



# Texture Mapping



# Reading

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## ■ Required

- Watt, intro to Chapter 8 and intros to 8.1, 8.4, 8.6, 8.8.

## ■ Recommended

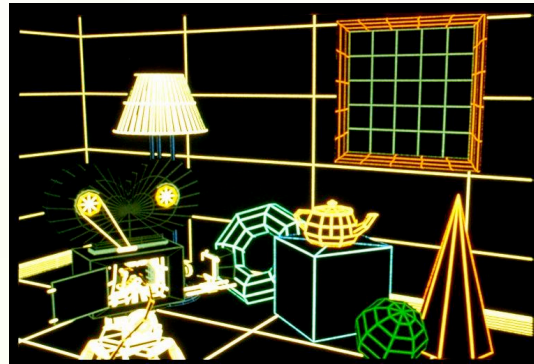
- Paul S. Heckbert. Survey of texture mapping. **IEEE Computer Graphics and Applications** 6(11): 56--67, November 1986.

## ■ Optional

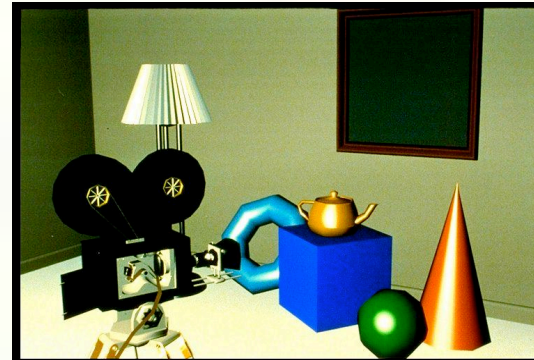
- Watt, the rest of Chapter 8
- Woo, Neider, & Davis, Chapter 9
- James F. Blinn and Martin E. Newell. Texture and reflection in computer generated images. **Communications of the ACM** 19(10): 542--547, October 1976.



# What adds visual realism?



*Geometry only*



*Phong shading*



*Phong shading +  
Texture maps*



# Texture mapping



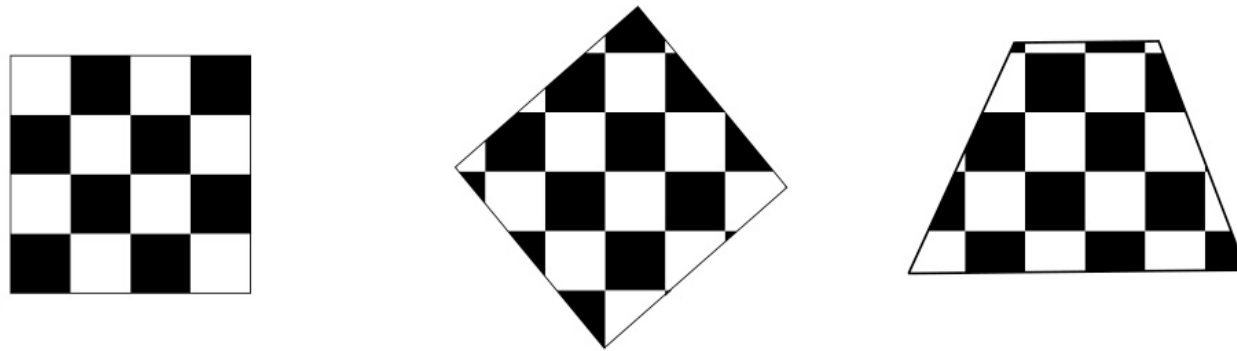
*Texture mapping (Woo et al., fig. 9-1)*

- Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex.
  - Due to Ed Catmull, PhD thesis, 1974
  - Refined by Blinn & Newell, 1976
- Texture mapping ensures that “all the right things” happen as a textured polygon is transformed and rendered.





