hardness of Debiasing

- ▶ Not that effective...and the male and female words are still clustered together
- ▶ Bias pervades the word embedding space and isn't just a local property of a few words



(a) The plots for HARD-DEBIASED embedding, before (top) and after (bottom) debiasing.



# Takeaways

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- ▶ Word vectors: learning word  $\rightarrow$  context mappings has given way to matrix factorization approaches (constant in dataset size)
- ▶ Lots of pretrained embeddings work well in practice, they capture some desirable properties
- ▶ Even better: context-sensitive word embeddings (ELMo)
- ▶ Next time: language modeling and Transformers