

# Supplement to Lecture 16

## Global Illumination: View Dependent



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Notes and figures from *Ed Angel: Interactive Computer  
Graphics, 6<sup>th</sup> Ed., 2012* © Addison Wesley  
University of Texas at Austin Jan 2010

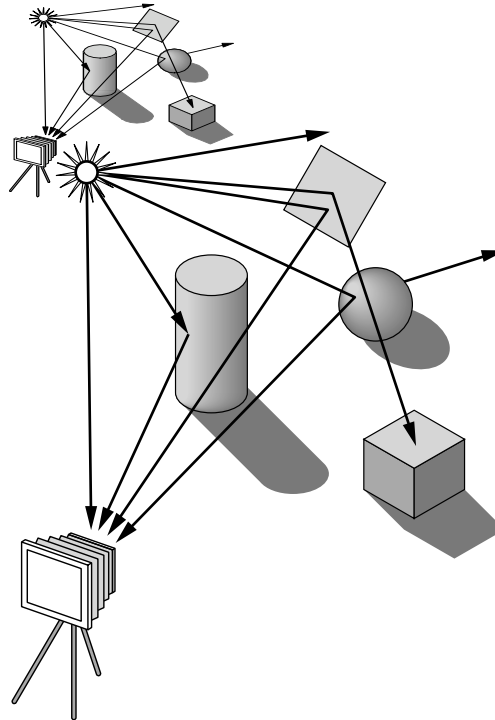
# Local vs Global Illumination

- OpenGL is based on a pipeline model in which primitives are rendered one at time
  - No shadows (except by tricks or multiple renderings)
  - No multiple reflections
- Global approaches
  - Rendering equation
  - Ray tracing
  - Radiosity



# Ray Tracing/Casting-1

- Follow rays of light from a point source
- Can account for reflection and transmission

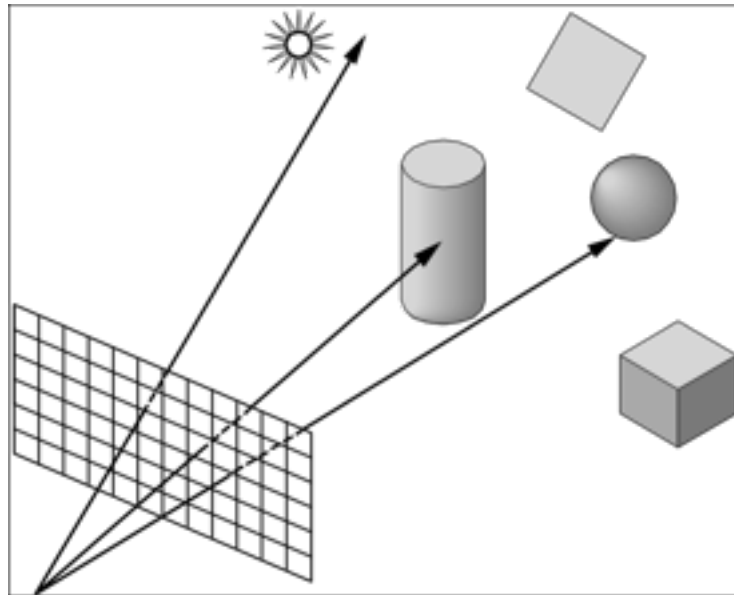


- However, scattering produces many (infinite) additional rays



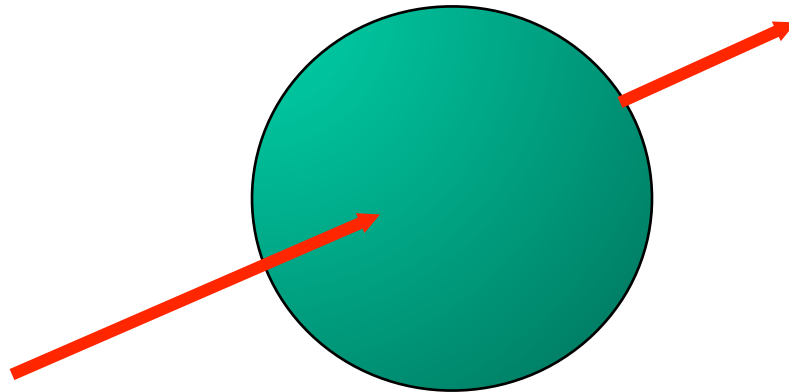
# Ray Tracing/Casting-2

- Only rays that reach the eye matter
- Reverse direction and cast rays
- Need at least one ray per pixel



