

Modeling Time-Triggered Protocols and Verifying Their Real-Time Schedules

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Time-triggered systems

Time-triggered systems are **distributed** systems in which the nodes' local clocks stay synchronized within some bound.

Characteristics include:

- :) Behavior is driven according to the **passage of time** and a **globally-known schedule**.
 - ▶ Protocols execute in *rounds*; each round has a **communication** and **computation** phase.
 - ▶ Opposed to **event-triggered** behavior, which is driven by the **occurrence of events**.
- :) Allows **real-time behavior** & and **fault-tolerance** to be treated at the platform level rather than being application-specific.
 - ▶ **Predictable** and **analyzable** since they're "almost synchronous."
 - ▶ Relieves application programmers from dealing with these issues.
 - ▶ Makes reasoning about fault-tolerance easier.
- :(Worse performance under unusual/peak workloads.

How the paper came about

- ▶ I was formally verifying NASA Langley's SPIDER time-triggered protocols.
- ▶ ...And I thought I'd apply John Rushby's paper, *Systematic formal verification for fault-tolerant time-triggered algorithms* (IEEE TSE, 1999).
- ▶ ...But I realized I needed to **extend the theory**.
- ▶ ...So starting with Rushby's original specs and proofs, I **added my own axioms** and generalized some of the existing theory.

The story (continued)

- ▶ ...Worried that I'd introduced an **inconsistency**, I did a **formal theory interpretation** (i.e., show the axioms have a model) in PVS to **prove the consistency** of my added axioms.
- ▶ ...But I could find **no satisfying model!**
- ▶ ...But my axioms *looked* right.
- ▶ ...After longer than I'd like to admit, I realized Rushby's axioms were **inconsistent**: 3 of the 4 system assumptions were inconsistent.
- ▶ ...So I wrote a note to IEEE TSE (2006) mending the axioms.

An example inconsistent axiom

- ▶ *Inverse Clock*: a total function from *realtime* to *clocktime*:
 $C_\rho : \mathbb{R} \rightarrow \mathbb{N}$.
- ▶ The drift of nonfaulty clocks is bounded by a realtime constant $0 < \rho < 1$.
- ▶ *Clock Drift Rate* axiom: For all realtimes t_1 and t_2 ,
 $(1 - \rho)(t_1 - t_2) \leq C_\rho(t_1) - C_\rho(t_2) \leq (1 + \rho)(t_1 - t_2)$.

The axiom is **inconsistent**, in **three** separate ways!

Proof.

One proof is...



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One proof is... By contradiction. Let $t_2 > t_1$. Then $(1 - \rho)(t_1 - t_2) > (1 + \rho)(t_1 - t_2)$, so there is no $i \in \mathbb{N}$ between the bounds. □

