Thus for	r: PRP/PRF in "counter	mode" gives us a stre	am cipher (one-time en	cryption scheme)	
				typically, the I	V is divided into a
How do	be reuse it? Choose a	random starting point	(called an initialization ve	ector) nonce (value that	t does not repeat) and
		'randomized counter mode!		a counter: I	V = nonce counter
	m	1 M2 M3 M4	divide message	into blocks (based on	block size of PRF)
	random				
	⊕ I√ F(k,	IV) F(k, IV+1) F(k, IV+2) F(k, I	U45)		
			_		
	IV C	C ₂ C ₃ C ₄	ciphentext		
	Observe: Cio	hartext is longer than t			
		ssage (required for (
		, - Jul. 6(, ,)			
Themen	: Lot F: K×X→Y be	a secure PRF and	let There denote the	andonized country	made correction scheme
. 1955, G			il). Then, for all efficient		, and the second se
). 1100, 100 (21) (21)		, the cours and
	efficient PRF advers				
	CPAAA	$V[A, \Pi_{cTR}] \leq \frac{4Q^2L}{ X }$	+ J. PREALVER FT		
	0 111 100	12, 1212 1 171	5 1101 MAY (6), 1 1		
		₾ (2: number of encryption qu	eries .	
			l: number of blocks in	message	
T.A. 38		a callistans (i.e. PDE acc	ver evaluated on the Sa	عزين ما (اعماد م	
Intuition			7 C.	me block), Them 17 is	as it earlything is
	'''	a fresh one-time pad.	1 11 11 11	, , , , , , , , ,	(R ~
	2. Collision event:	(X, X +1,, X +k-1)	overlaps with (x', x'	+ 1,, X + X-1) when	$x, x \leftarrow \lambda$
		(. x x+1		
		X-2			. <u>2l</u>
			probability that x'	lies in this interval	's ≥ χ
	< 0	2 ()			
	There are ? C	Q^2 possible poins (X, X') ,	so by a union bound,		
		$Pr[collision] \leq \frac{2lQ}{ \chi }$	2		
		Pricollision] = 1x1			
	3. Remaining factor		to intermediate distribu	tion:) ²
		Encrypt mo with F	PRF	PRFAJV[B,F] + 21G	1
		Encrypt mo with -	fresh one-time pad	50	
		Encrypt m, with	fresh one-time pad fresh one-time pad PRF	9 PREALIER ET + 2	2 L Q 2
		Encrypt m, with	PRF	א וצרוניי (פינו) , -	1x1
Interpreta	tion: It x1 = 2128 (eg	,, AES), and messages	are 1 MB long (216 bloc	ks) and we want the	e distinguishing advantage
1		, then we can use the			5 5
		() < [1x1.2-32]	$\int \frac{2^{96}}{2^{18}} = \sqrt{2^{78}} = 2^{3}$	39 (~ 1 trillian massaa	es / \
		~ ~ ~ +L ~ ~	1 218 - 72 - 2	(1 11/11/10/ 1-620/09	٠٠.)

Nonce-based counter mode: divide IV into two pieces: IV = nonce 11 counter value that does not repeat Common choices: 64-bit nonce, 64-bit counter ? only nonce needs to be sent! (slightly smaller ciphertests) 96-bit nonce, 32-bit counter Only requirement for security is that IV closs not repeat: - Option 1: Choose randomly (either IV or nonce) " Option 2: If sender + recipient have shared state (e.g., packed counter), can just use a counter, in which case, IVI nonce does not have to be sent Counter mode is popullelizable, simple-to-implement, just requires PRF - preferred mode of using block ciphers Other block cipher modes of operation: Cipher block chaining (CBC): common mode in the past (e.g., TLS 1.0, still widely used today) chosen $F(k,\cdot)$ $F(k,\cdot)$ $F(k,\cdot)$ $F(k,\cdot)$ $F(k,\cdot)$ $F(k,\cdot)$ $F(k,\cdot)$ [V C₁ C₂ F⁻¹(k,·) F"(k,·) Observe: ned

to conquite F-1

here (need PRP, m1 m2 not just PRF) Decryption Encryption Theorem: Let F: K x > y be a secure PRF and let TICBC denote the CBC encryption scheme for l-block messages $(M = X^{\leq R})$. Then, for all efficient CPA adversaries A, there exists an efficient PRF adversary B such that CPAAdv[A, TICBC] < 2021 + J. PRFAdv[B, F] C: number of encryption queries l: number of blocks in message <u>Intuition</u>: Similar to analysis of randomized counter mode: 1. Ciphertext is indistinguishable from random string if PRP is evaluated on distinct injusts
2. When encrypting, PRP is invoked on I random blocks, so after Q queries, we have QI random blocks. \Rightarrow Collision probability $\leq \frac{Q^2 l^2}{|x|} \approx 2$ this is larger than collision probability $\leq \frac{Q^2 l^2}{|x|} \approx 2$ this is larger than collision probability $\leq \frac{Q^2 l^2}{|x|} \approx 2$ this is larger than collision probability of Q random intervals V_3 . Q random points 3. Factor of 2 arises for some reason as before Interpretation. CBC mode provides weaker security compared to counter mode: $\frac{20^2 l^2}{|\chi|}$ Vs. $|\chi|$ Concretely: for some parameters as before (1 MB messages, 2^{-52} distinguishing advantage): $Q \leq \sqrt{\frac{1 \times 1 \cdot 2^{-32}}{2 \cdot 2^2}} = \sqrt{\frac{2^{n_8} \cdot 2^{-52}}{2 \cdot (2^{16})^2}} = \sqrt{2^{63}} = 2^{31.5} \quad (\sim 1 \text{ billion messages})$ L > 1.75 ~ 180 x smaller than using counter mode

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