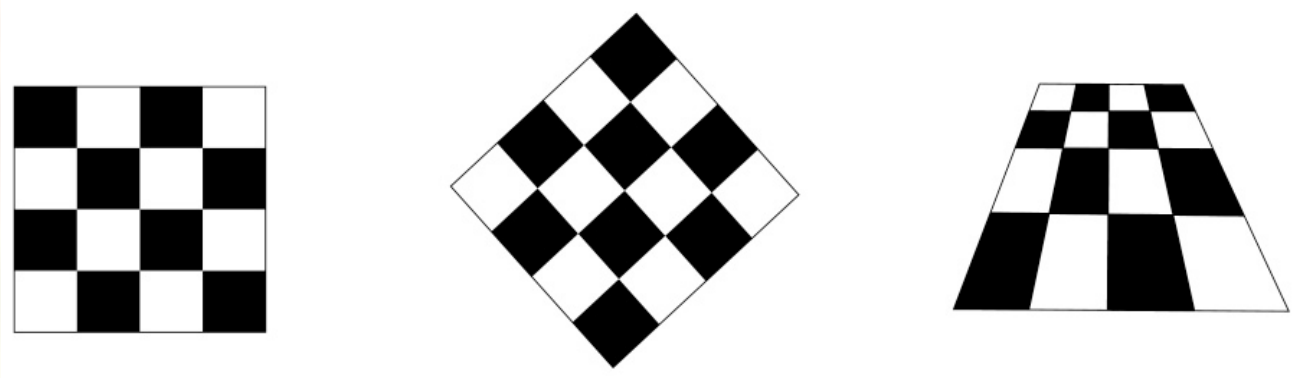
# Non-parametric texture mapping



- With “non-parametric texture mapping”:
  - Texture size and orientation are fixed
  - They are unrelated to size and orientation of polygon
  - Gives cookie-cutter effect



# Parametric texture mapping

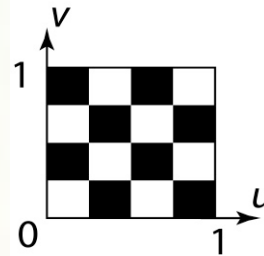


- With “parametric texture mapping,” texture size and orientation are tied to the polygon.
- Idea:
  - Separate “texture space” and “screen space”
  - Texture the polygon as before, but in texture space
  - Deform (render) the textured polygon into screen space
- A texture can modulate just about any parameter – diffuse color, specular color, specular exponent, ...

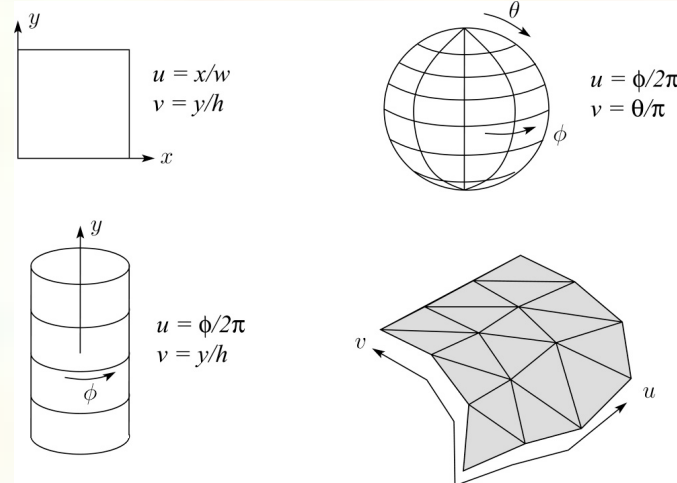


# Implementing texture mapping

- A texture lives in its own abstract image coordinates parameterized by  $(u, v)$  in the range  $([0..1], [0..1])$ :



- It can be wrapped around many different surfaces:



- Computing  $(u, v)$  texture coordinates in a ray tracer is fairly straightforward.
- Note: if the surface moves/deforms, the texture goes with it.