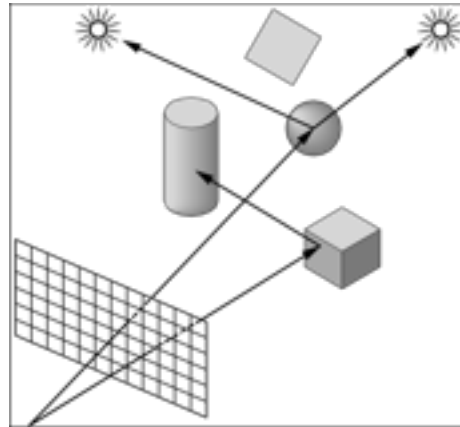
# Ray Tracing/Casting a Sphere

- Ray is parametric
- Sphere is quadric
- Resulting equation is a scalar quadratic equation which gives entry and exit points of ray (or no solution if ray misses)



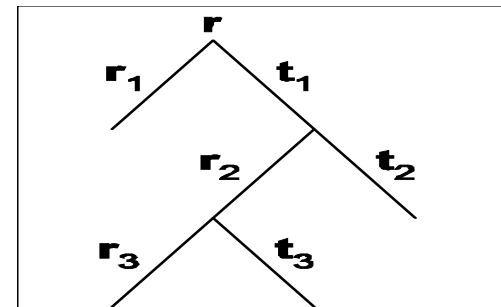
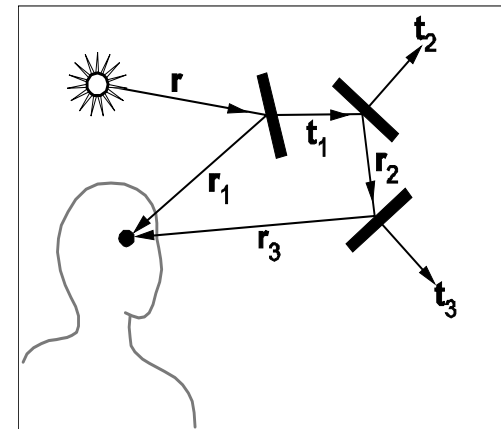
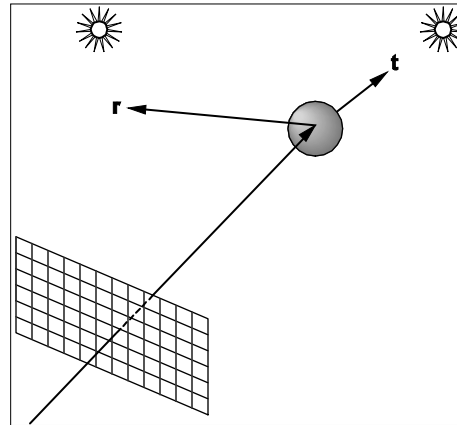
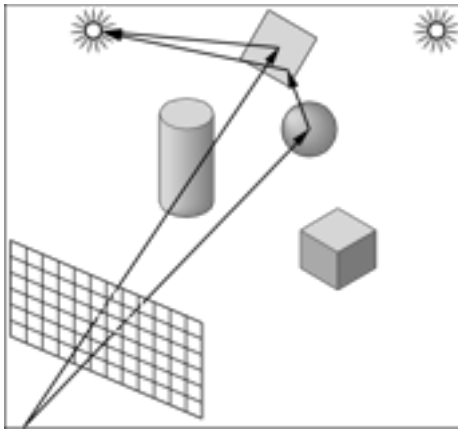
# Shadow Rays

- Even if a point is visible, it will not be lit unless we can see a light source from that point
- Cast shadow or feeler rays



# Reflection/Transmission

- Must follow shadow rays off reflecting or transmitting surfaces - Ray Trees
- Ray Tree Traversal - Process is recursive



