Signatures from trapoloor permutations (the full domain hash): In order to appeal to security of TDP, use need that the argument to F-((td,.) to be random

Idea: hash the message first and sign the hash value (often called "hash-and-sign")

-> Another benefit: Allows signing long messages (much larger than domain size of TDF)

FDH construction:

-Setup (1^{γ}) : Sample (pp, td) < Setup (1^{γ}) for the TDP and output Vk= pp, sk = td -Sign (sk,m): Output $\sigma \leftarrow F^{-1}(+d, H(m))$ - Verify (vk, m, σ) : Output 2 if $F(pp, \sigma) = H(m)$ and σ otherwise

Theorem. If F is a trapoloor permutation and H is modeled as an ideal hash function (i.e., random oracle), then the full domain hash signature scheme defined above is secure. L> function that behaves like a traly random function Proof Intuition: To forge a signature on a message m, need to compute

(does not exist but functions like SHA-256 or F⁻¹ (td, H(m)) where H(m) is <u>uniformly random</u> in domain SHA-3 believed to be "close enough") of the permutation - security follows from TDP. <u>Caveat</u>: still need to simulate signing queries morelies on

"programming" the random oracle (see office hours) Some (partial) attacks can exploit very small public exponent (e-3)

Recap: RSA-FDH signatures:

Setup (1?): Sample modulus N, e, d such that ed = 1 (mod 4(N)) - typically e = 3 or e= 65537 Output Vk = (N, e) and sk = (N, d)Sign (sk, m): $\sigma \leftarrow H(m)^d$ [Here, we are assuming that H maps into \mathbb{Z}_{N}^{*}]

Verify (VK, m, o): Output 1 : f H(m) = o and O otherwise

Standard: PKCS1 V1.5 (typically used for signing certificates)

→ Standard cryptographic hosh functions hosh into a 256-bit space (e.g., SHA-256), but FDH requires full domain

has PKCS I UI.5 is a way to god hashed message before signing:

00 01 FF FF ··· FF FF 00 DI H(m) 16 bits pad digest info

(e.g., which hash function) was used

> Padding important to protect against chosen message attacks (e.g., preprocess to find messages m1, m2, m3 where H (m1) = H(m2) · H(m3) (but this is not a full-domain hash and <u>cannot</u> prove security under RSA - can make stronger assumption...)

Also possible to use RSA to build PRE:

This is an example of hybrid encryption or KEM: y is used to encapeulate the key and ct' is an encryption under h

<u>Theorem</u>. If F is a trapoloor permutation and H is modeled as an ideal hash function, then the above encryption scheme is semantically secure. [In fact, this scheme is CCA-secure in the random oracle model] Proof intuition. Given a ciphertext (y, ct') and public key pk = pp:

RSA instantiation:

- <u>In practice</u>: Most widely-used standard for RSA encryption is PKCS1 (by RSA labs) → Has shorter cipturtexts if we are encrypting a single ZN element (no need for KEM + symmetric component]
 - (helpful if PKE just used to encrypt short token or metadata)
 - General approach: suppose N is 2048 bits and use want to encrypt 256-bit messages

ive will first apply a randomized pudding to m to obtain a 2048-bit pudded message

PKCS 1 podding:

(mode 2) 00 02 non-zero rondom bytes 00 m 16 bits s bits where s t

t-bits long

Encryption: Compute mond ~ PKCS(m) and set C ~ mond [i.e., directly apply RSA traphoor permutation to padded] Decryption: Compute mond ~ C^d and recover m from mond

- In ESL v3.0: during the handshake, server oberrypts client's message and checks if resulting mod is well-formed (i.e., has valid PKCS1 padding) and rejects if not
 - L> scheme is voluerable to a chosen ciphentext attack!
 - illows adversory to eavesdrop on convection
- Devastating attack on SSL3.0 and very hard to fix: need to change both servers + clients!

TLS 1.0: fix is to set m 2 2% if decryption over fails and proceed normally (never alert client if podding is malformed) — some fails at a later point in time, but hopefully no critical information is leabed... Take-away = PKCS1 is not CCA-secure which is very problematic for key exchange

https:// Absence of security proof should always be traubling ...

New standard: Optimal Asymmetric Encryption Badding (OAEP) [1994] } Standardized in PKCS1 Scan be shown to be CCA-secure in random aracle model version 2.0