

Nonce-based counter mode: divide IV into two pieces: $IV = \text{nonce} \parallel \text{counter}$

↑
value that does not repeat

Common choices: 64-bit nonce, 64-bit counter } only nonce needs to be sent!
96-bit nonce, 32-bit counter } (slightly smaller ciphertexts)

Only requirement for security is that IV does not repeat:

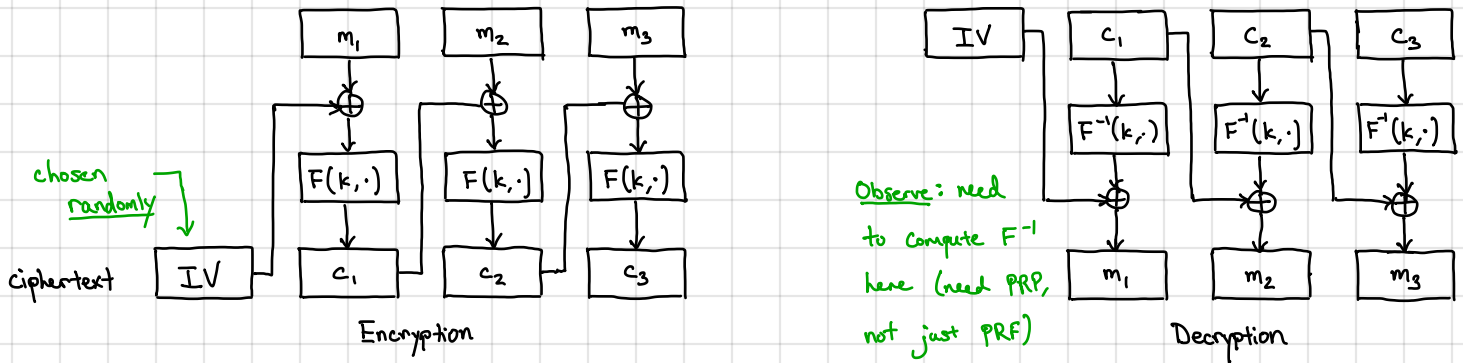
- Option 1: Choose randomly (either IV or nonce)
- Option 2: If sender + recipient have shared state (e.g., packet counter), can just use a counter, in which case, IV/nonce does not have to be sent

(CTR)

Counter mode is parallelizable, simple-to-implement, just requires PRF — preferred mode of using block ciphers

Other block cipher modes of operation:

Cipherblock chaining (CBC): common mode in the past (e.g., TLS 1.0, still widely used today)



Theorem: Let $F: K \times X \rightarrow Y$ be a secure PRF and let Π_{CBC} denote the CBC encryption scheme for l -block messages ($M = X^{\leq l}$). Then, for all efficient CPA adversaries A , there exists an efficient PRF adversary B such that

$$\text{CPAAdv}[A, \Pi_{CBC}] \leq \frac{2Q^2 l^2}{|X|} + 2 \cdot \text{PRFAdv}[B, F]$$

↑ Q : number of encryption queries
 l : number of blocks in message

Intuition: similar to analysis of randomized counter mode:

1. Ciphertext is indistinguishable from random string if PRP is evaluated on distinct inputs
2. When encrypting, PRP is invoked on l random blocks, so after Q queries, we have Ql random blocks.
⇒ Collision probability $\leq \frac{Q^2 l^2}{|X|}$ (this is larger than collision prob. for randomized counter mode by a factor of $\frac{l}{2}$ [overlap of Q random intervals vs. Ql random points])
3. Factor of 2 arises for same reason as before

Interpretation. CBC mode provides weaker security compared to counter mode: $\frac{2Q^2 l^2}{|X|}$ vs. $\frac{4Q^2 l}{|X|}$

Concretely: for same parameters as before (1 MB messages, 2^{-32} distinguishing advantage):

$$Q \leq \sqrt{\frac{|X| \cdot 2^{-32}}{2l^2}} = \sqrt{\frac{2^{18} \cdot 2^{-32}}{2(2^{16})^2}} = \sqrt{2^{63}} = 2^{31.5} \quad (\sim 1 \text{ billion messages})$$

↳ $2^{31.5} \sim 180 \times$ smaller than using counter mode

Padding in CBC mode: each ciphertext block is computed by feeding a message block into the PRP

⇒ message must be an even multiple of the block size

⇒ when used in practice, need to pad messages

Can we pad with zeroes? **Cannot decrypt!** What if original message ended with a bunch of zeroes?

Requirement: padding must be invertible

CBC padding in TLS 1.0: if k bytes of padding is needed, then append k bytes to the end, with each byte set to $k-i$

(for AES-CBC) if 0 bytes of padding is needed, then append a block of 16 bytes, with each byte equal to 15

↳ dummy block needed to ensure pad is invertible injective functions must expand: $|\{0,1\}^{\leq 256}| > |\{0,1\}^{256}|$

↳ called PKCS#5/PKCS#7 (public-key cryptography standards)

Need to pad in CBC encryption can be exploited in "padding oracle" attacks - see HW1 for one example

Padding in CBC can be avoided using idea called "ciphertext stealing" (as long as messages are more than 1 block)

Comparing CTR mode to CBC mode:

CTR mode

1. no padding needed (shorter ciphertexts)
2. parallelizable
3. only requires PRF (no need to invert)
4. tighter security
5. IVs have to be non-repeating (and spaced far apart)

easy to implement:
IV = nonce || counter

↑
only needs to be non-repeating (can be predictable)

CBC mode

1. padding needed
2. sequential
3. requires PRP
4. less tight security (re-key more often)
5. requires unpredictable IVs

interesting traffic analysis attack: each keystroke is sent in separate packet, so it leaks info on length of user's password!

imagine 1 byte messages (e.g., encrypted key strokes) over SSH

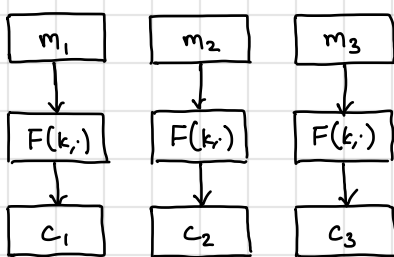
1 block + 1 byte with CTR
2 blocks with CBC

requires more structured primitive, more code to implement forward and backward evaluation

↑
TLS 1.0 used predictable IVs (see HW1 for an attack)
SSH v1 used a 0 IV (even worse!)

Bottom-line: use randomized or nonce-based counter mode whenever possible: simpler, easier, and better than CBC!

A tempting and bad way to use a block cipher: ECB mode (electronic codebook)



Scheme is deterministic! Cannot be CPA secure!

Not even semantically secure!

(m_0, m_0) vs. (m_0, m_1) where $m_1 \neq m_0$

↑
ciphertext blocks output are same

↑
ciphertext blocks output are different

Encryption: simply apply block cipher to each block of the message

Decryption: simply invert each block of the ciphertext

NEVER USE ECB MODE FOR ENCRYPTION!