# Diffuse Surfaces

- Theoretically the scattering at each point of intersection generates an infinite number of new rays that should be traced
- In practice, we only trace the transmitted and reflected rays but use the Phong model to compute shade at point of intersection
- Radiosity works best for perfectly diffuse (Lambertian) surfaces



# Building a Ray Tracer

- Best expressed recursively
- Can remove recursion later
- Image based approach
  - For each ray .....
- Find intersection with closest surface
  - Need whole object database available
  - Complexity of calculation limits object types
- Compute lighting at surface
- Trace reflected and transmitted rays

# When to stop

- Some light will be absorbed at each intersection
  - Track amount left
- Ignore rays that go off to infinity
  - Put large sphere around problem
- Count steps

# Recursive Ray Tracer I

## Program Sketch for Ray Tracing

```
program raytrace
var lsou; (* intensity of light source *)
  back; (* background intensity *)
  ambi; (* ambient light intensity *)
  depth; (* depth of ray tree consisting of multiple
          reflection/refraction paths *)

  ray = record (* ray          x = a + ti
                point: (a, b, c)      y = b + tj
                unit direction: (i, j, k)  z = c + tk *)
  end;
  r: ray;
```

# Recursive Ray Tracer II

```
function intensity (r);
    (* intensity = spec + refr + dull
    spec = specular reflection component
    refr = refraction component
    dull = non-reflecting, non refracting
    component *)

L: unit vector pointing to light source
V: unit vector pointing from current position to eye
N: unit surface normal
Objects [1...n] (* list of n objects in scene *)
Ka [1...n](* ambient reflectivity factor for each object
Ks [1...n](* specular reflectivity factor for each object
Kr [1...n](* refractivity index for each object *)
Kd [1...n](* diffuse reflectivity factor for each object
S[1...n](* shininess factor for each object *)
(* Additional Comments: For a transparent object, Kd[j]=0
and Ks[j]+Kr[j]=1 i.e. partly reflecting + partly
refracting. For an opaque object Kr[j]=0, Ks[j] and
Kd[j] can be anything as no simple relation between
them *)
```

# Recursive Ray Tracer III

```
function intensity(r: ray): rgb
  var flec, frac: ray;    spec, refr, dull: rgb;
  begin
    depth := depth + 1
    if depth > 5 then intensity := back
    else
      begin (* label 1 *)
        check ray r for intersection with all objects
                                     in scene

        if no intersection
        then if r parallel to L
              then intensity := lsou
              else intensity := back
        else
          begin (* label2 *)
            Take closest intersection which is object[j]
            compute normal N at the intersection point
            if Ks[j] > 0 (* non-zero specular reflectivity)
            then begin
              compute reflection ray flec;
```

```
          spec := Ks[j]*(intensity(flec) + (normalize(r).V)^S[j]
            end
          else spec:=0;
          if(Kr[j]>0)      (* non-zero refractivity *)
          then begin
            compute refraction ray frac;
            refr := Kr[j]*intensity(frac);
          end
          else refr:=0;
          check for shadow;
          if shadow
          then dull:= Ka[j]*ambi
          else dull:= Kd[j]*lsou* N.L +Ka[j]*ambi);
          intensity :=spec +refr +dull;
        end (* label2 *)
      end(* label 1*)
      depth := depth - 1
    end(* function *)

  begin (* raytrace*)
    for each pixel P of projection viewport in raster order
    begin
      r = ray emanating from viewer through P; V = r;
      set intensity(r) to the frame buffer pixel corresponding
        to P
    end
  end (*raytrace *)
```

