



# Efficient Symbolic Execution for Software Testing

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# Symbolic Execution

- Automatically explore program paths
  - *Execute program on “symbolic” input values*
  - *“Fork” execution at each branch*
  - *Record branching conditions*
- Constraint solver
  - *Decides path feasibility*
  - *Generates test cases for paths and bugs*

# Symbolic Execution

- (Very brief) history
  - *Test generation by SE in 70s* [King '75] [Boyer et al. '75]
  - *SAT / SMT solvers lead to boom in 2000s*  
[Godefroid et al. '05][Cadar et al. '06]
- Many successful tools
  - *KLEE, SAGE, PEX, SPF, CREST, Cloud9, S2E, ...*
- Specific advantages
  - *No false positives, useful partial results*
  - *Reduces need for modeling*

# Outline

- Symbolic Execution for Testing
- State Merging – Fighting Path Explosion
- Interpreted High-Level Code

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- Symbolic Execution for Testing
- State Merging – Fighting Path Explosion
- Interpreted High-Level Code

*pc* = true

*x* = *X*

*r* = 0

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1  int proc(int x) {  
2  
3    int r = 0  
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6    if (x > 8) {  
7      r = x - 7  
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Symbolic  
program state

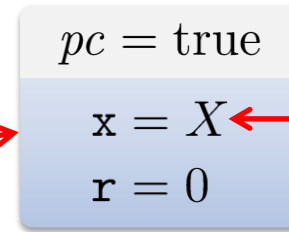
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$x = X$

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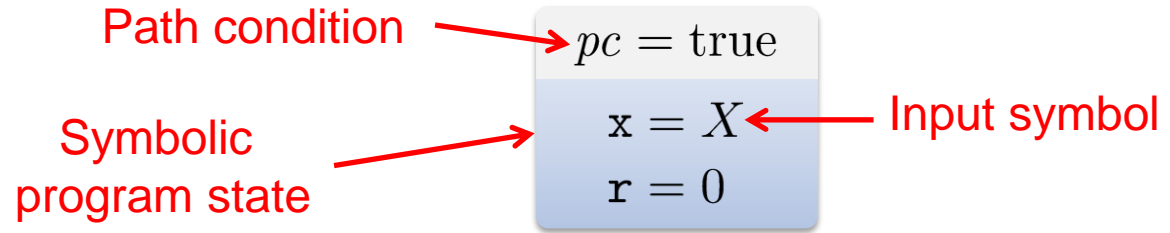
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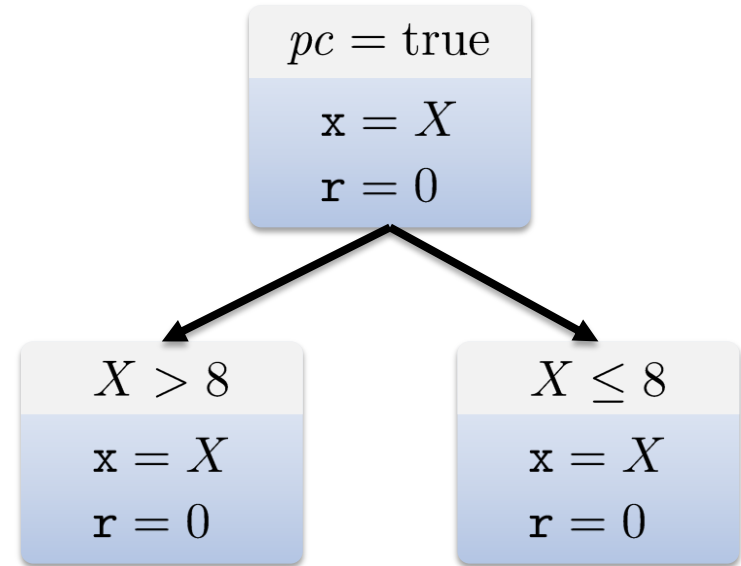
Input symbol



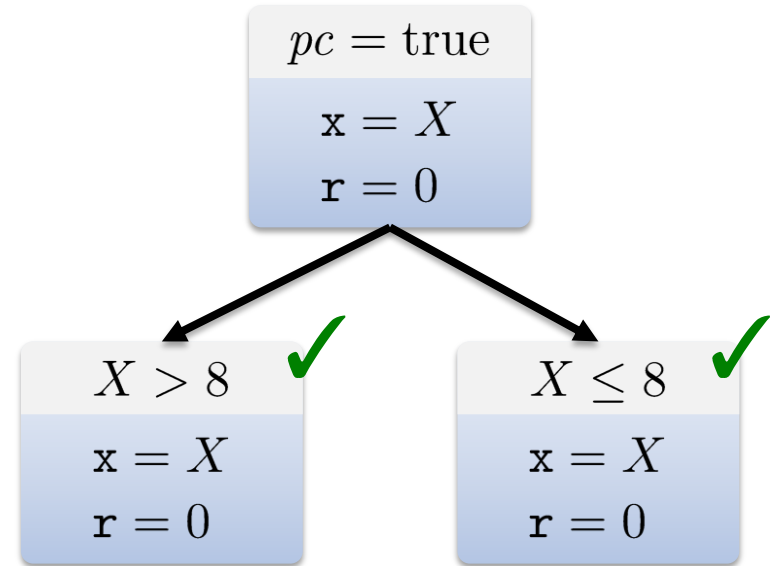
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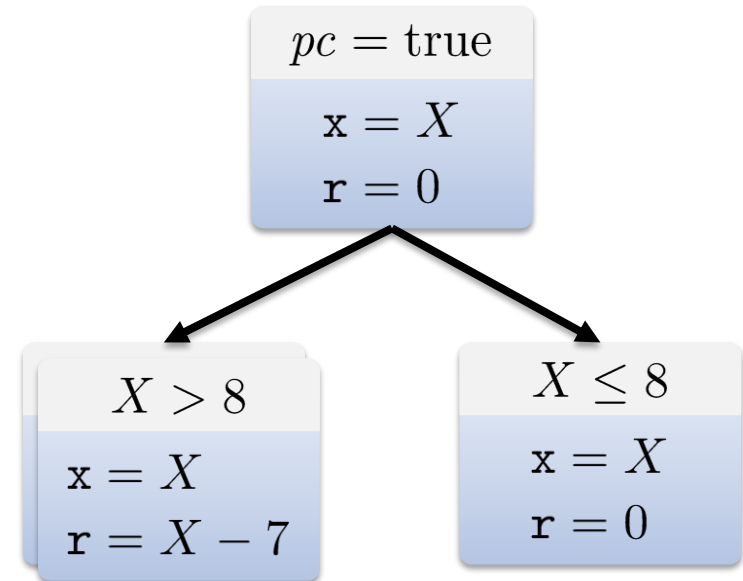
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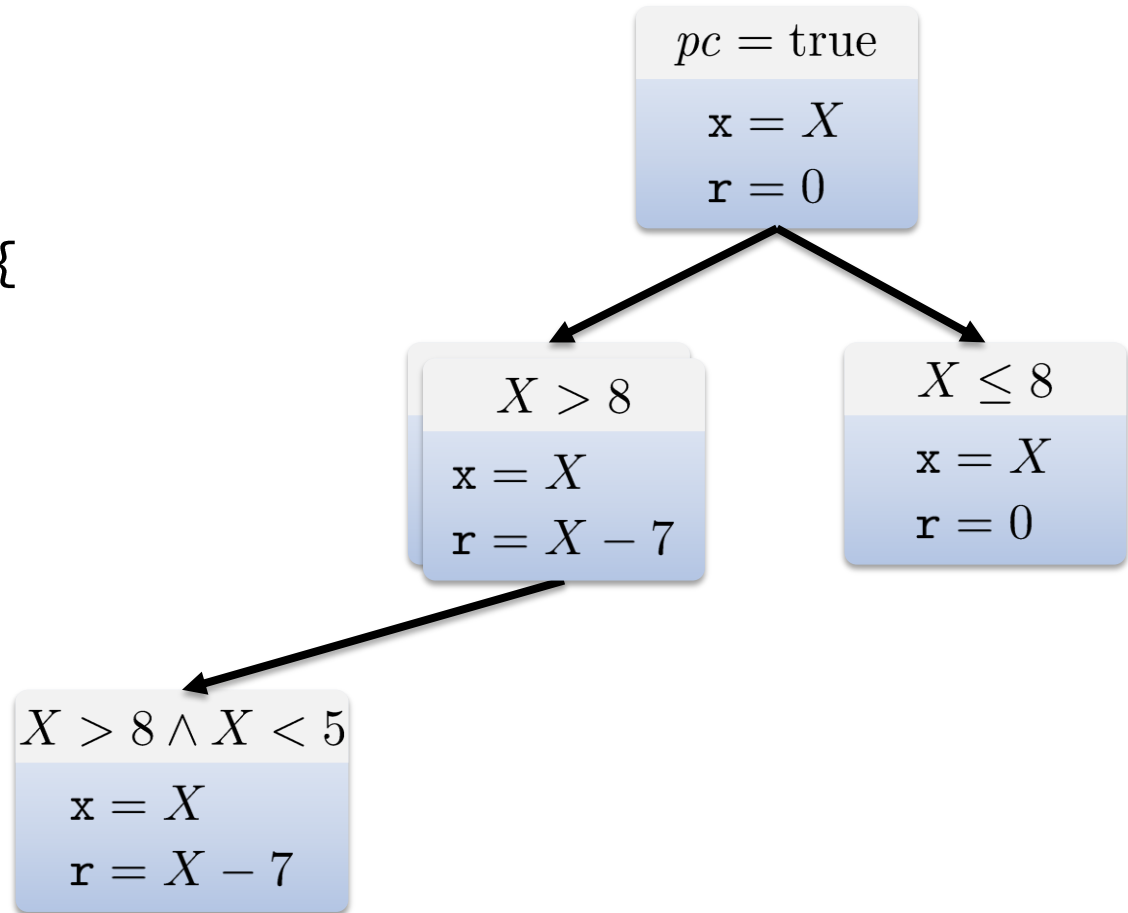
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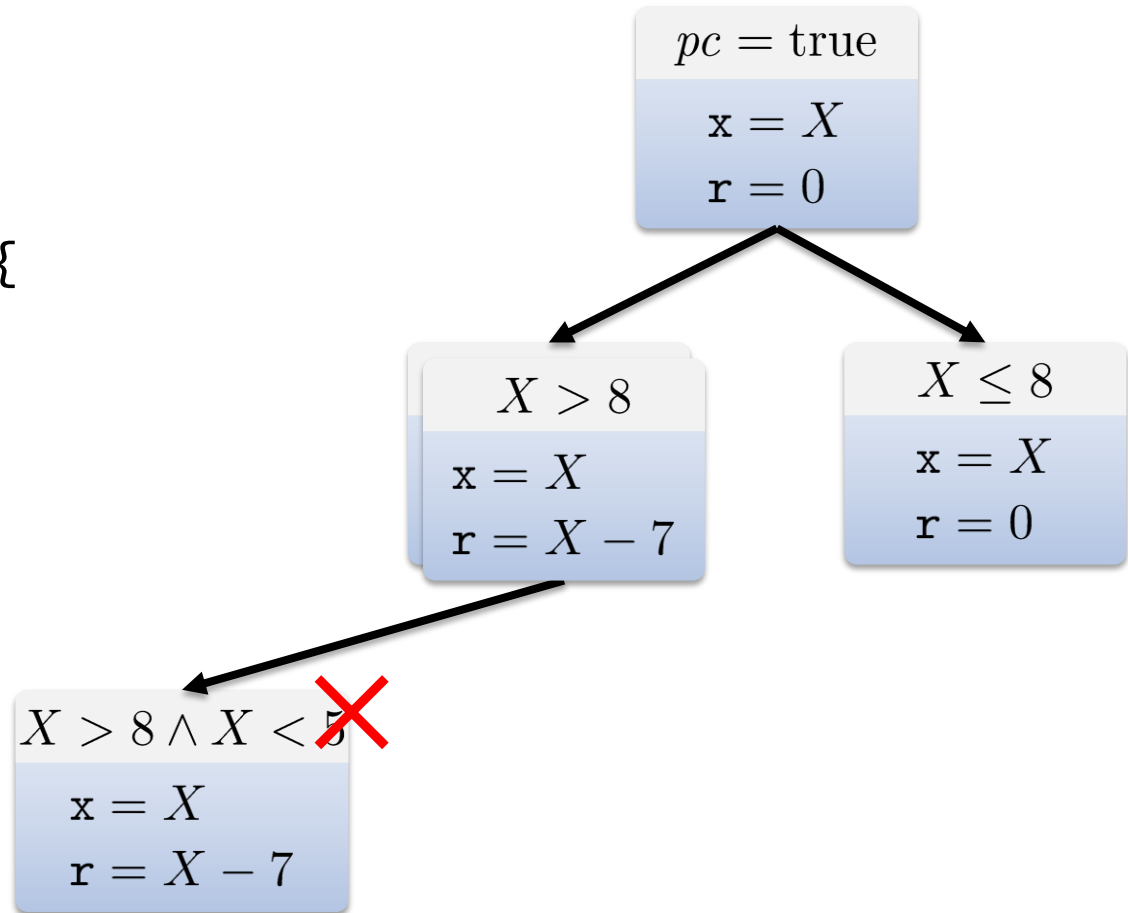
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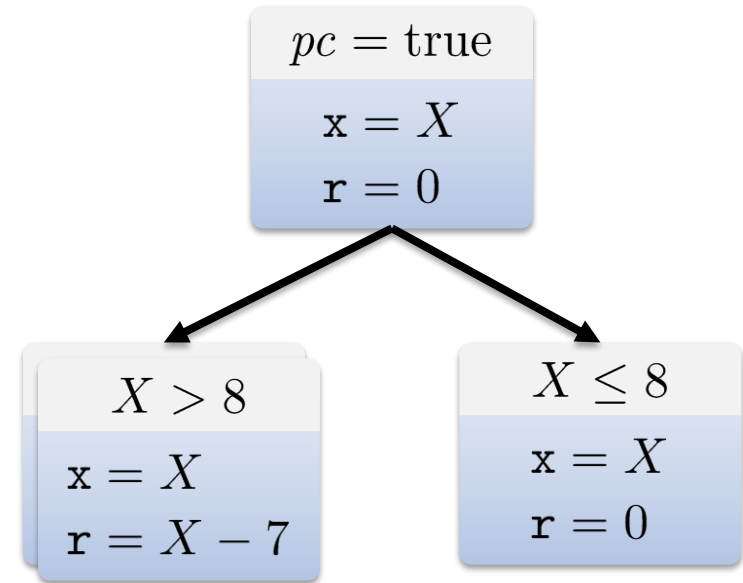
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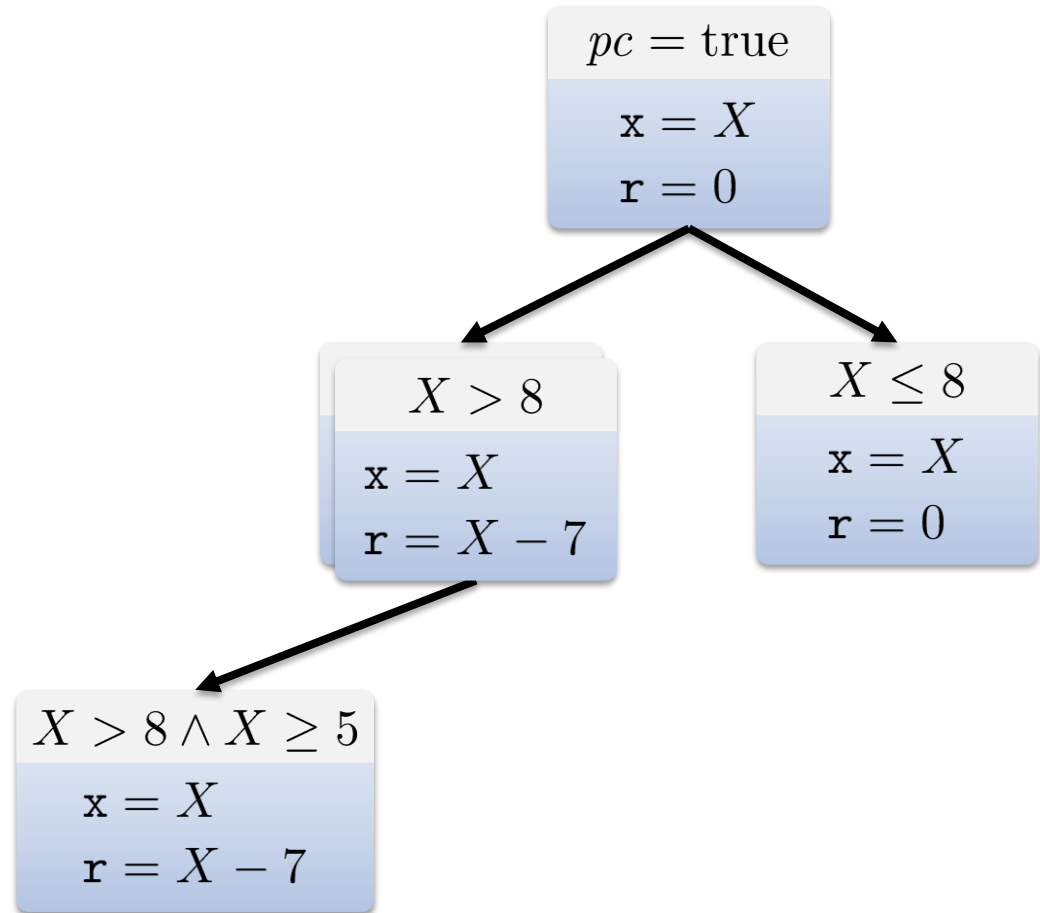
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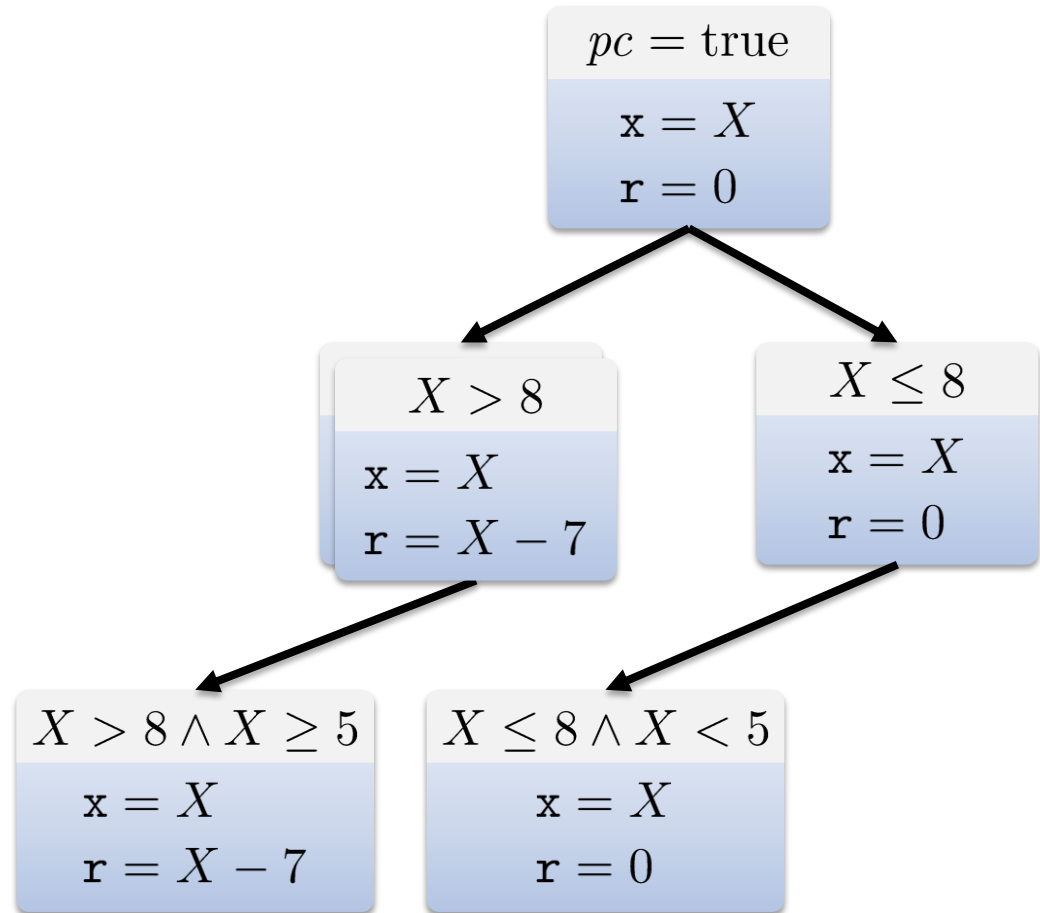