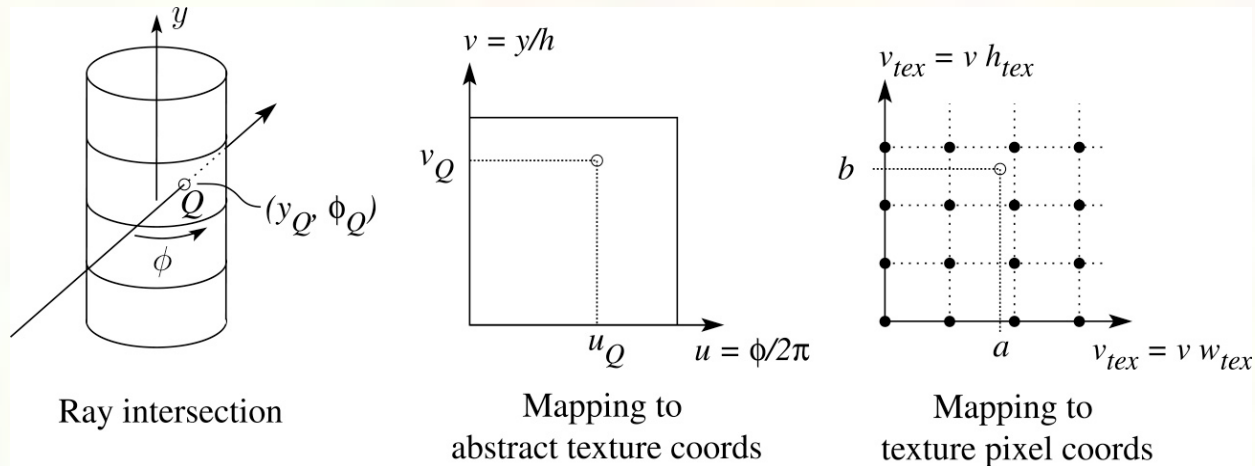
# Mapping to texture image coords

- The texture is usually stored as an image. Thus, we need to convert from abstract texture coordinate:

$(u, v)$  in the range  $([0..1], [0..1])$

to texture image coordinates:

$(u_{tex}, v_{tex})$  in the range  $([0.. w_{tex}], [0.. h_{tex}])$

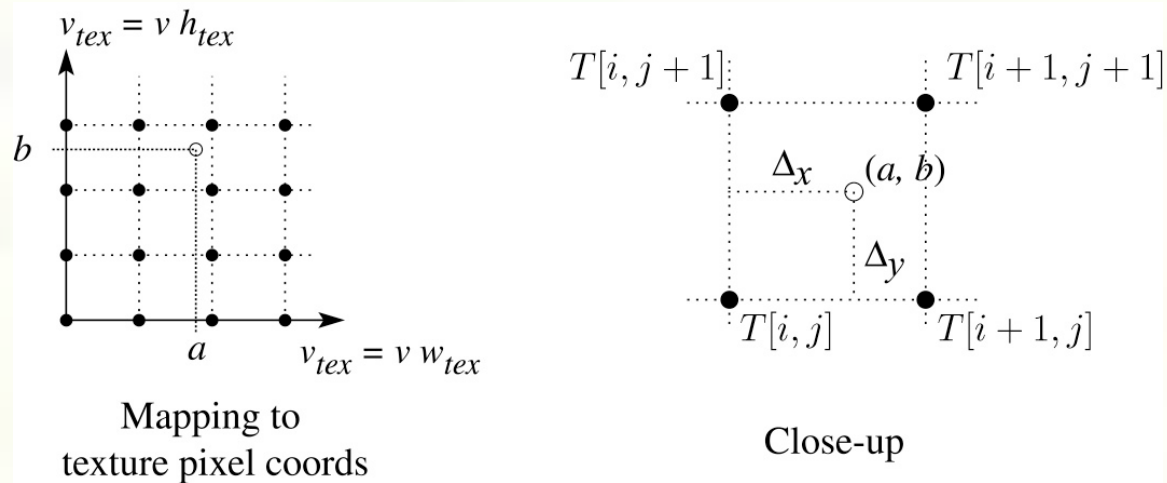


- **Q:** What do you do when the texture sample you need lands between texture pixels?



# Texture resampling

- We need to resample the texture:



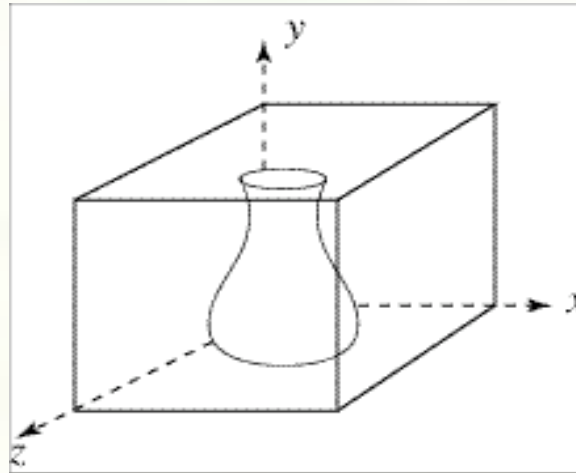
- A common choice is **bilinear interpolation**:

$$\begin{aligned} T(a,b) &= T[i + \Delta_x, j + \Delta_y] \\ &= (1 - \Delta_x)(1 - \Delta_y)T[i, j] + \Delta_x(1 - \Delta_y)T[i + 1, j] \\ &\quad + (1 - \Delta_x)\Delta_y T[i, j + 1] + \Delta_x\Delta_y T[i + 1, j + 1] \end{aligned}$$



# Solid textures

- **Q:** What kinds of artifacts might you see from using a marble veneer instead of real marble?



