

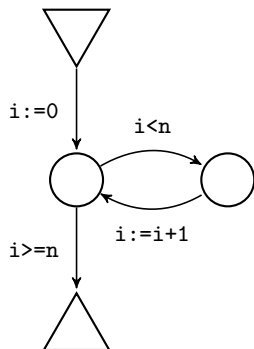
Upper and Lower Loop Bound Estimation by Symbolic Execution and Loop Acceleration

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Loop Bound Analysis



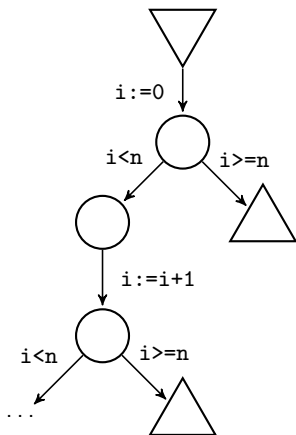
Upper loop bound: $\max\{n, 0\}$

Lower loop bound: $\max\{n, 0\}$

Usage:

- worst case execution time
- memory consumption
- complexity analysis
- ...

Symbolic Execution - Path Explosion



Path conditions:

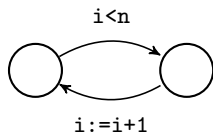
$$\varphi_1 \equiv 0 \geq n$$

$$\varphi_2 \equiv 0 < n \wedge 1 \geq n$$

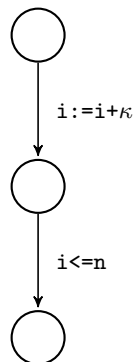
$$\varphi_3 \equiv \dots$$

\dots

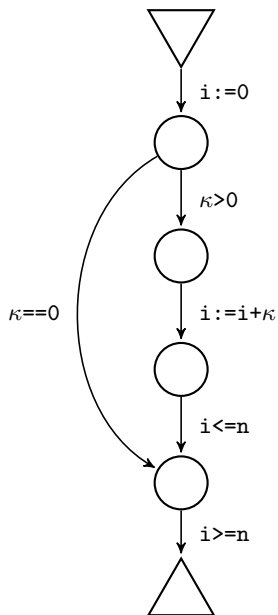
Loop Acceleration



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Combination



Path conditions:

$$\varphi_1 \equiv \kappa = 0 \wedge 0 \geq n$$

$$\varphi_2 \equiv \kappa > 0 \wedge \kappa \leq n \wedge \kappa \geq n$$

$$\implies \kappa = \mathbf{max}\{n, 0\}$$