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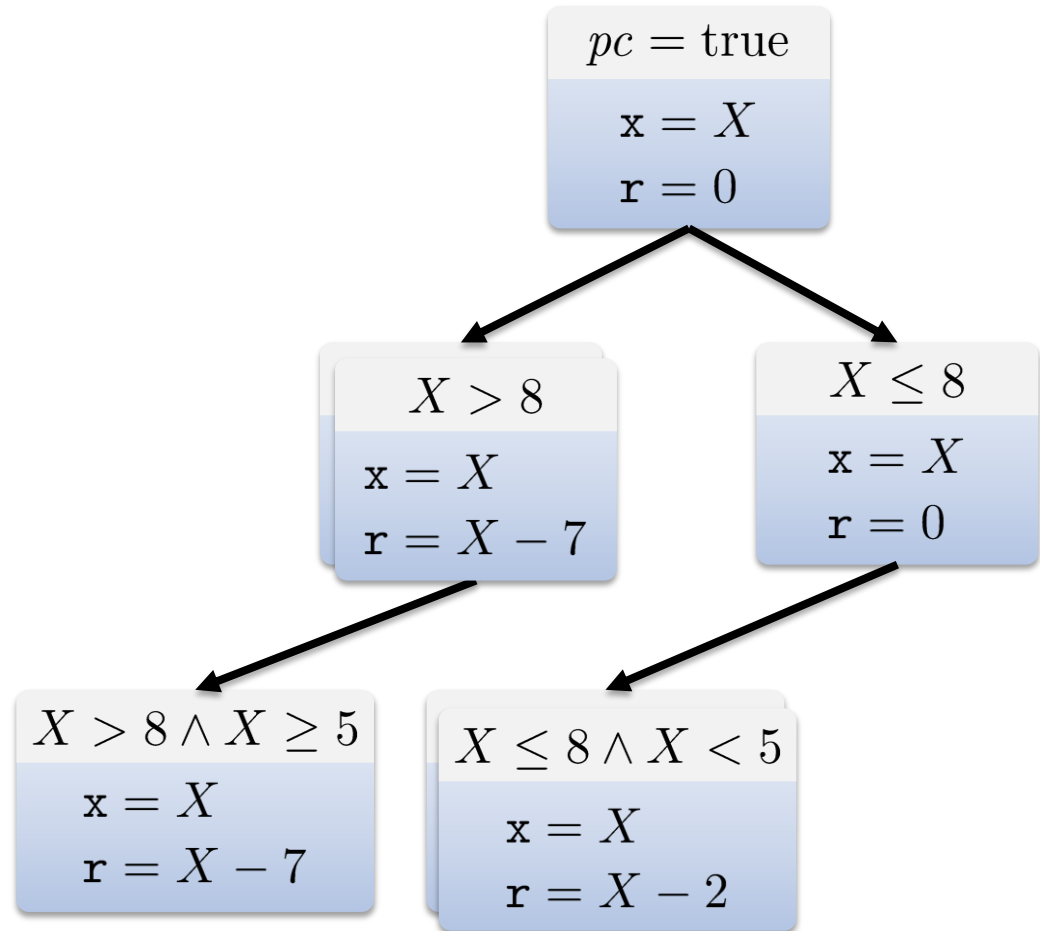
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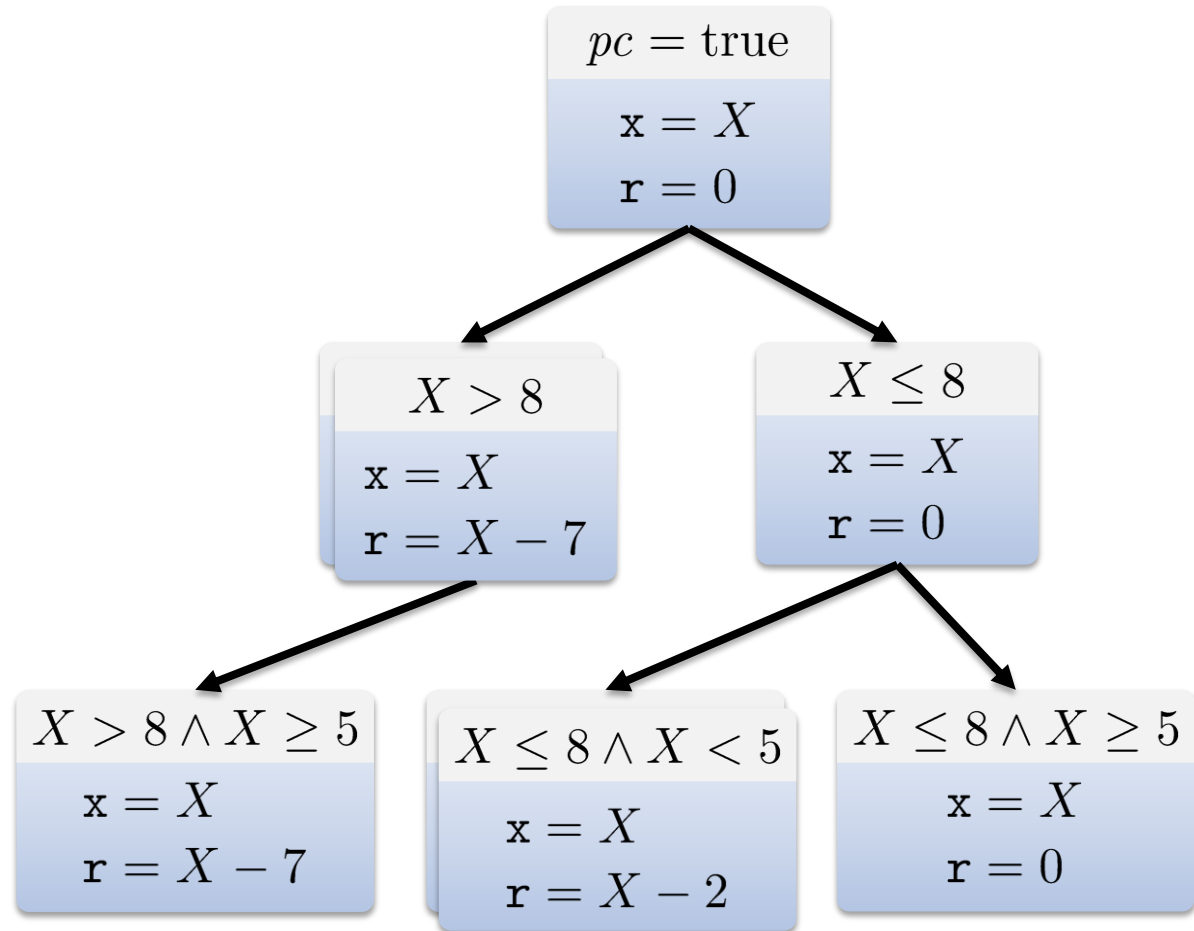
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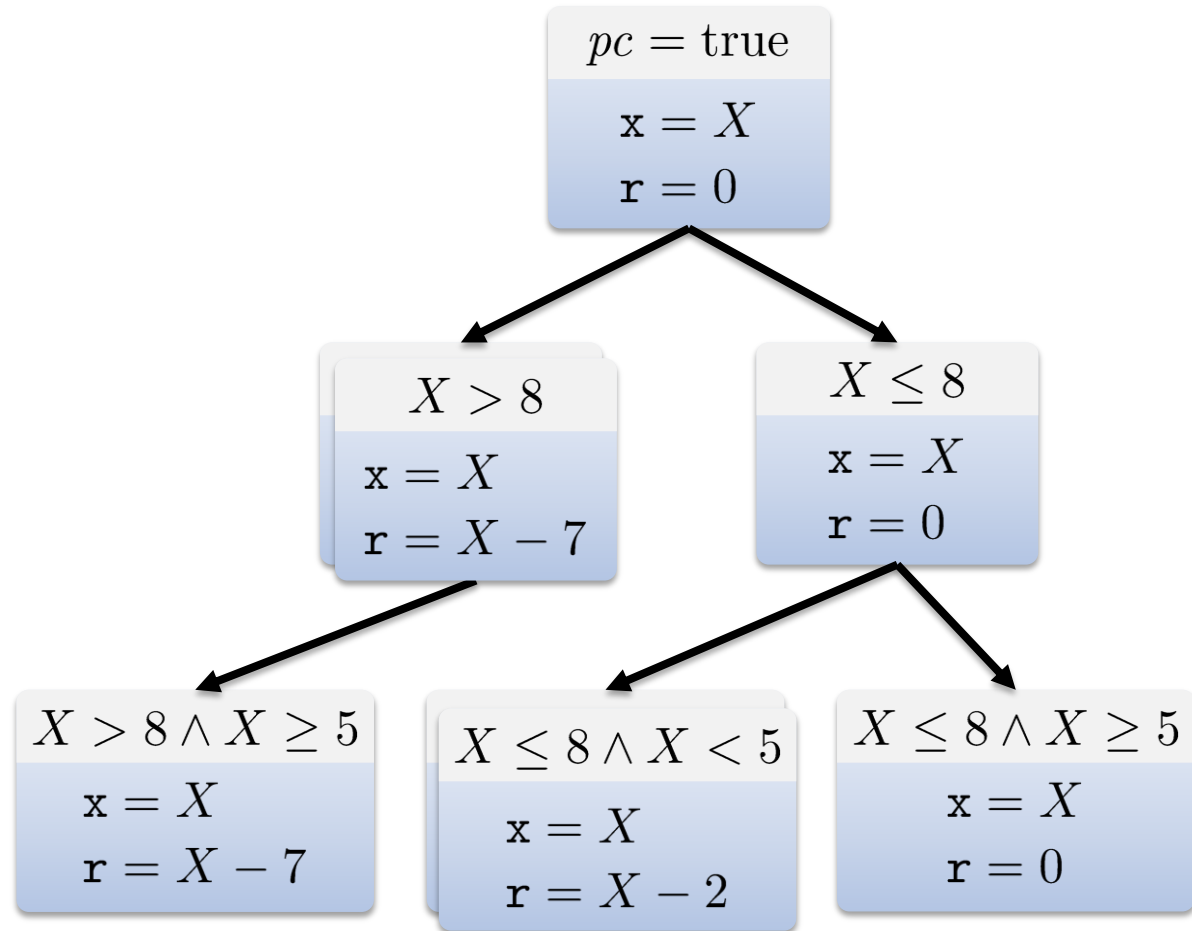
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Satisfying assignments:

$$X = 9$$

$$X = 4$$

$$X = 7$$

Test cases:

proc(9)

proc(4)

proc(7)

# Finding Bugs

- Symbolic execution enumerates paths
  - *Runs into bugs that trigger whenever path executes*
  - *Assertions, buffer overflows, division by zero, etc., require specific conditions*
- Error conditions
  - *Treat assertions as conditions*

`assert x != NULL`        `if (x == NULL)  
abort();`

- *Creates explicit error paths*

# Finding Bugs

- Instrument program with properties
  - *Translate any safety property to reachability*
- Division by zero

$y = 100 / x$



`assert x != 0`  
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- Instrument program with properties
  - *Translate any safety property to reachability*
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`y = 100 / x`            `assert x != 0`  
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- Buffer overflows

`a[x] = 10`            `assert x >= 0 && x < len(a)`

# Finding Bugs

- Instrument program with properties
  - *Translate any safety property to reachability*

- Division by zero

$y = 100 / x$             `assert x != 0`  
`y = 100 / x`

- Buffer overflows

$a[x] = 10$             `assert x >= 0 && x < len(a)`

- Implementation is usually implicit



# Symbolic Execution Algorithms

- Static symbolic execution
  - *Simulate execution on program source code*
  - *Computes strongest postconditions from entry point*
- Dynamic symbolic execution (DSE)
  - *Run / interpret the program with concrete state*
  - *Symbolic state computed in parallel (“concolic”)*
  - *Solver generates new concrete state*
- DSE-Flavors
  - *EXE-style [Cadar et al. ‘06] vs. DART [Godefroid et al. ‘05]*

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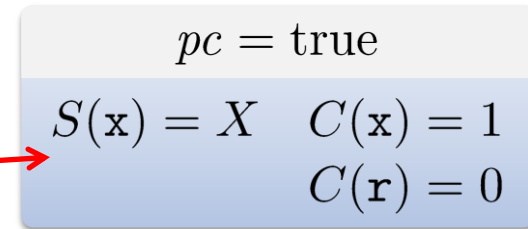
$pc = \text{true}$

$S(x) = X$     $C(x) = 1$   
 $C(r) = 0$

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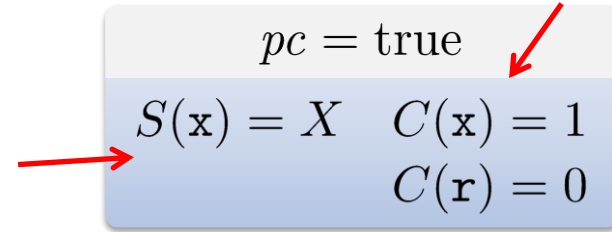
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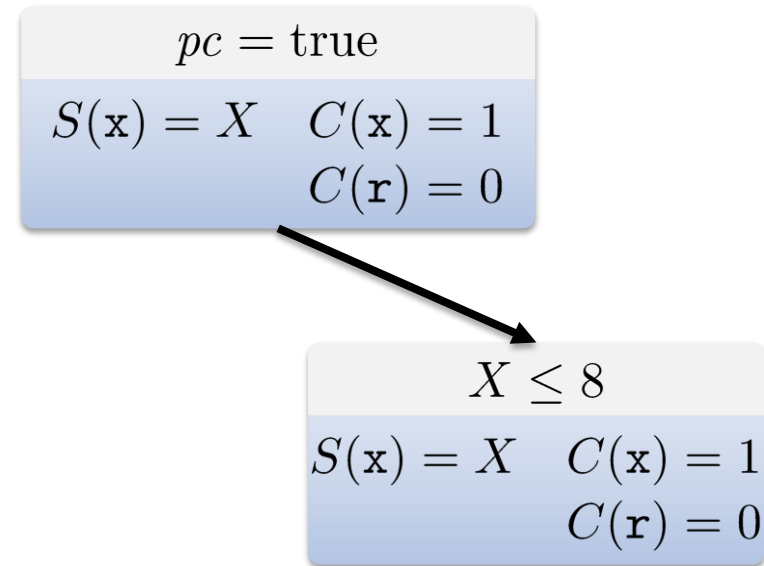
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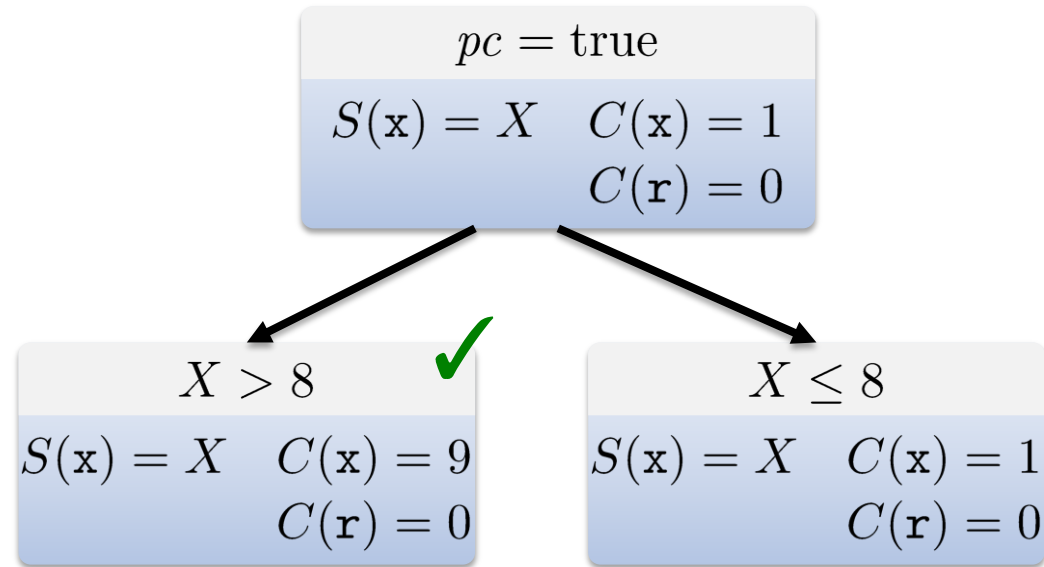
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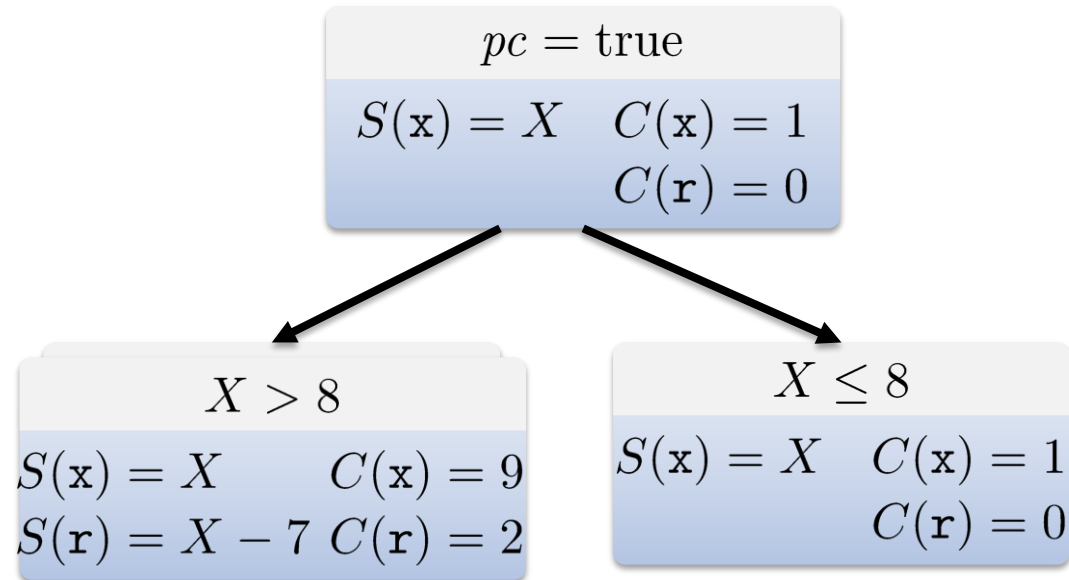
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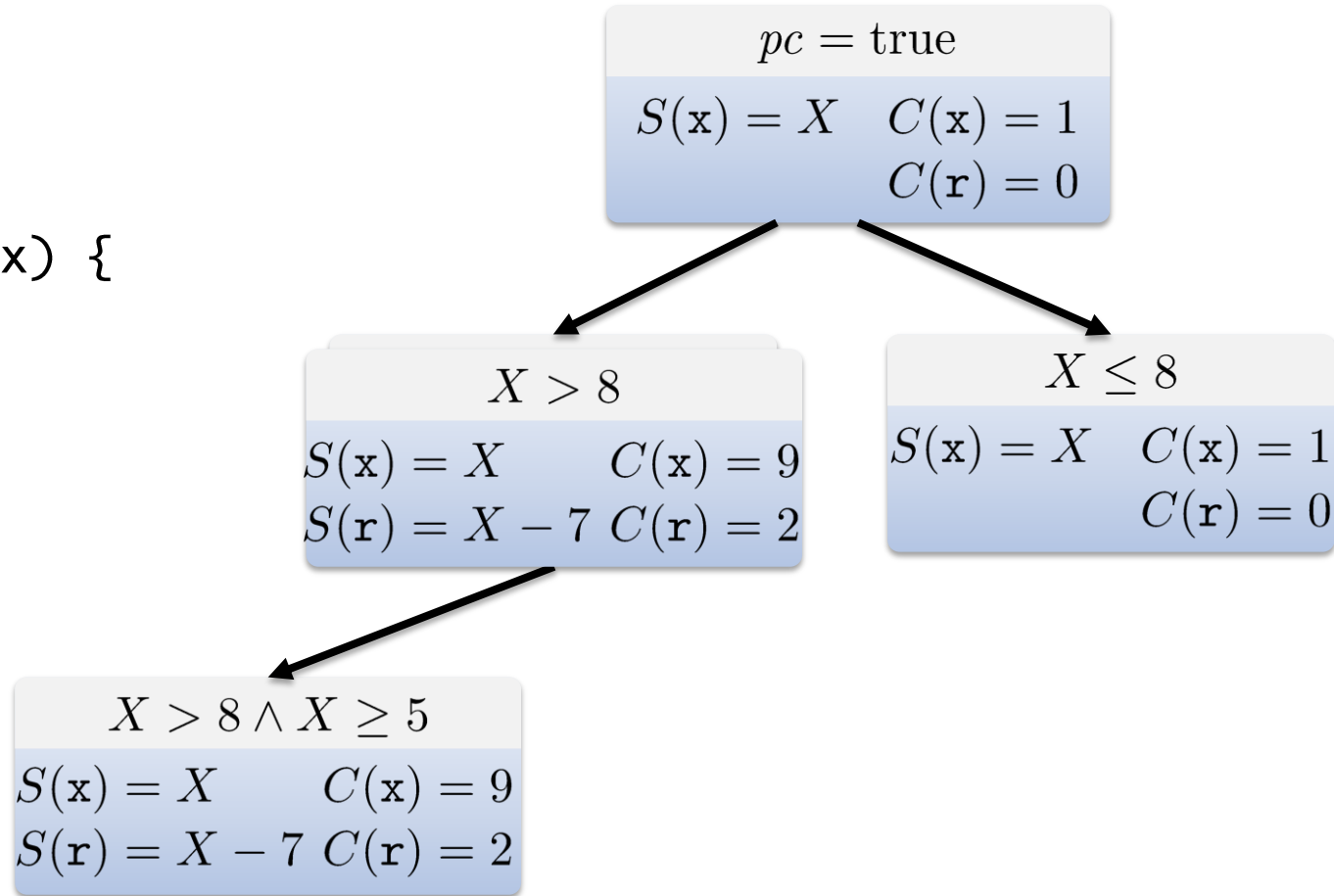
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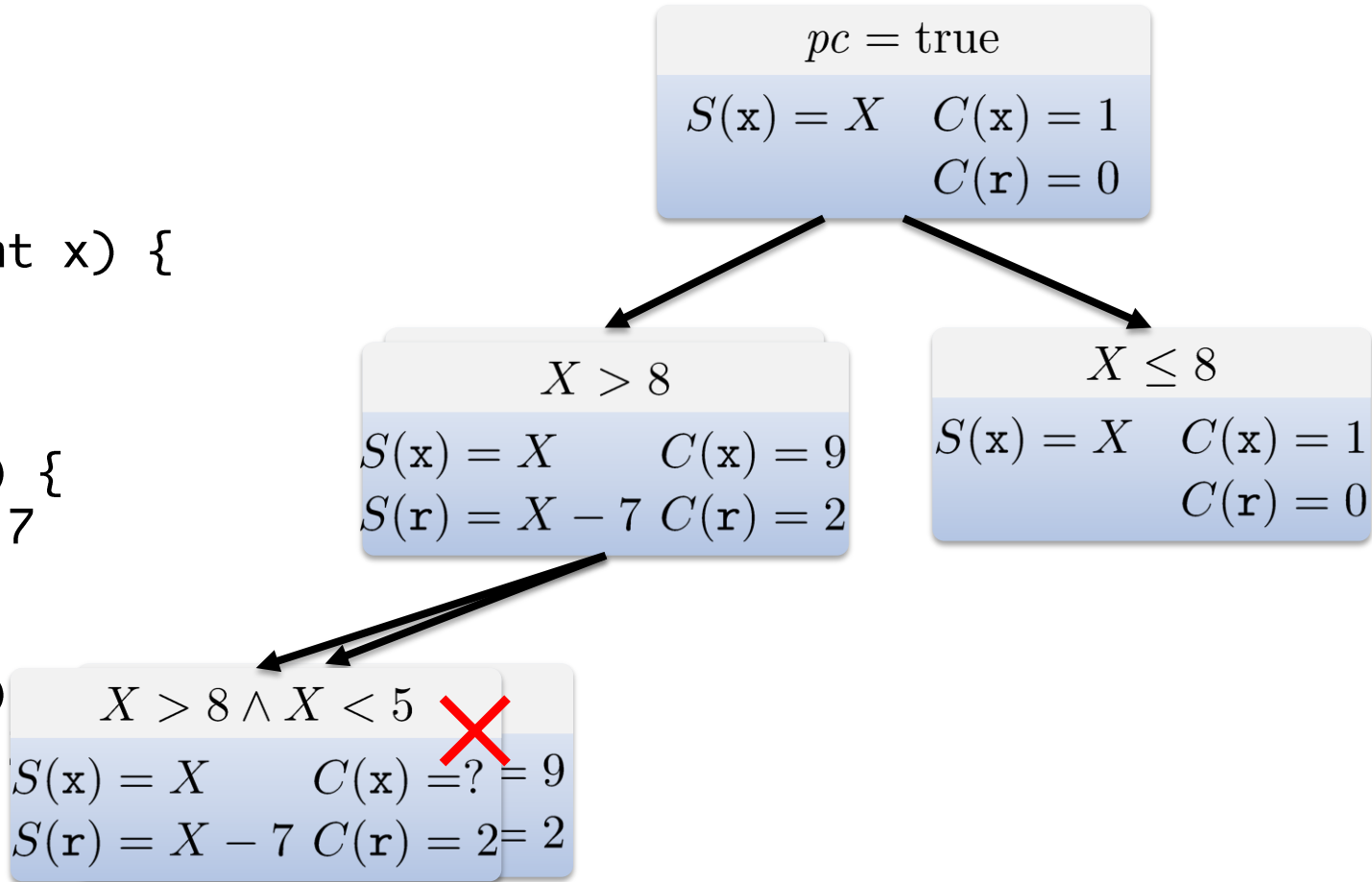