- One solution is to use **solid textures**:
  - Use model-space coordinates to index into a 3D texture
  - Like “carving” the object from the material
- One difficulty of solid texturing is coming up with the textures.



# Solid textures (cont'd)

- Here's an example for a vase cut from a solid marble texture:



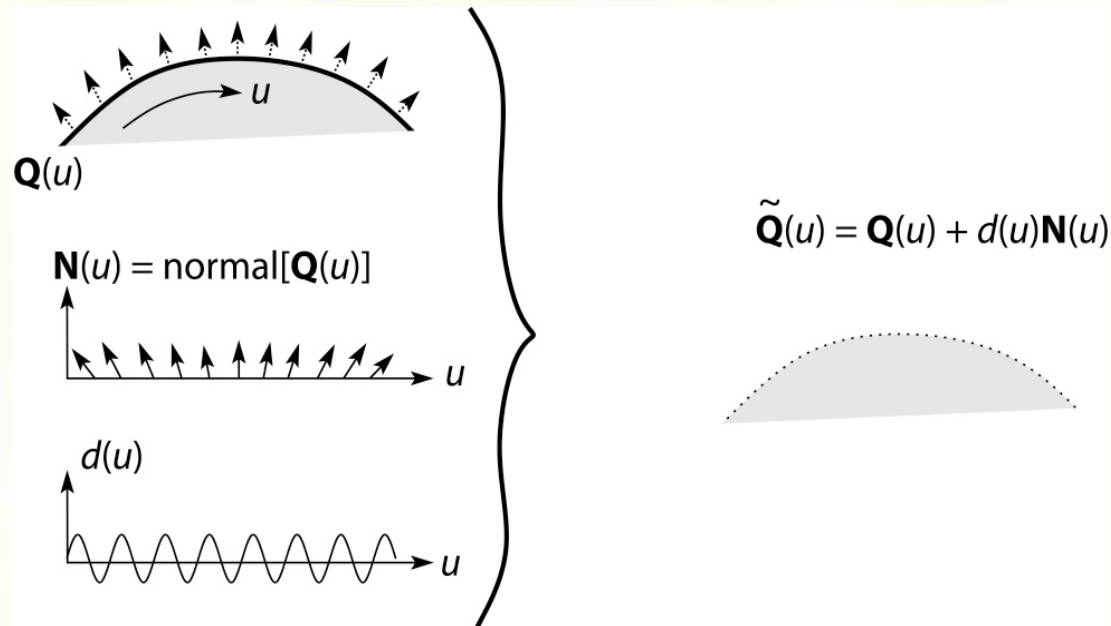
- *Solid marble texture by Ken Perlin, (Foley, IV-21)*





# Displacement mapping

- Textures can be used for more than just color.
- In **displacement mapping**, a texture is used to perturb the surface geometry itself:



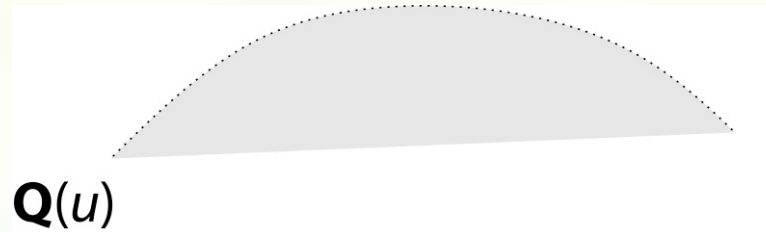
- These displacements “animate” with the surface
- **Q:** Do you have to do hidden surface calculations on  $\tilde{Q}$ ?