# Computing Intersections

- Implicit Objects
  - Quadrics
- Planes
- Polyhedra
- Parametric Surfaces

# Implicit Surfaces

Ray from  $\mathbf{p}_0$  in direction  $\mathbf{d}$

$$\mathbf{p}(t) = \mathbf{p}_0 + t \mathbf{d}$$

General implicit surface

$$f(\mathbf{p}) = 0$$

Solve scalar equation

$$f(\mathbf{p}(t)) = 0$$

General case requires numerical methods

# Quadratics

General quadric can be written as

$$\mathbf{p}^T \mathbf{A} \mathbf{p} + \mathbf{b}^T \mathbf{p} + c = 0$$

Substitute equation of ray

$$\mathbf{p}(t) = \mathbf{p}_0 + t \mathbf{d}$$

to get quadratic equation



# Sphere

$$(\mathbf{p} - \mathbf{p}_c) \cdot (\mathbf{p} - \mathbf{p}_c) - r^2 = 0$$

$$\mathbf{p}(t) = \mathbf{p}_0 + t \mathbf{d}$$

$$\mathbf{p}_0 \cdot \mathbf{p}_0 t^2 + 2 \mathbf{p}_0 \cdot (\mathbf{d} - \mathbf{p}_0) t + (\mathbf{d} - \mathbf{p}_0) \cdot (\mathbf{d} - \mathbf{p}_0) - r^2 = 0$$

# Planes

$$\mathbf{p} \cdot \mathbf{n} + c = 0$$

$$\mathbf{p}(t) = \mathbf{p}_0 + t \mathbf{d}$$

$$t = -(\mathbf{p}_0 \cdot \mathbf{n} + c) / \mathbf{d} \cdot \mathbf{n}$$

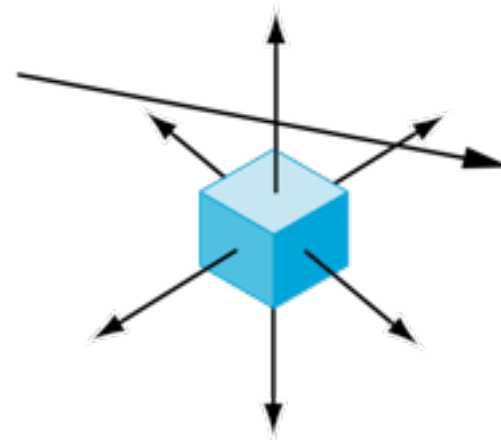
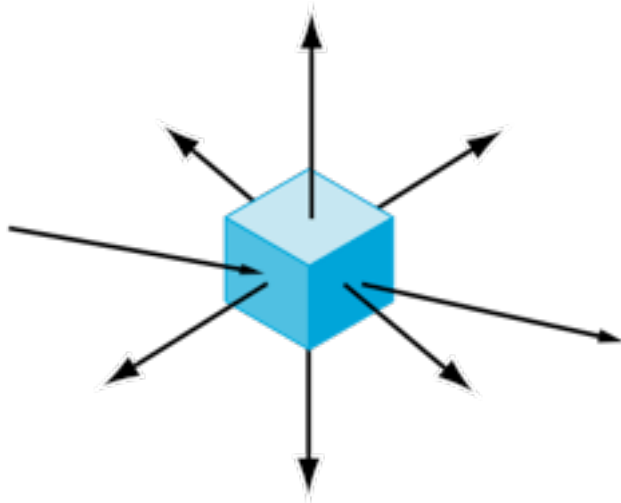
# Polyhedra

- Generally we want to intersect with closed objects such as polygons and polyhedra rather than planes
- Hence we have to worry about inside/outside testing
- For convex objects such as polyhedra there are some fast tests