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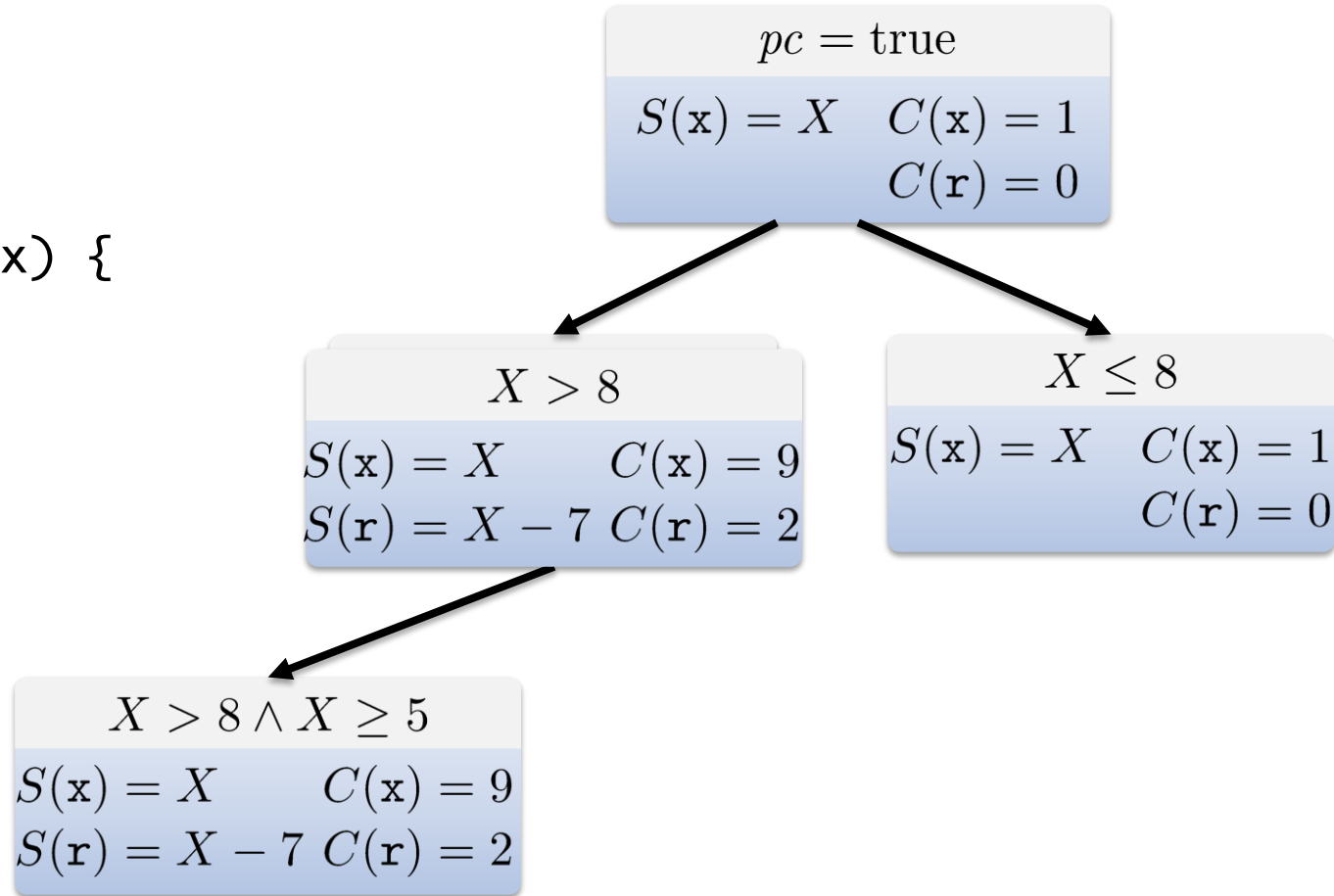
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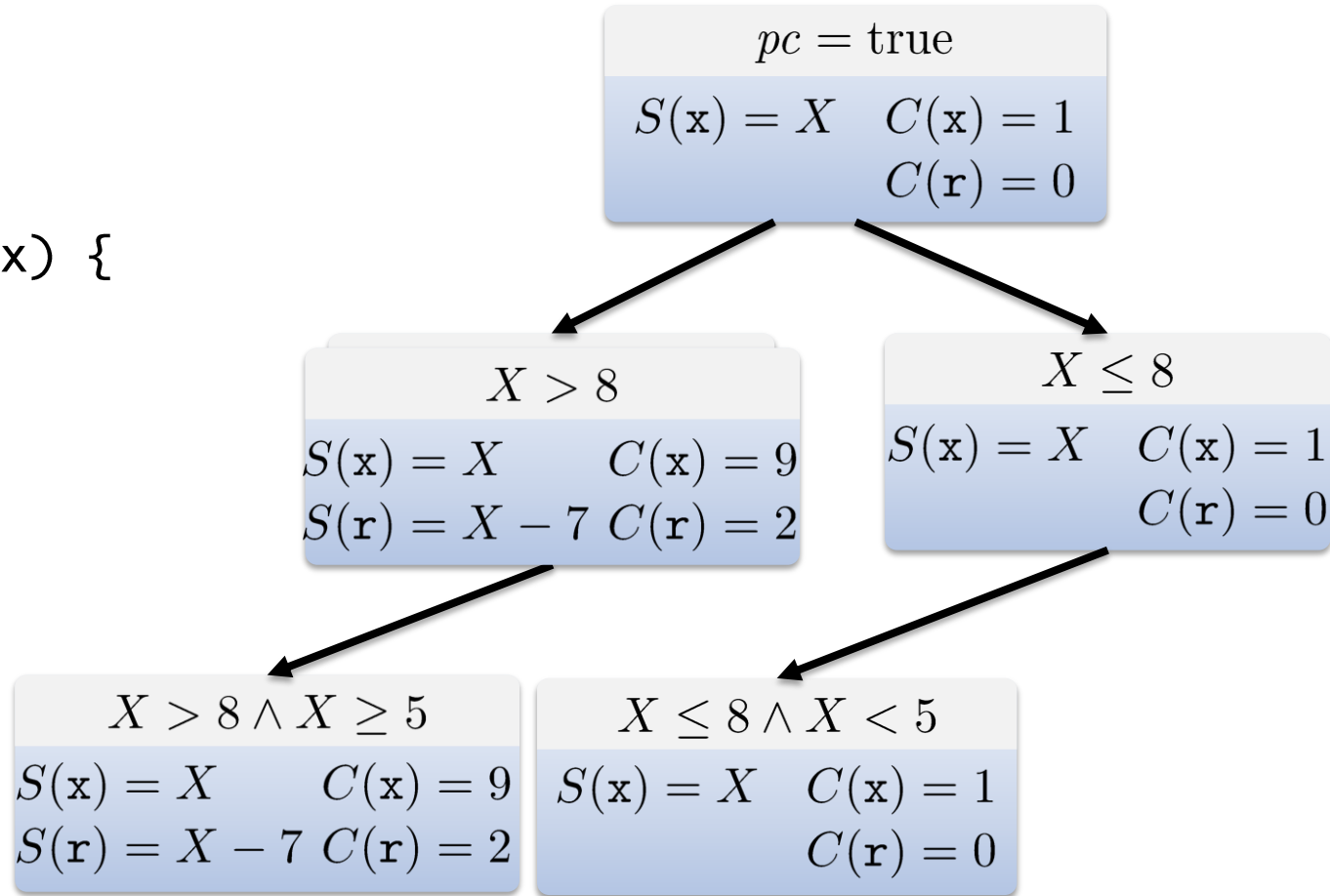
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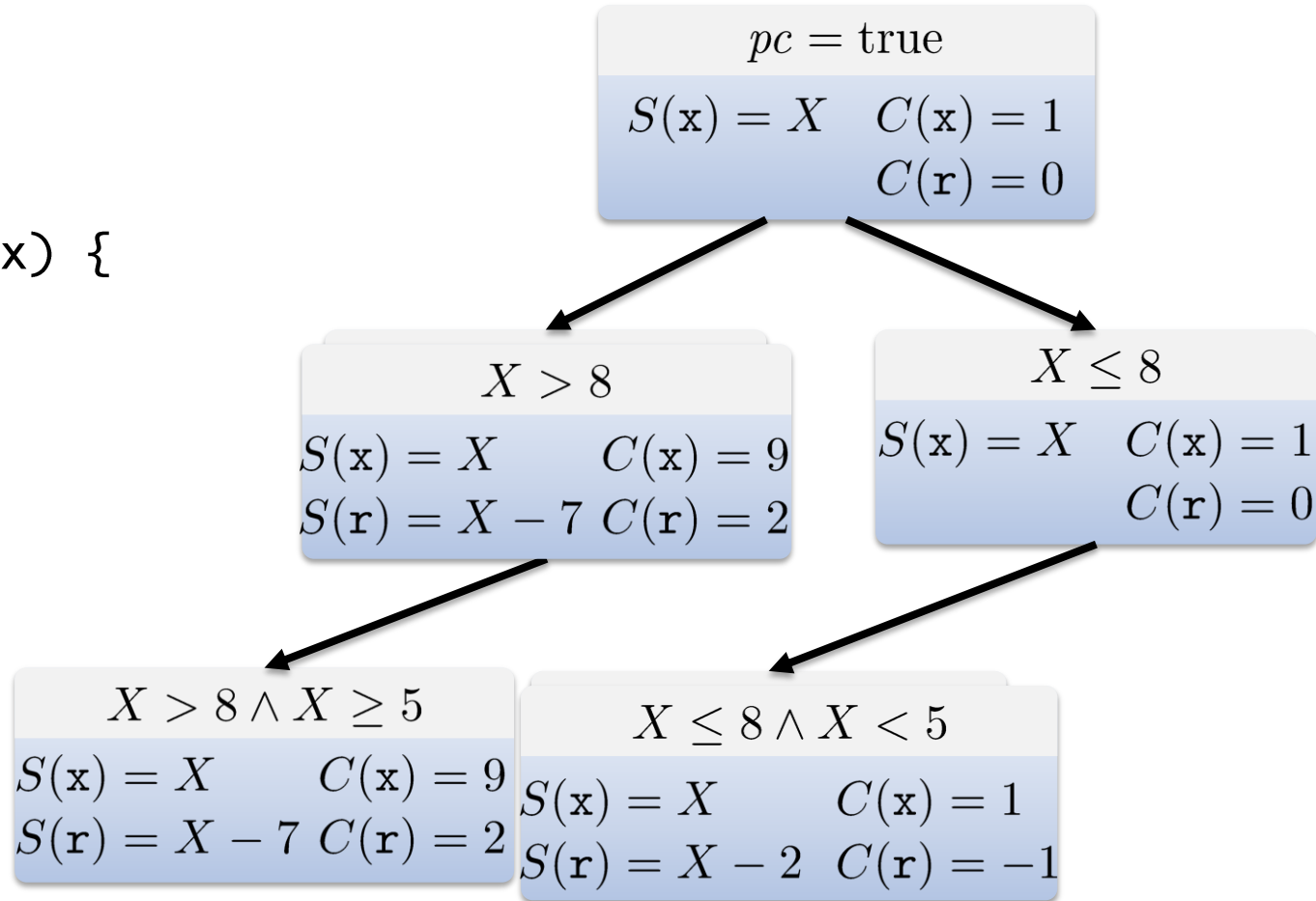
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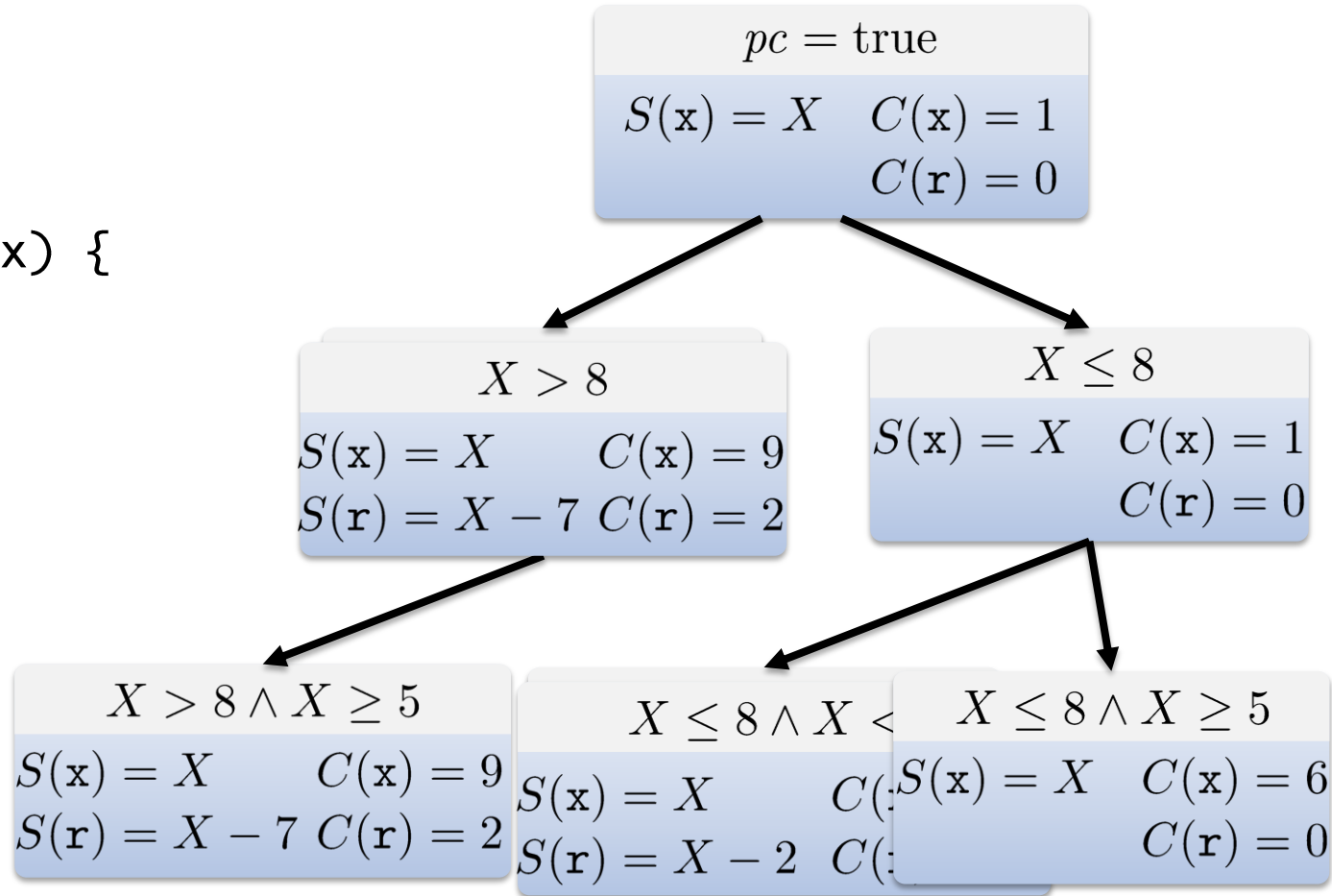