# Bump mapping

- In **bump mapping**, a texture is used to perturb the normal:
  - Use the original, simpler geometry,  $\mathbf{Q}(u)$ , for hidden surfaces
  - Use the normal from the displacement map for shading:

$$\tilde{\mathbf{N}} = \text{normal}[\tilde{\mathbf{Q}}(u)]$$



- **Q:** What artifacts in the images would reveal that bump mapping is a fake?

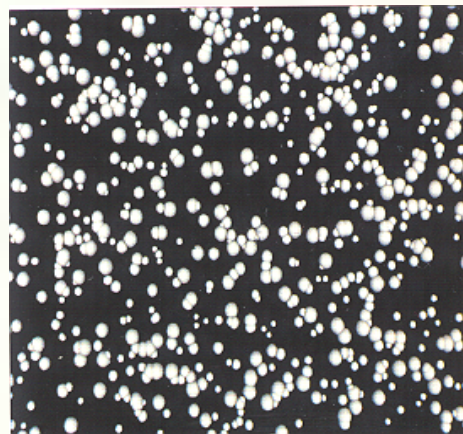


# Bump mapping example

Texture #1  
(diffuse color)



Texture #2  
(bump map)



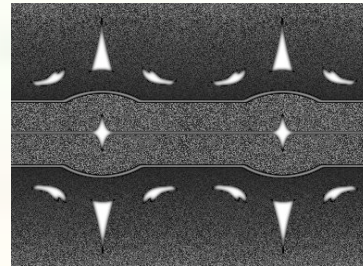
Rendered Image



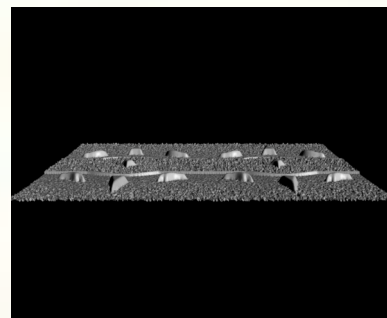
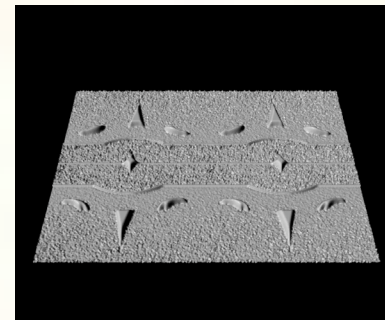
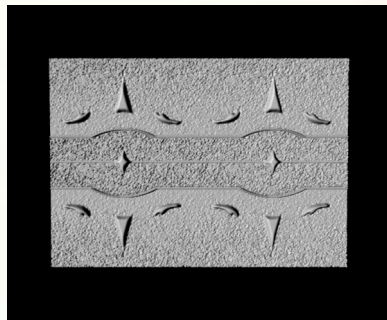


# Displacement vs. bump mapping

- Input texture



- Rendered as displacement map over a rectangular surface





# Displacement vs. bump mapping (cont'd)



Original rendering



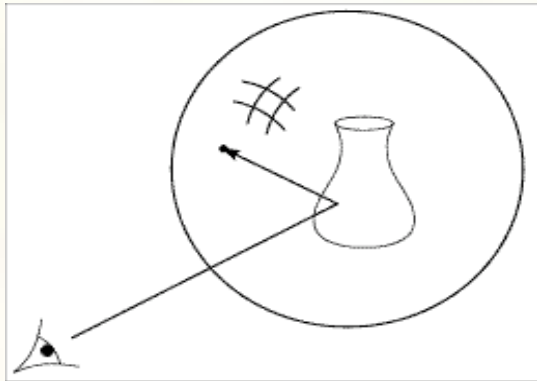
Rendering with bump map wrapped around a cylinder