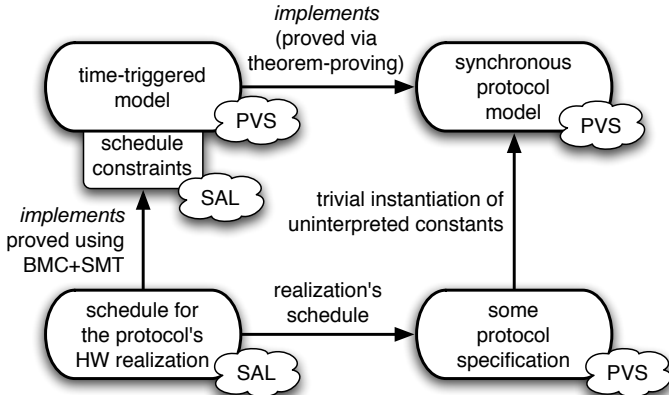
John Rushby

Please keep in mind

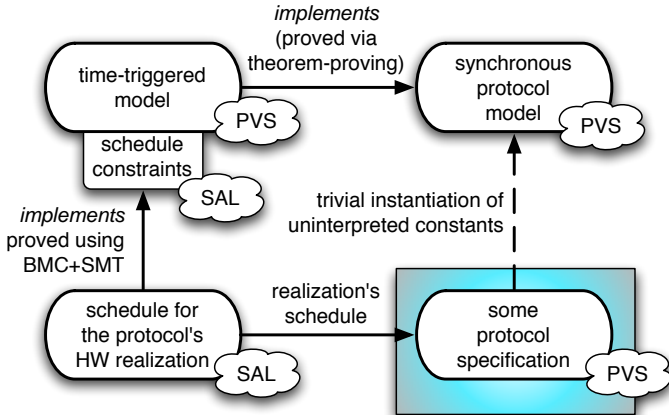
- ▶ The **concepts** behind Rushby's theory were **correct**.
- ▶ I uncovered the errors because Rushby **publicized** his specs (thanks!).
- ▶ Referees (twice) **overlooked the errors**, as well as researchers citing the work (including me).
- ▶ Rushby's work in time-triggered system verification is **seminal** (like his work in security, mechanical theorem-proving, etc.).

Okay, onto the actual methodology...

Verification approach



Verification approach



Synchronous specification

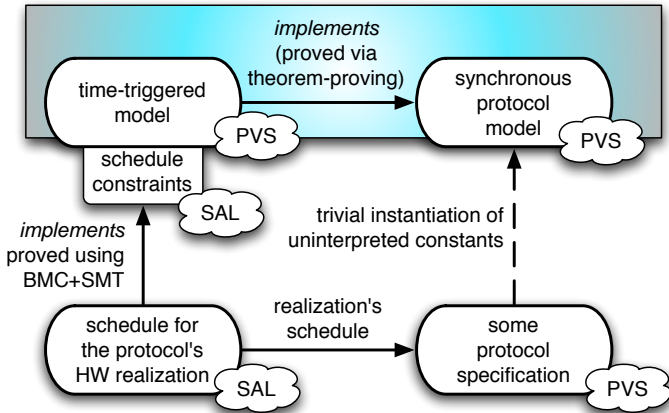
$$\begin{aligned} \text{run}(r, s) &\stackrel{\text{df}}{=} \\ &\text{if } r = 0 \text{ then } s \\ &\text{else } \lambda p. \text{trans}_p(\text{run}_p(r - 1, s), \\ &\quad \lambda q. \text{msg}_q(\text{run}_q(r - 1, s), p)), \\ &\text{where } q \in \text{in_nbrs}_p \end{aligned}$$

trans_p : state-transition function for node p .

msg_q : message-generation function for node q .

in_nbrs_p : inbound-neighbor-nodes for node p .

Part I: the theory



Part I: the theory

The theory Rushby built and I expanded upon is an **axiomatic** theory of time-triggered protocols. The axioms fall into the following categories:

1. **System assumptions** (4 axioms)

Assumptions made about the underlying clocks—e.g., clock monotonicity, drift rate, skew bound, & communication delay.

2. **Schedule constraints** (6 axioms)

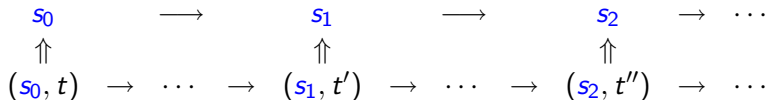
Constraints on the local schedules—e.g., computation phase, communication phase, reception windows, & pipelining.

3. **Semantics** (9 axioms)

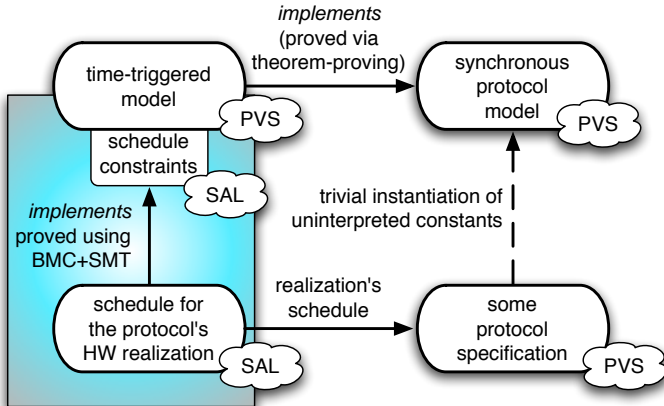
The semantics of time-triggered behavior is a transition system, the states of which are (s, t) where s is the **global state of the system** and t is a **realtime**. The transitions between states are constrained by the axioms.