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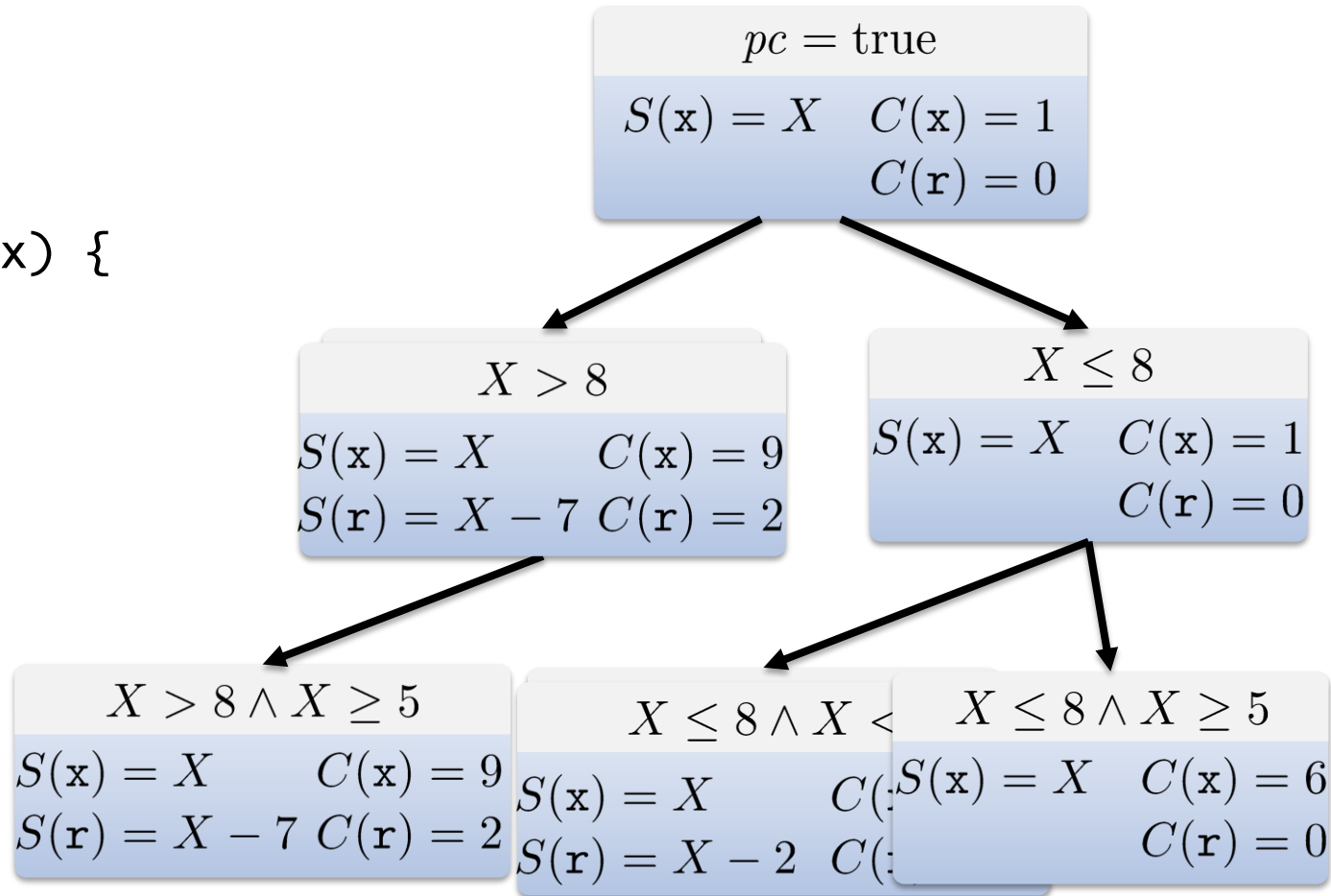


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Satisfying assignments:

$$X = 9$$

$$X = 1$$

$$X = 6$$

Test cases:

proc(9)

proc(1)

proc(6)

# DART

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Path condition:

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proc(1)