*Bump map and rendering by Wyvern Aldinger*





# Environment mapping

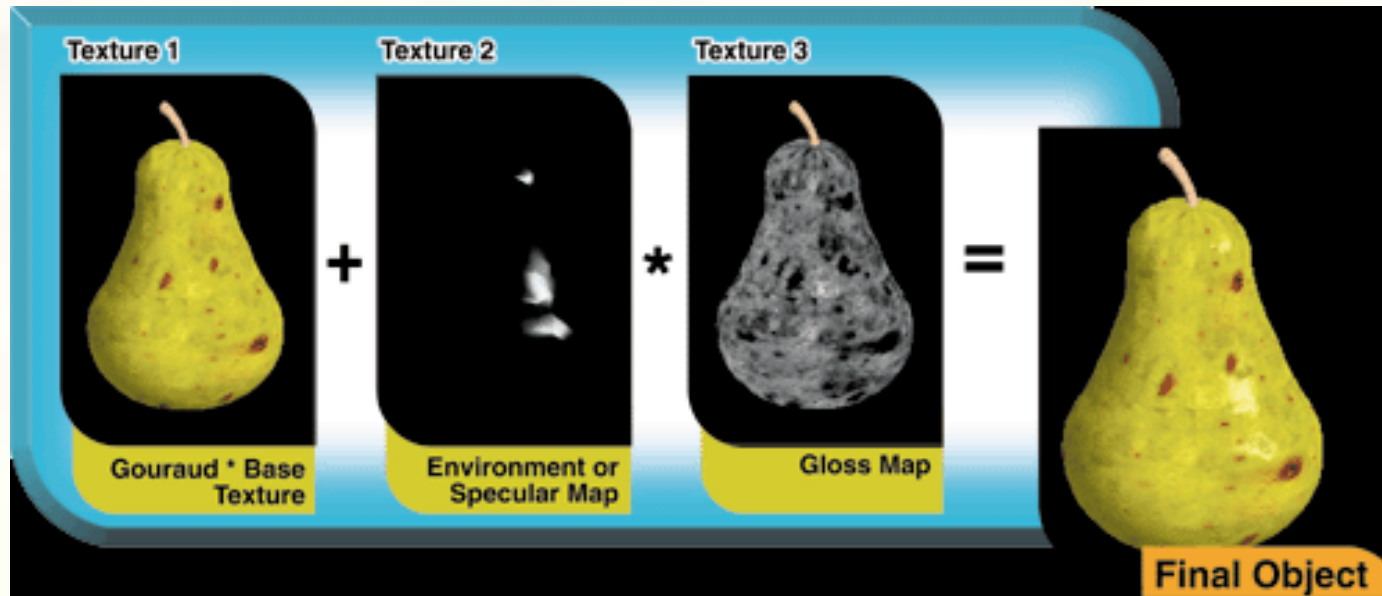


- In **environment mapping** (also known as **reflection mapping**), a texture is used to model an object's environment:
  - Rays are bounced off objects into environment
  - Color of the environment used to determine color of the illumination
  - Really, a simplified form of ray tracing
  - Environment mapping works well when there is just a single object – or in conjunction with ray tracing
- Under simplifying assumptions, environment mapping can be implemented in hardware.
- With a ray tracer, the concept is easily extended to handle refraction as well as reflection.



# Combining texture maps

- Using texture maps in combination gives even better effects.



*Diffuse  
color*

*Environment map  
(not necessary  
in ray tracer)*

*Specular  
coefficient*

*Material  
properties  
(coefficients  
in shading  
equation)*





# Can define material by program

- A ‘surface shader’ computes the color of each ray that hits the surface.
- Example: Renderman surface shader