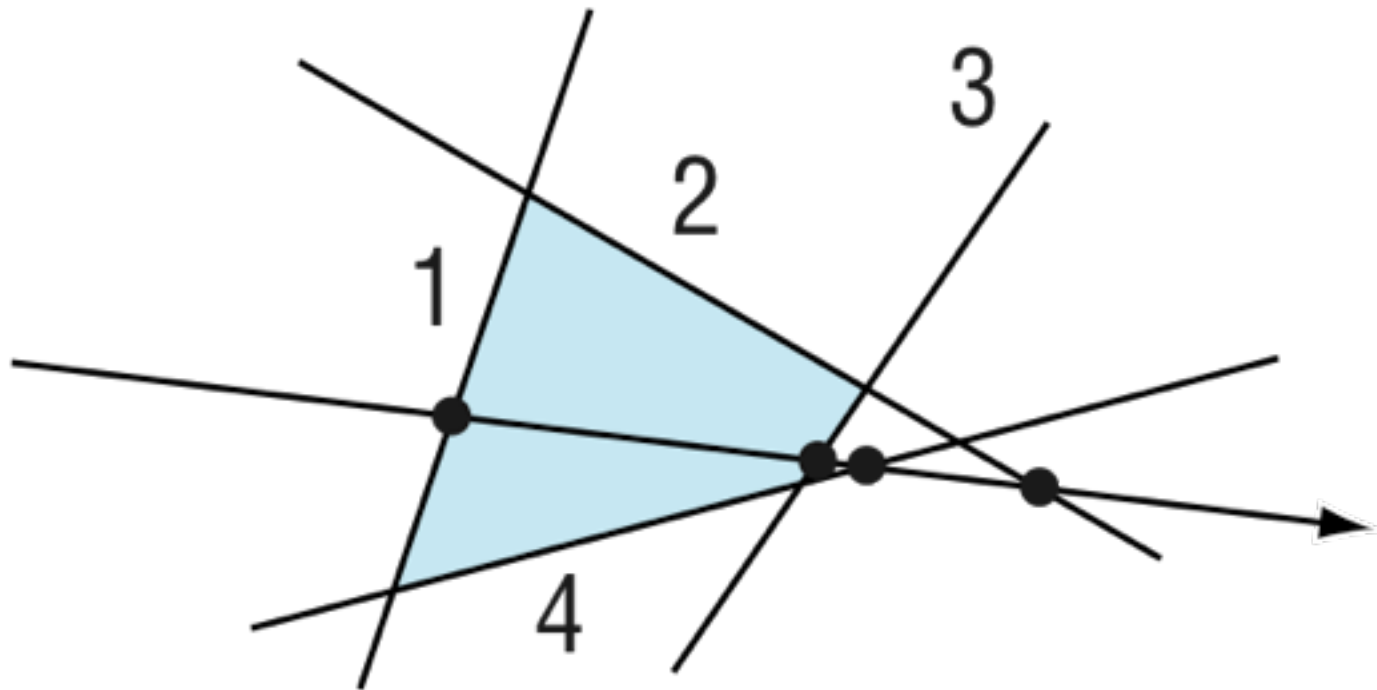
# Ray Intersection with Polyhedron

- If ray enters an object, it must enter a front facing polygon and leave a back facing polygon
- Polyhedron is formed by intersection of planes
- Ray enters at furthest intersection with front facing planes
- Ray leaves at closest intersection with back facing planes
- If entry is further away than exit, ray must miss the polyhedron