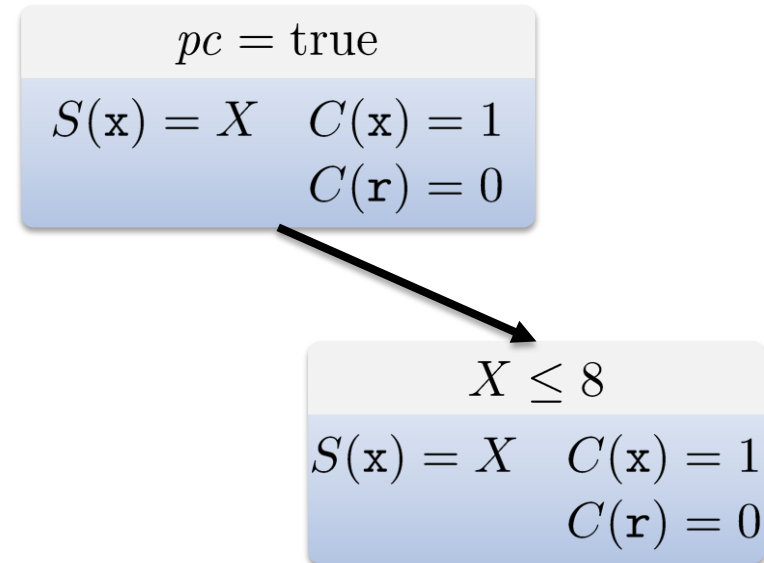
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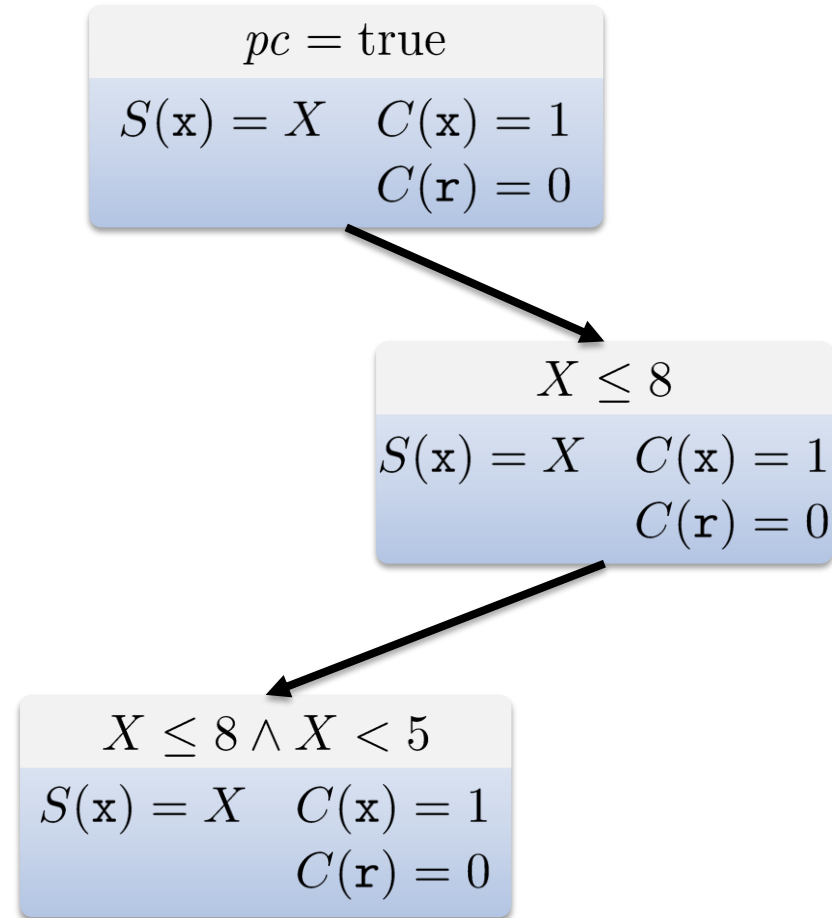
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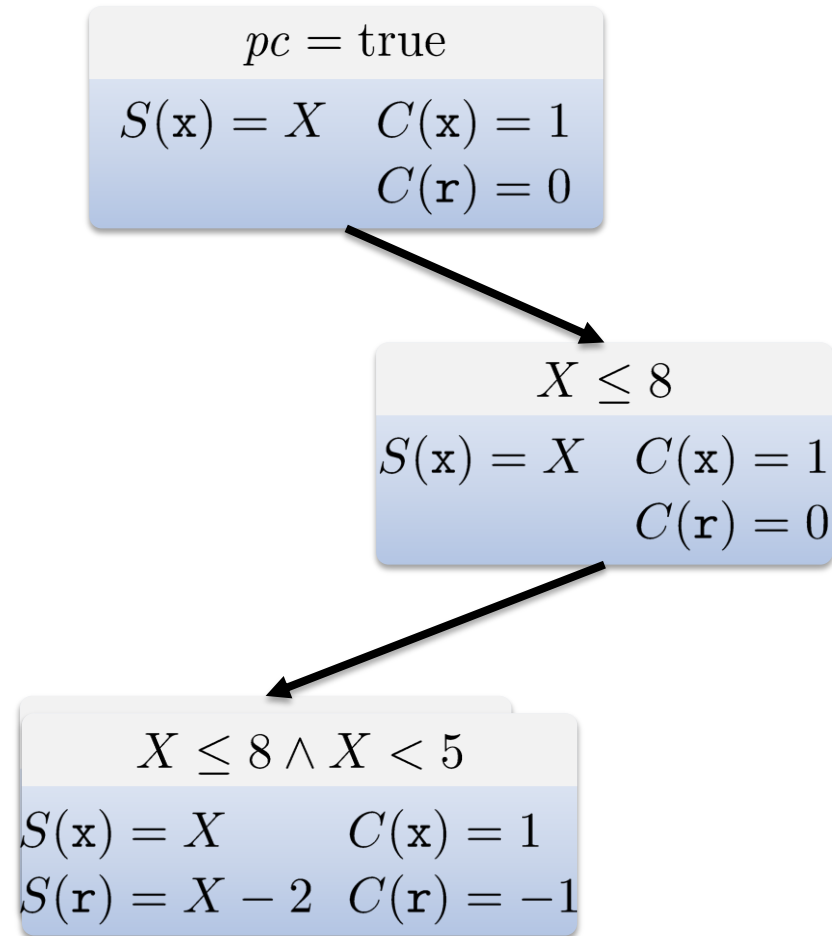
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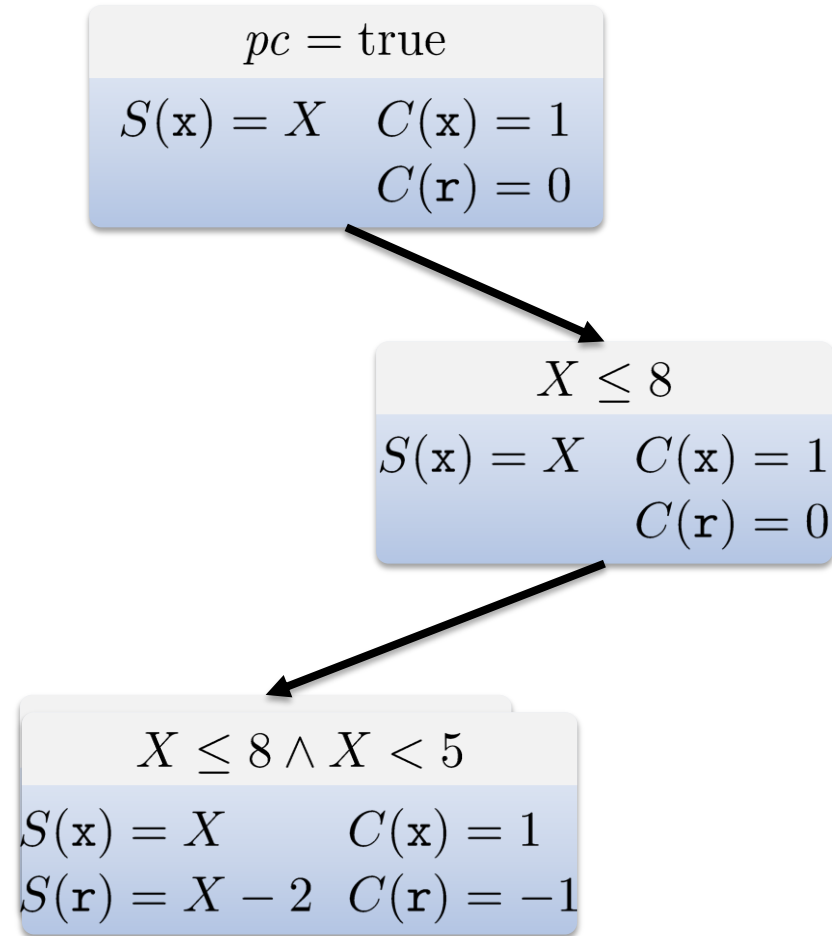
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Path condition:

$$X \leq 8 \wedge \neg(X < 5)$$

Test cases:

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Path condition:

Test cases:

$pc = \text{true}$   
 $S(\mathbf{x}) = X \quad C(\mathbf{x}) = 1$   
 $C(\mathbf{r}) = 0$

$X \leq 8$   
 $S(\mathbf{x}) = X \quad C(\mathbf{x}) = 1$   
 $C(\mathbf{r}) = 0$

$X \leq 8 \wedge X < 5$   
 $S(\mathbf{x}) = X \quad C(\mathbf{x}) = 1$   
 $S(\mathbf{r}) = X - 2 \quad C(\mathbf{r}) = -1$

$X \leq 8 \wedge \neg(X < 5)$  ✓

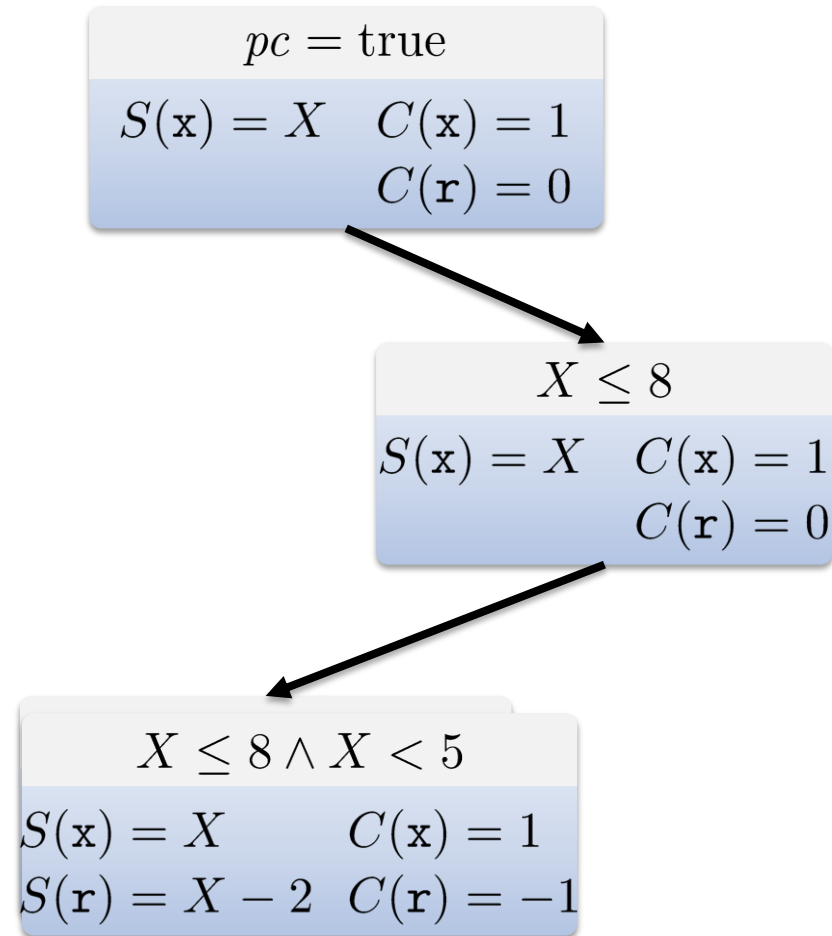
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Path condition:

Test cases:



$$X \leq 8 \wedge \neg(X < 5) \quad \checkmark$$

proc(1)

proc(6)

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```

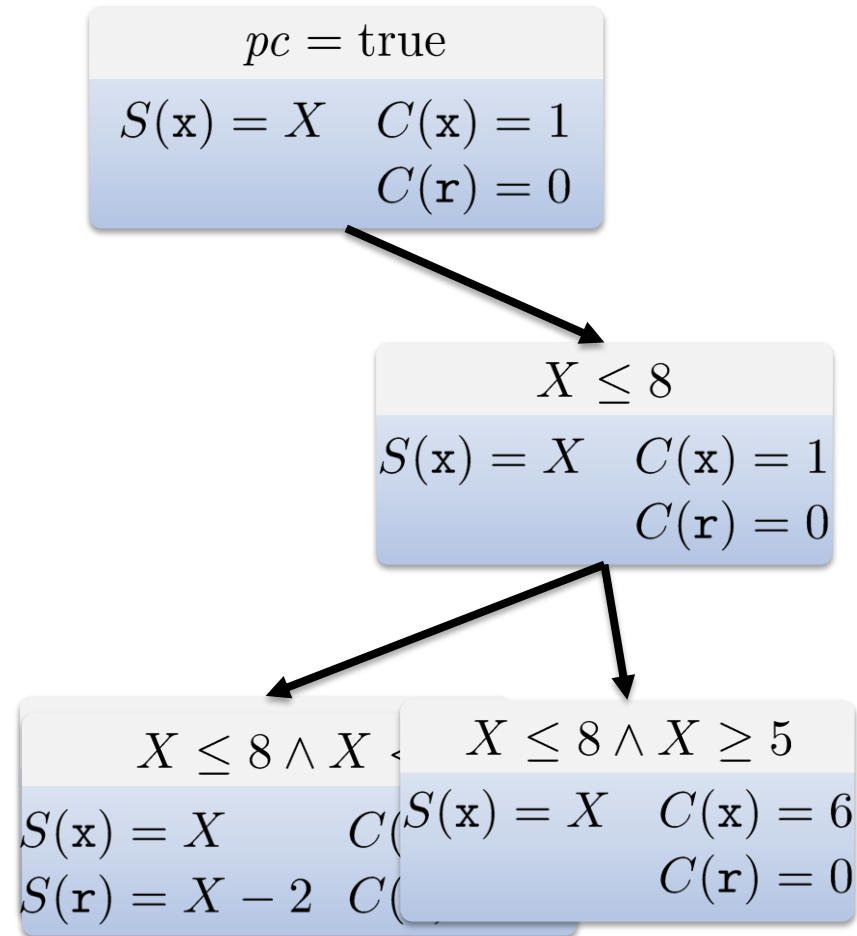
Path condition:

$$X \leq 8 \wedge \neg(X < 5)$$

Test cases:

proc(1)

proc(6)



# DART

```

1  int proc(int x) {
2
3    int r = 0
4
5
6    if (x > 8) {
7      r = x - 7
8    }
9
10   if (x < 5) {
11     r = x - 2
12   }
13
14   return r;
15 }