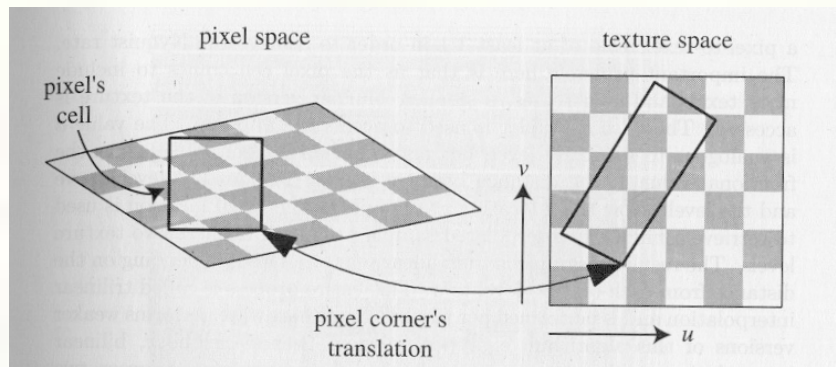
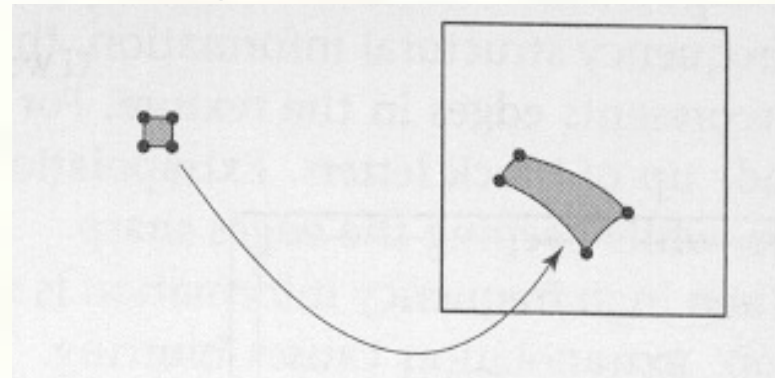
```
/*  
 * Checkerboard  
 */  
surface checker(float Kd=.5, Ka=.1) {  
    float smod = mod(10*s, 1);  
    float tmod = mod(10*t, 1);  
    if (smod < 0.5) {  
        if (tmod < 0.5) Ci=Cs; else Ci=color(0,0,0);  
    } else {  
        if (tmod < 0.5) Ci=color(0,0,0); else Ci=Cs;  
    }  
    Oi = Os;  
    Ci = Oi*Ci*(  
        Ka*ambient() +  
        Kd*diffuse(faceforward(normalize(N),I)));  
}
```





# How do we anti-alias textures?

- We could just super-sample.
- But textures (and shader programs) are a special case; we can use true area integration!

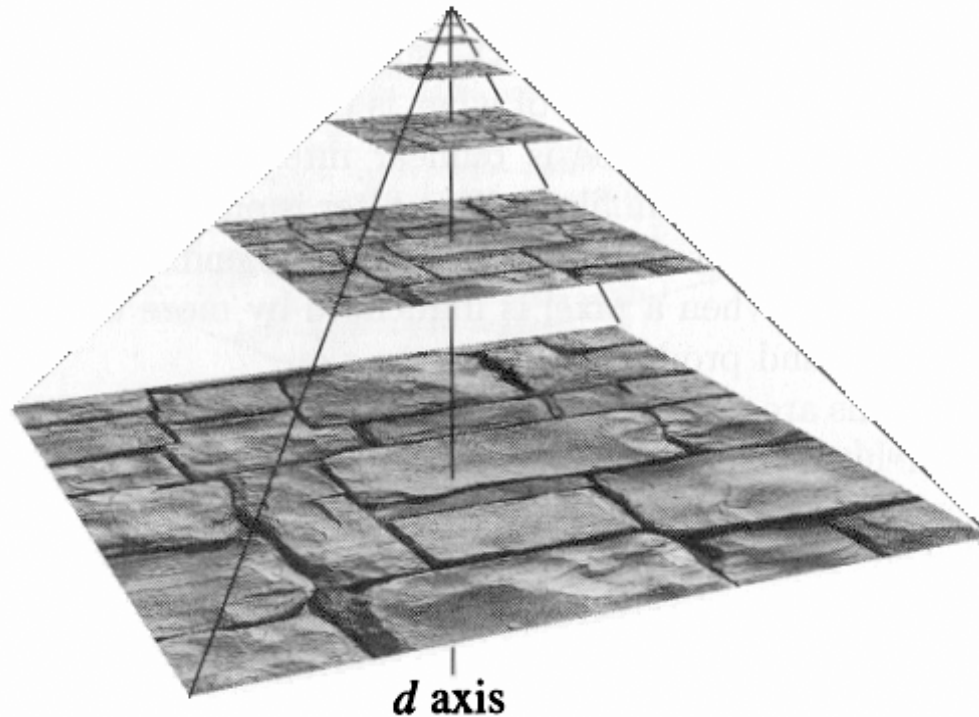


- *Approximate footprint as parallelogram*
- *Determine this approximate footprint using discrete differences*



# Cost of filtering can be reduced

- Store a pyramid of pre-filtered images:



- During texture lookup, read from appropriate level of the pyramid.



# Next time: Hierarchical modeling

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- How do we represent translation and rotation of complex objects using hierarchies of transformations?
- (Easy in principle, tough to get right in practice)
- Read:
  - Angel, sections 9.1 - 9.6 [reader pp. 169-185]
  - OpenGL Programming Guide, chapter 3 [available [online](#)]