

# Problem Set 11

CS 331

Due Friday, May 6

1. Show NP-completeness for each of the following problems. Both are simple, direct reductions from one of the problems we have shown to be NP-complete in class.

- (a) **Minimum set cover.** You are given a set  $S$ , a collection of subsets  $S_1, \dots, S_n \subseteq S$ , and an integer  $k$ . Do there exist a set of  $k$  subsets  $T \subseteq [n]$  such that

$$\bigcup_{i \in T} S_i = S?$$

Hint, encoded as ROT-13: iregrk pbire.

- (b) **Subgraph Isomorphism.** You are given two graphs,  $G$  and  $H$ . Does  $G = (V_G, E_G)$  contain a subgraph isomorphic to  $H = (V_H, E_H)$ ? That is, is there an injection  $f : V_H \rightarrow V_G$  such that for every  $u, v \in V_H$ ,  $(u, v) \in E_H$  if, and only if,  $(f(u), f(v)) \in E_G$ ?

Hint, encoded as ROT-13: znk pyvdhr be vaqrcraqrag frg.

2. The problem ALLORNOTHINGSAT asks, given a 3CNF boolean formula, whether there is an assignment to the variables such that each clause either has three True literals or has three False literals.

Describe a polynomial time algorithm for ALLORNOTHINGSAT.