```

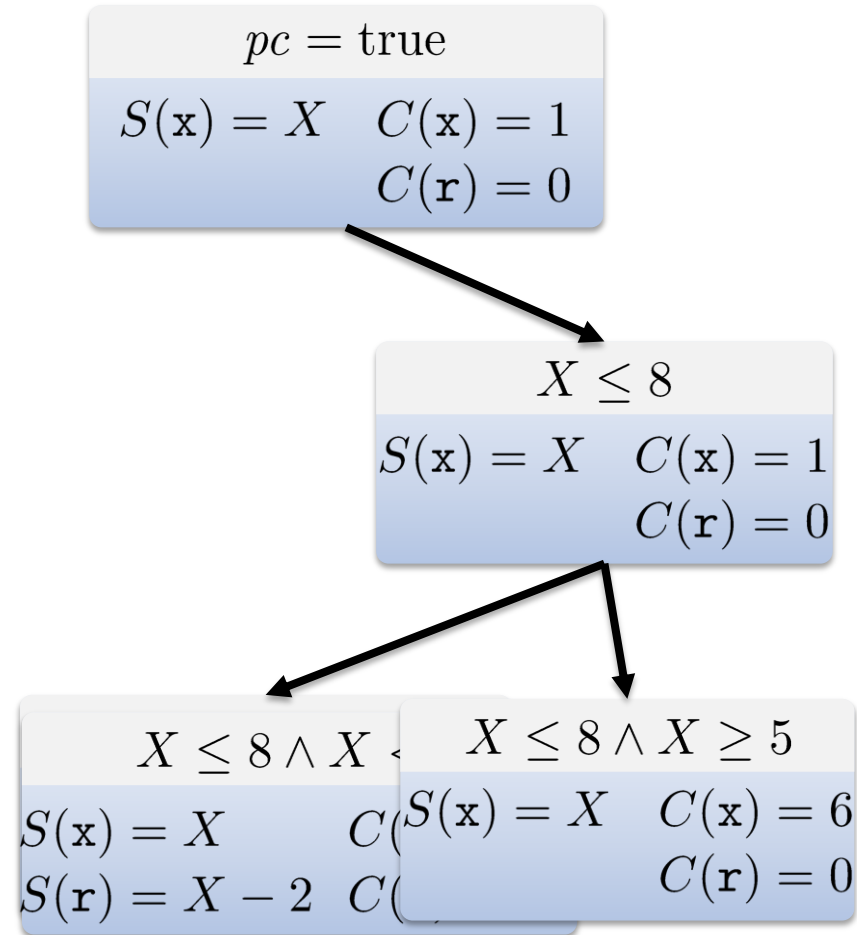
Path condition:

$$\neg(X \leq 8)$$

Test cases:

proc(1)

proc(6)



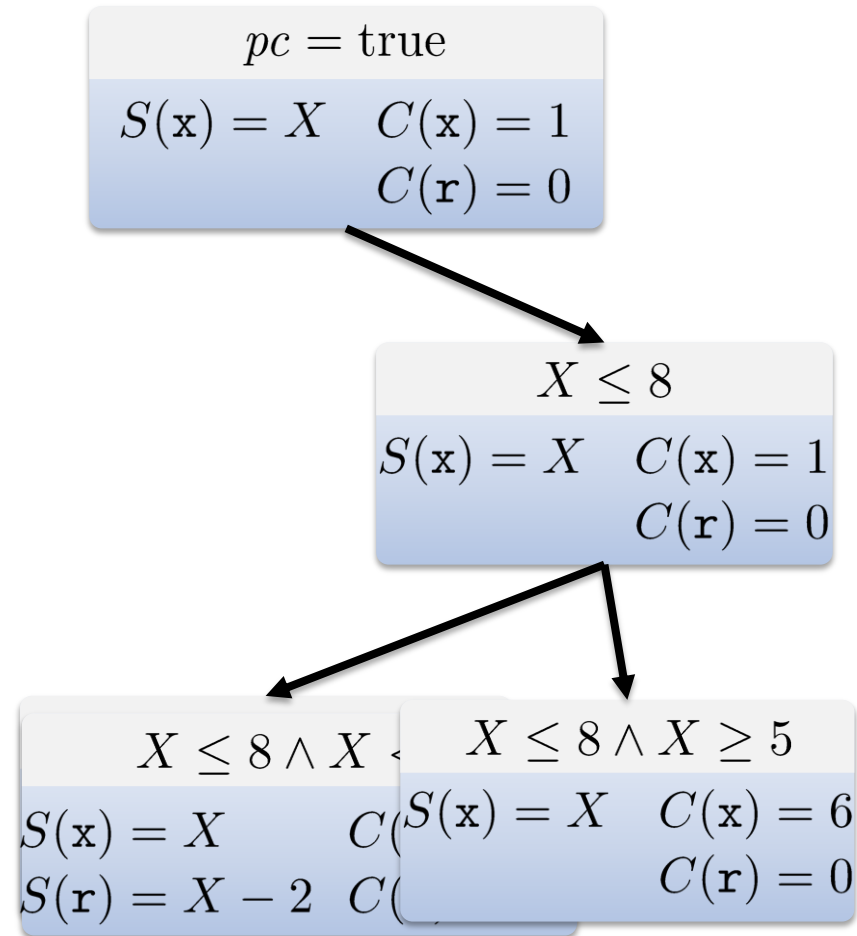


# DART

```
1 int proc(int x) {  
2  
3   int r = 0  
4  
5  
6   if (x > 8) {  
7     r = x - 7  
8   }  
9  
10  if (x < 5) {  
11    r = x - 2  
12  }  
13  
14  return r;  
15 }
```

Path condition:

Test cases:



$\neg(X \leq 8)$  ✓

proc(1)

proc(6)

# DART

```

1  int proc(int x) {
2
3  int r = 0
4
5
6  if (x > 8) {
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12 }
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14 return r;
15 }

```

Path condition:

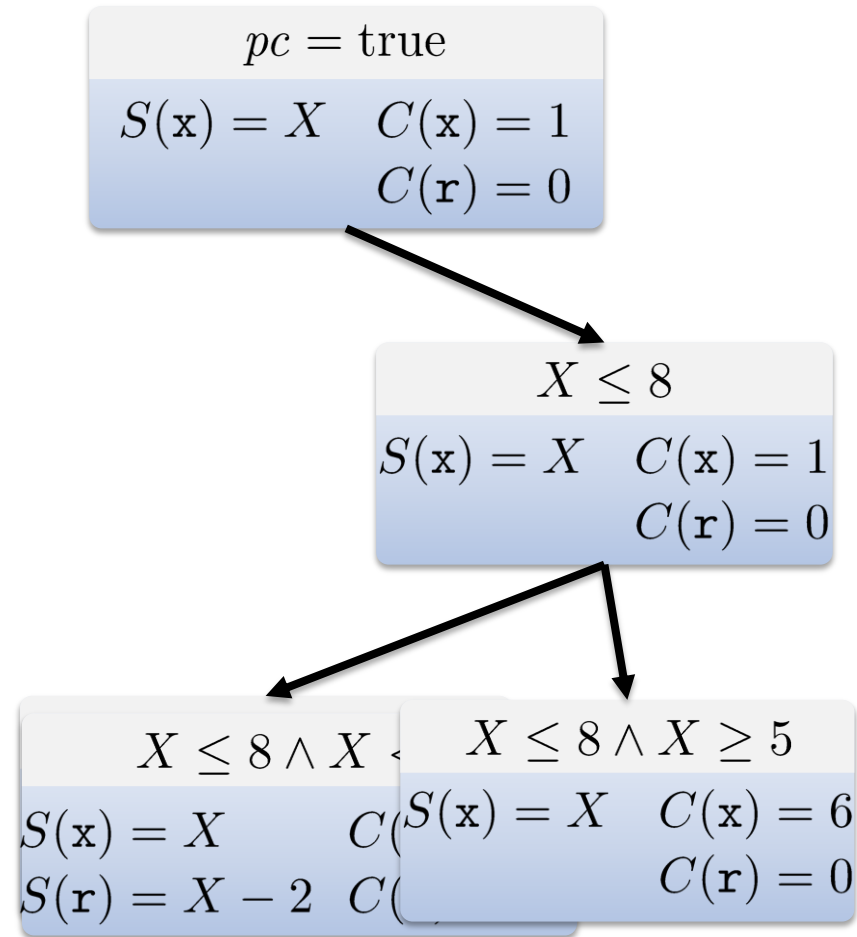
$$\neg(X \leq 8) \quad \checkmark$$

Test cases:

proc(9)

proc(1)

proc(6)

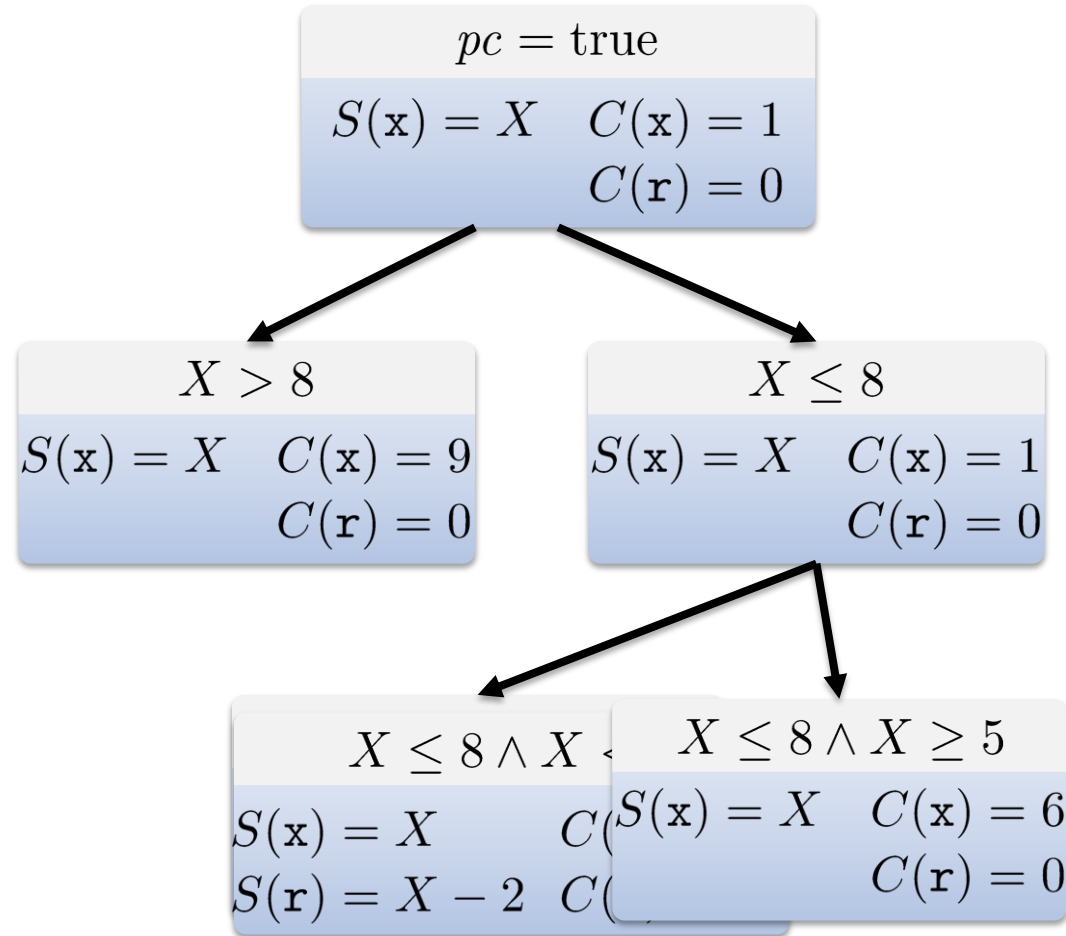


# DART

```

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2
3  int r = 0
4
5  if (x > 8) {
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10 if (x < 5) {
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14 return r;
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```



Path condition:

$$\neg(X \leq 8)$$

Test cases:

proc(9)

proc(1)

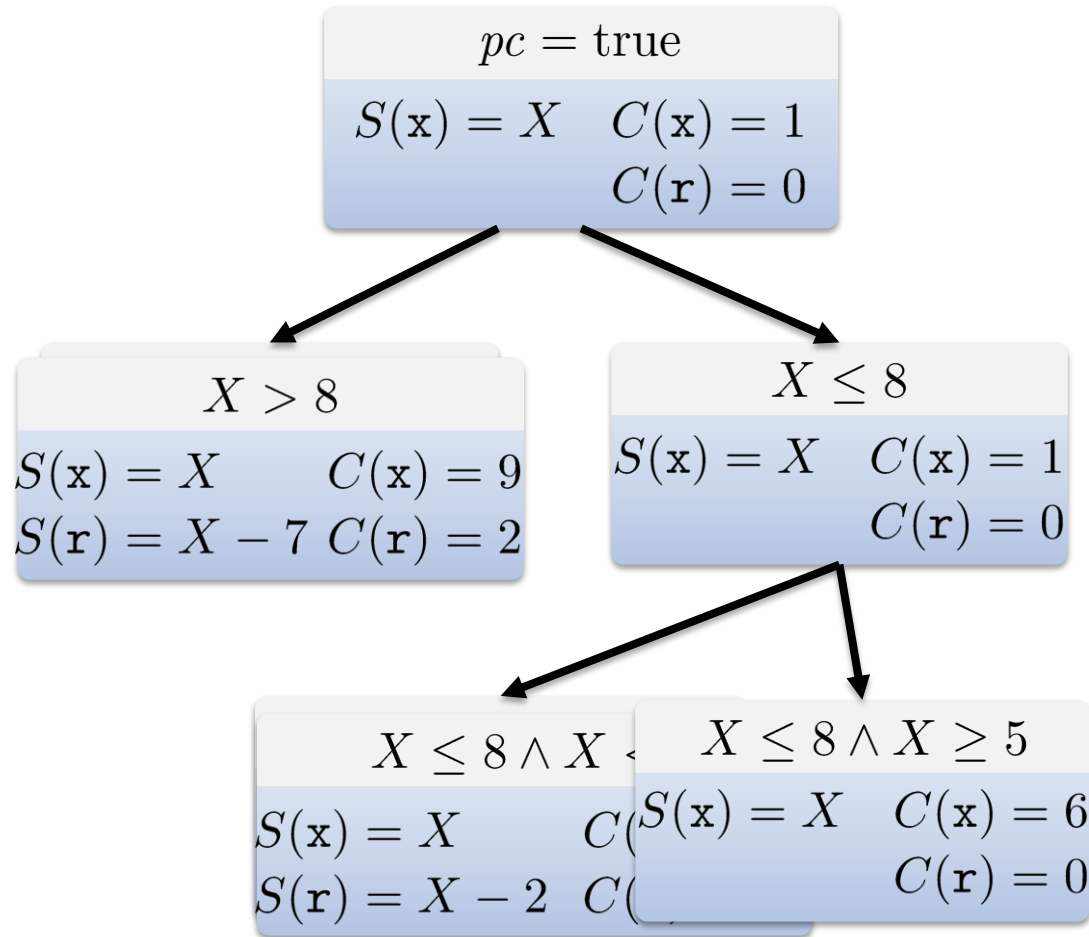
proc(6)

# DART