The simulation theorem

Via taking “cuts” at regular points in time:



Part II: the implementation



SAL in a slide

SRI's Symbolic Analysis Laboratory (SAL) is a [GPL open-source](#) high-level language interface & model-checking tools:

- ▶ The language includes predicate subtypes, higher-order functions, algebraic datatypes, etc.
- ▶ To a [family of model checkers](#) (symbolic, explicit, and bounded).
- ▶ And other tools like a deadlock checker, path-finder, test-case generator, etc.
- ▶ And a SMT solver (mainly SRI's Yices).

Verifying the schedules

1. The **six schedule constraints** are reformulated from PVS into SAL (nearly verbatim).

Schedule constraints

1. **Offset constraint** $0 < P(r) < sched(r + 1) - sched(r)$.
2. **Communication Constraint #1**
 $D(r) \geq \Sigma(r) + \Lambda(r) - \lfloor (1 - \rho) \cdot (\delta_{nom} - e_l) \rfloor$.
3. **Computation offset constraint**
 $P(r) > D(r) + \Sigma(r) + \Lambda(r) + \lceil (1 + \rho) \cdot (\delta_{nom} + e_u) \rceil$.
4. **Pipeline constraint** $\neg independent(r)$ implies $D(r) \geq 0$.
5. **Communication constraint #2** $r > 0$ implies
 $D(r) \geq P(r - 1) - sched(r) + sched(r - 1)$.
6. **Reception window constraint**
 $0 \leq R(r) \leq D(r) + \lfloor (1 - \rho) \cdot (\delta_{nom} - e_l) \rfloor - \Sigma(r) - \Lambda(r) + 1$.

$sched(r)$: clocktime round r begins.

$P(r)$: clocktime offset computation begins in round r .

$D(r)$: clocktime offset when communication begins in round r .

$\Lambda(r)$: maximum schedule discrepancy in round r .

$\Sigma(r)$: maximum clock skew in round r .

Verifying the schedules

1. The **six schedule constraints** are reformulated from PVS into SAL (nearly verbatim).
2. Schedules for the hardware are specified as simple **infinite-state** machines (variables & constraints from the reals and integers).
 - ▶ State variables include the round counter and schedule-variables (e.g., computation offset, communication offset, reception window opening time, etc).
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 - ▶ State variables may be **nondeterministically** updated.
3. We **prove** the constraints using infinite-state bounded model checking via ***k*-induction**.
 k = number of rounds of the protocol.

Lessons (re)-learned

- ▶ Don't be a verification **purist**! Or as J. Moore put it...

Quoting J. Moore

February 27, 2007, ac12@lists.cc.utexas.edu

I think of theorem provers sort of like vehicles. What is the best kind of vehicle to buy? Isn't that silly question? If you're hauling kids to soccer practice, it might be a minivan. If you're hauling hay to the cattle, it might be a pickup.

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- ▶ A benefit of FV is to give engineers confidence that **aggressive optimizations** are **provably correct**.
- ▶ Try out **infinite-state bounded model checking** for real-time verification!

Towards a complete verification story

Abstraction levels:

- ▶ Application properties.
- ▶ Synchronous protocol abstraction. } Miner et. al., FTRTFT'04
- ▶ Time-triggered protocol abstraction. } This paper
- ▶ Real-time constraints. }
- ▶ Distributed communicating state-machines. } Schmaltz, FMCAD'07
- ▶ HW realization & physical-layer protocols. } Knapp&Paul, LNCS4444

SPIDER is open-spec and is a great testbench for new approaches!

Thanks

Steve Johnson, Paul Miner, Geoffrey Brown, Larry Moss, and Wilfredo Torres-Pomales.

I was extraordinarily impressed with the thoroughness of my anonymous reviewers. Thanks!

Web resources

Slides, specifications, and proofs

http://www.cs.indiana.edu/~lepik/pub_pages/fmcd.html

Google: lee pike fmcad

NASA SPIDER

<http://shemesh.larc.nasa.gov/fm/spider/>

Google: spider nasa

PVS & SAL

<http://fm.csl.sri.com/>

Google: formalware (please ignore tuxedo-related Google ads)