Suppose H is a Merkle-Damgerd Lash function built from a secure compression function

Approach 1: use CBC (without IV) $ \begin{array}{c} m_1 \\ m_2 \\ \hline F(k,) \\ F$	ong
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	ong]
$F(k, \cdot) = F(k, \cdot) = 0$	ong]
	ong]
اللها والمنافعة والمنافعة والمنافعة المنافعة المنافعة المنافعة المنافعة والمنافعة والمنافعة والمنافعة والمنافعة	ong
L> Mode often called "raw-CBC"	ong]
Raw-CBC is a way to build a large-domain PRF from a <u>small-domain</u> one	ong
L> Can show security for "prefix-free" messages [more precisely, raw-CBC is a prefix-free PRF: pseudorandon as]	. other I
messages as a special case	
But not secure for <u>variable-length</u> messages: "Extension attack" 1. Query for MAC on arbitrary block X:	
$\begin{array}{c} & & \\$	
$ \begin{array}{c} \hline \\ \hline $	
$[F(k_i)] \rightarrow F(k_i, \chi) \rightarrow f(k_i$	
2. Output forgery on message $(x, x \oplus t)$ and tag $t \longrightarrow t$ is a valid tag on <u>extended message</u> \rightarrow Adversary succeed with advantage	(x, tox) I
row CBC can be used to build a MAC on fixed-length messages, but not variable-length messages (more generally, prefix-free)	
(ECBC) (ECBC) Standards for banking / financial services	
apply another PRF with a different key to the same key of	ist secure) FrowCBC
m_1 m_2 \cdots m_l k m_l	
$F(k_{i}) F(k_{i}) F(k_{2}, \cdot) output$	
To use encrypted CBC-MAC, we need to assume message length is even multiple of block size (similar to CBC enc	ryption)
L> to sign messages that are not a multiple of the block size, we need to first pad the message L> as was the case with encryption, padding must be injective	
L> in the case of encryption, injectivity needed for correctness	#** ***
in the case of integrity, injectivity hereas for security [it post(ine) - fuch (in()), the and the will have	tug _

Standard approach to pad: append 1000...0 to fill up block [ANSI X9.9 and ANSI X9.19 standards]

Note: if message is an even multiple of the block length, need to introduce a dummy block

→ Necessary for any injective function: [{0,13⁵n}] > [{0,13ⁿ]

This is a bit-padding scheme [PKCS #7 that we discuss previously in the context of CBC encryption is a byte-padding scheme]

Better approach: raw CBC-MAC secure for prefix-free messages

L> Can we apply a "prefix-free" encoding to the message? equal-length messages cannot have one be prefix of other - Option 1: Prepend the message length to the message different-length messages differ in first block Problematic if we do not know message length at the beginning (e.g., in a streaming setting) Still requires pudding message to multiple of block size)

- Option 2: Apply a random secret shift to the last block of the message

 $(\chi_1, \chi_2, ..., \chi_{\ell}) \mapsto (\chi_1, \chi_2, ..., \chi_{\ell} \oplus k)$ where $k \stackrel{e}{\leftarrow} \chi$

Adversary that closs not know k cannot construct two messages that are prefixes except with probability /1x1 (by guessing k)

basis for CMAC (standardized by NIST in 2005)