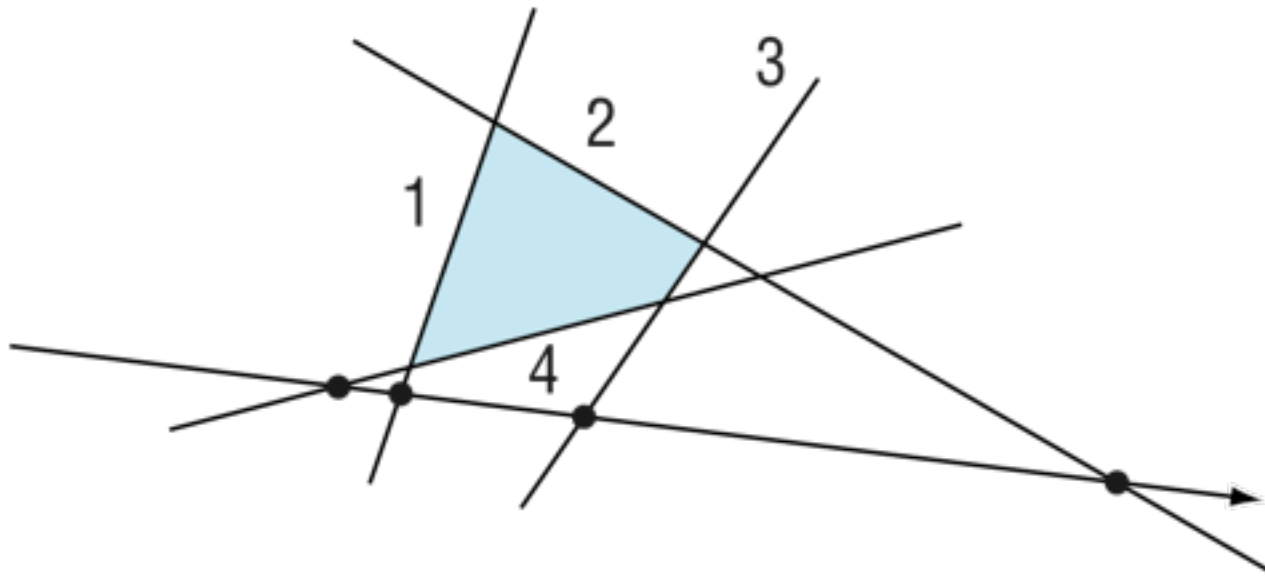
# Ray Intersection with a Polyhedron



# Ray Intersection with a Polygon

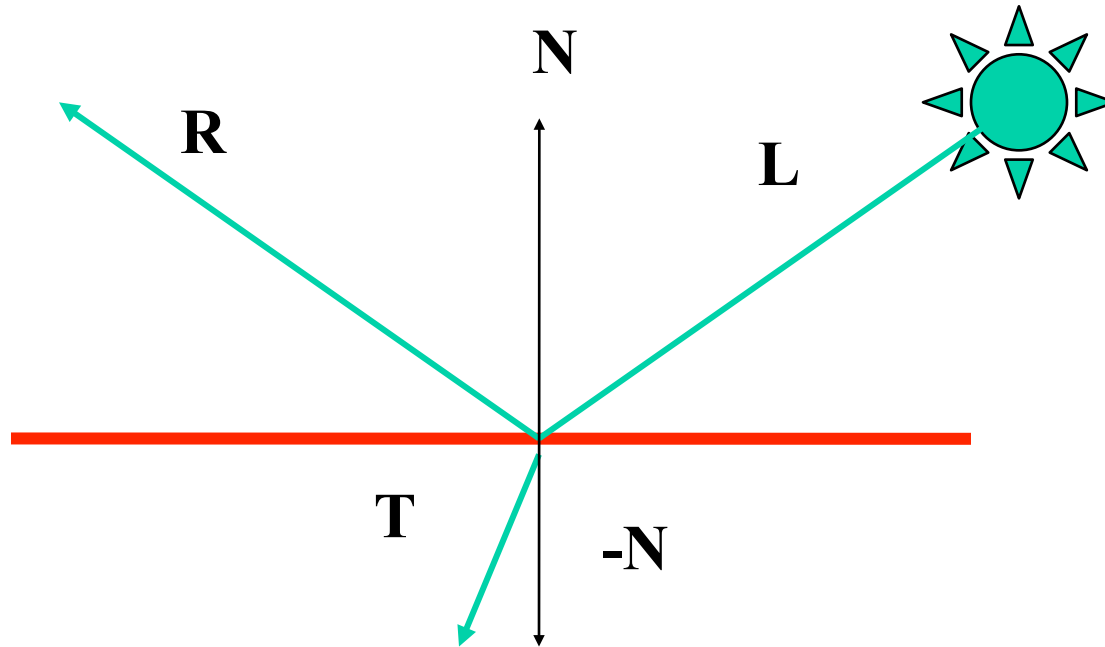


# Ray Intersection with a Polygon



# Ray Transmission Vectors

- Ray tracers can make use of all these effects in a global calculation by tracing rays





# Refraction

With pure refraction, all the light is transmitted but the angle of refraction is determined by Snell's law

$$\dot{n}_i \sin \theta_i = \dot{n}_t \sin \theta_t$$

where  $\dot{n}_i$  and  $\dot{n}_t$  are the speed of light relative to the speed of light in a vacuum

Let  $\dot{n} = \dot{n}_i / \dot{n}_t$

# Computing T

$$\dot{\eta}^2 \sin^2\theta_i = \dot{\eta}^2 (1 - \cos^2\theta_i) = \sin^2\theta_t = 1 - \cos^2\theta_t$$

Solving for  $\cos \theta_t$

Assuming normalized vectors

$$\cos \theta_t = \mathbf{T} \cdot \mathbf{N} = (1 - \dot{\eta}^2 (1 - \cos^2\theta_i))^{1/2}$$

$$\text{where } \cos \theta_i = \mathbf{L} \cdot \mathbf{N}$$

$\mathbf{T}$ ,  $\mathbf{N}$ , and  $\mathbf{L}$  must be coplanar

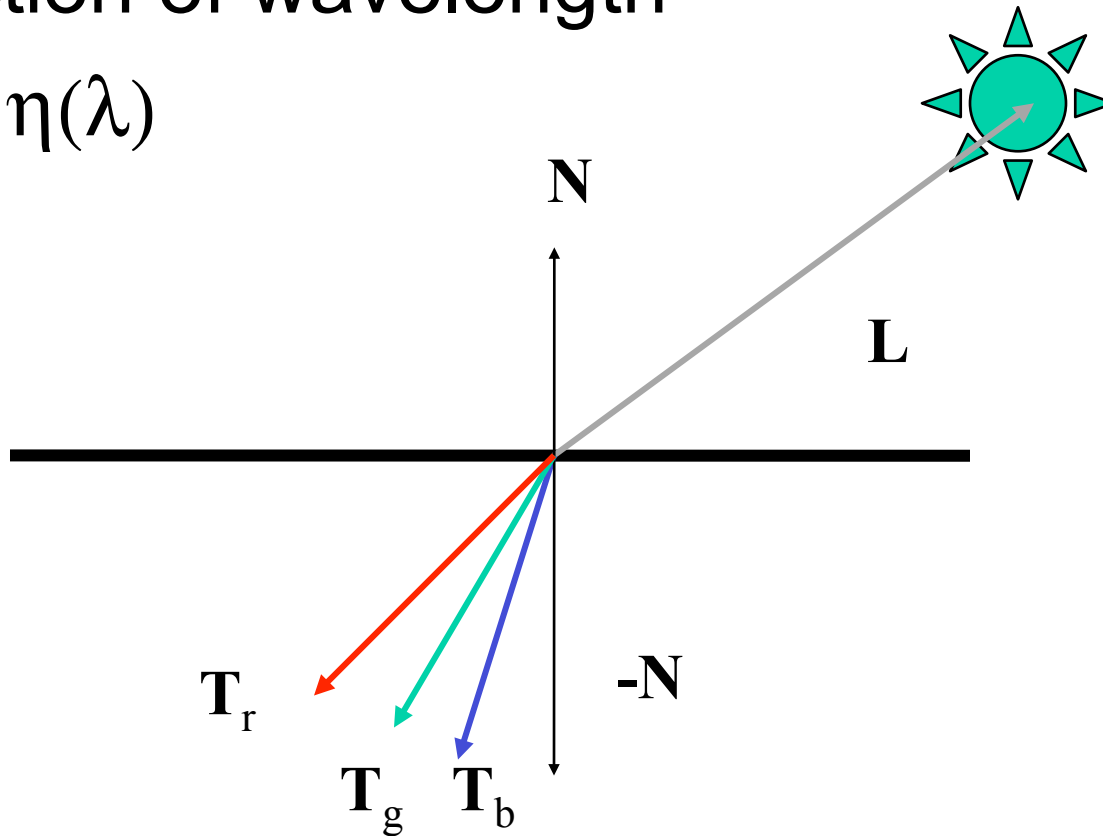
$$\mathbf{T} = \alpha \mathbf{L} + \beta \mathbf{N} \text{ and } \mathbf{T} \cdot \mathbf{T} = 1$$

Solving

$$\mathbf{T} = -1/\dot{\eta} \mathbf{L} - (\cos \theta_t - 1/\dot{\eta} \cos \theta_i) \mathbf{N}$$

# Chromatic Dispersion

- The refraction coefficient is actually a function of wavelength
- $\eta = \eta(\lambda)$



# Chromatic Dispersion with Shaders

- Easy to do with reflection maps
- Use three values of  $\eta$
- Make use of vector operations