```

1  int proc(int x) {
2
3  int r = 0
4
5
6  if (x > 8) {
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8  }
9
10 if (x < 5) {
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13
14 return r;
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```



Path condition:

$$\neg(X \leq 8)$$

Test cases:

proc(9)

proc(1)

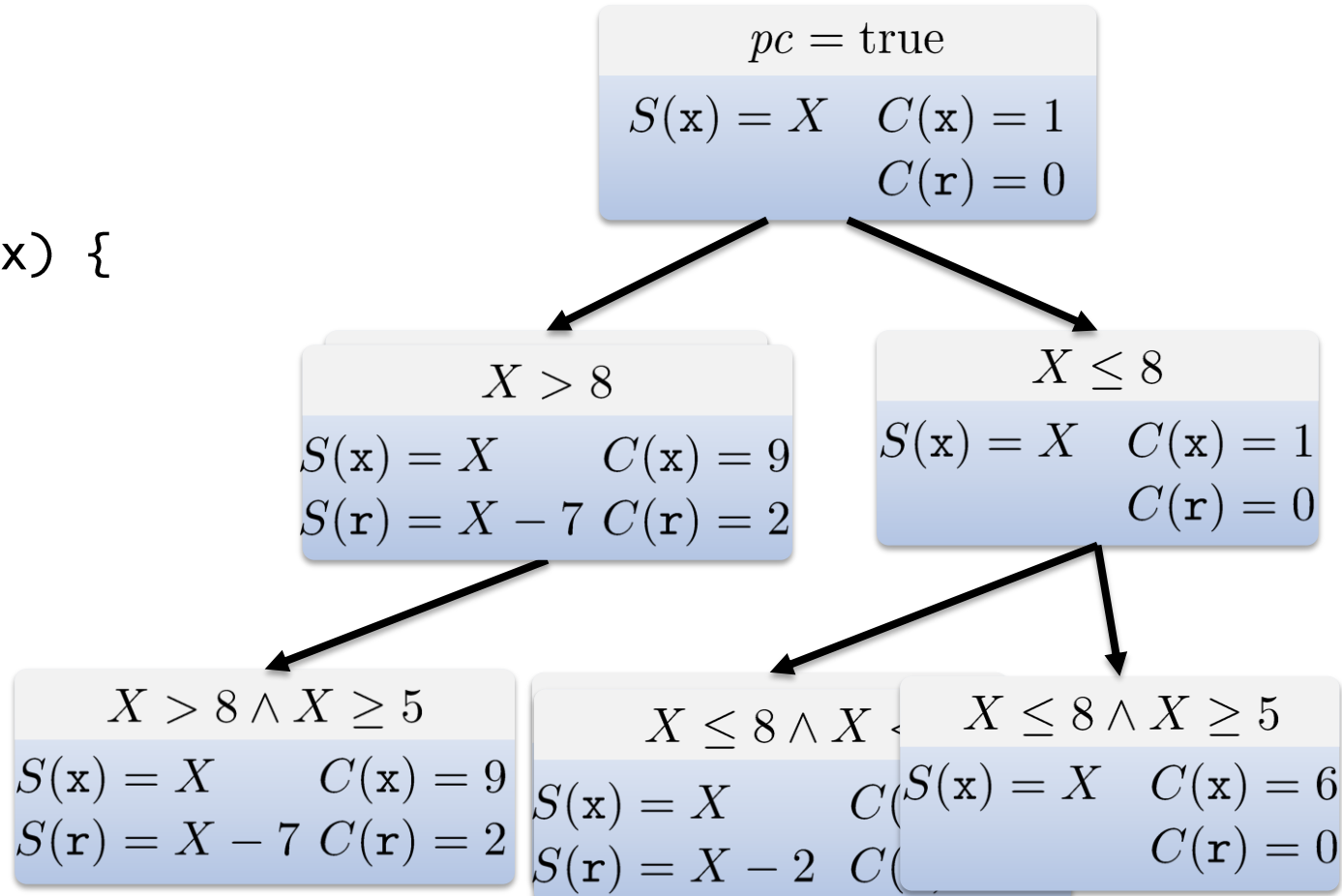
proc(6)

# DART

```

1  int proc(int x) {
2
3  int r = 0
4
5  if (x > 8) {
6      r = x - 7
7  }
8
9
10 if (x < 5) {
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```



Path condition:

$$\neg(X \leq 8)$$

Test cases:

proc(9)

proc(1)

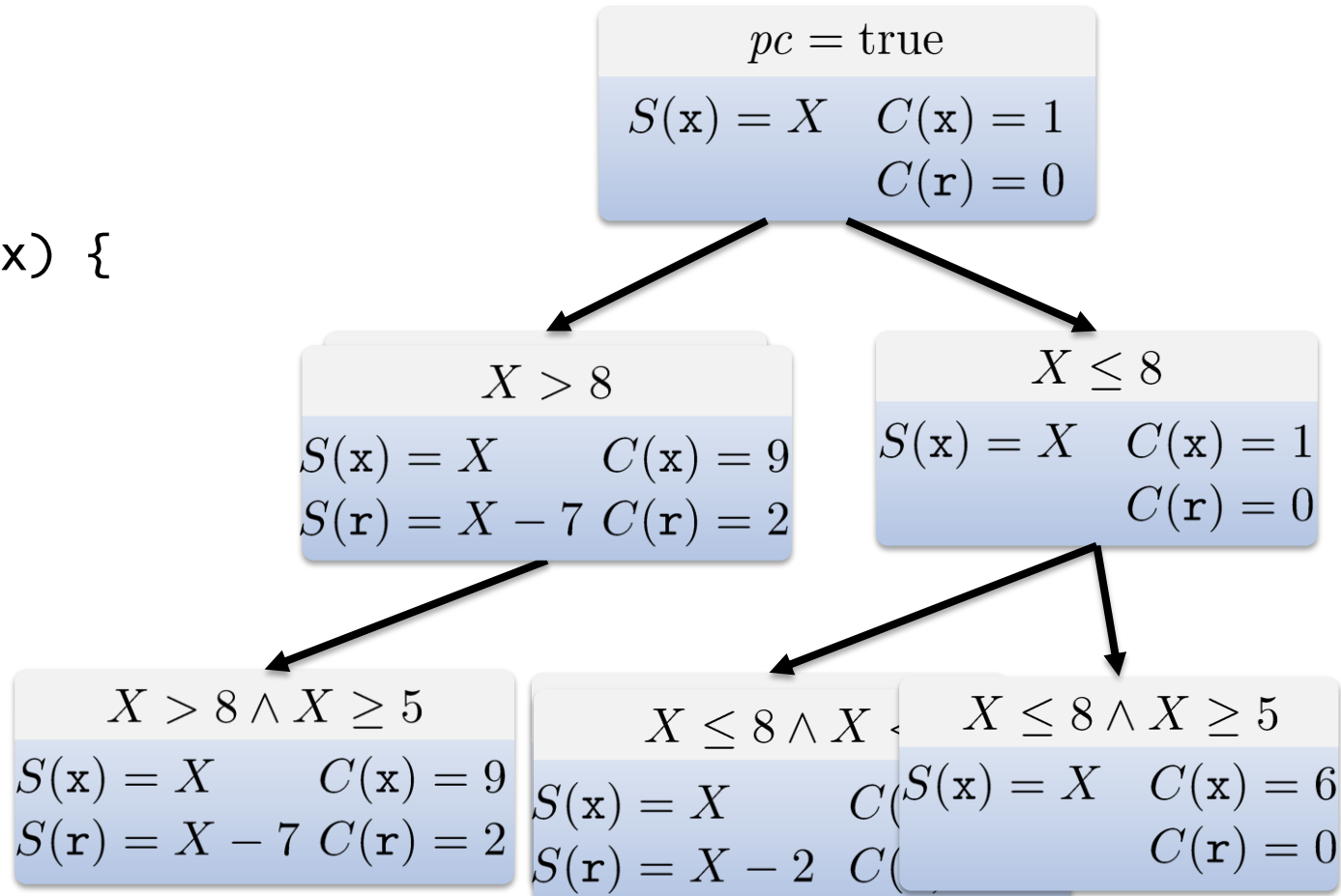
proc(6)

# DART

```

1  int proc(int x) {
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3  int r = 0
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12 }
13
14 return r;
15 }

```



Path condition:

$$X > 8 \wedge \neg(X \geq 5)$$

Test cases:

proc(9)

proc(1)

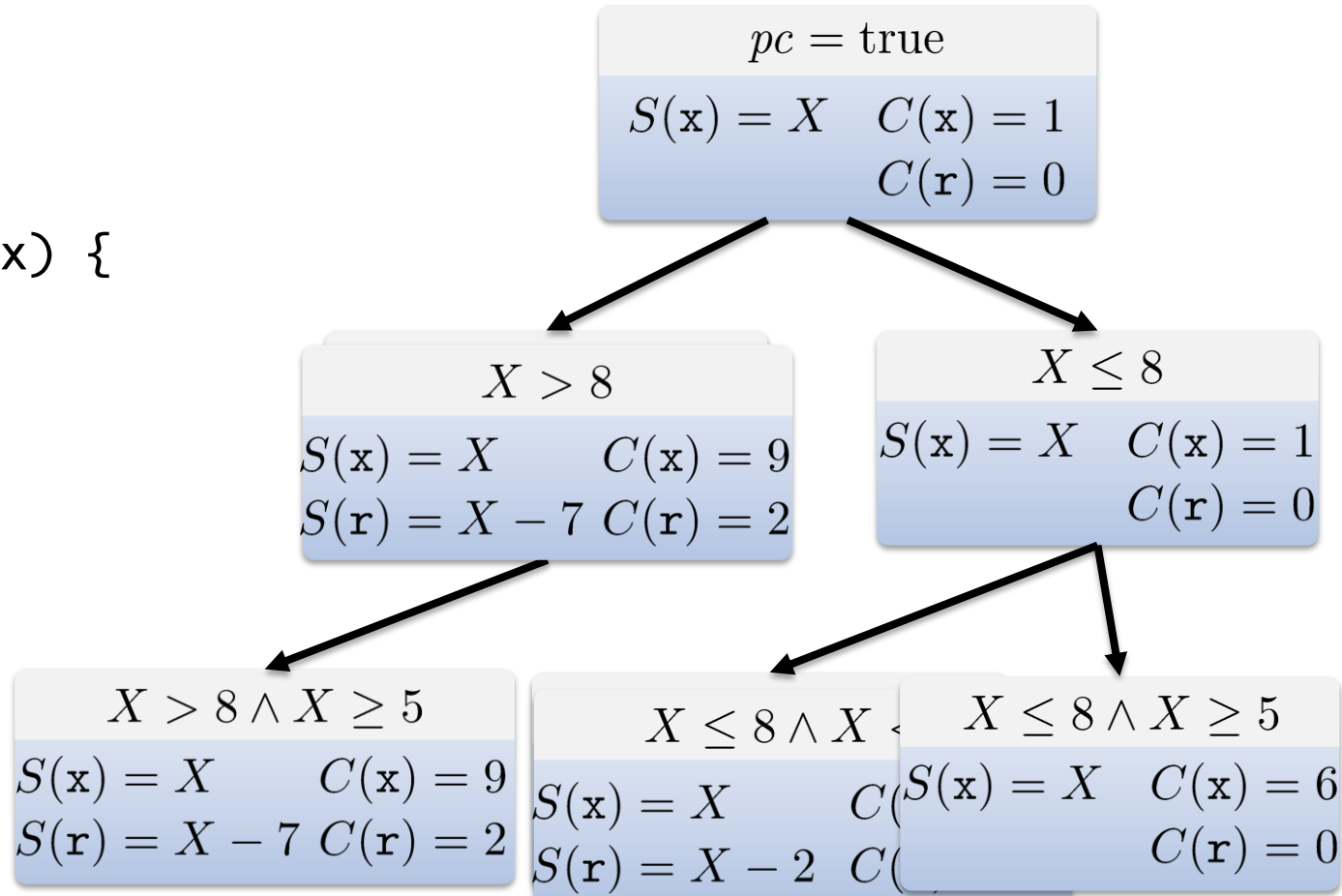
proc(6)

# DART

```

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14 return r;
15 }

```



Path condition:

$$X > 8 \wedge \neg(X \geq 5)$$

Test cases:

proc(9)

proc(1)

proc(6)

# DART vs. EXE

- Complete execution from 1<sup>st</sup> step
- Deep exploration
  - *One query per run*
- Offline SE possible
  - *Follow recorded trace*
- Fine-grained control of execution
- Shallow exploration
  - *Many queries early on*
- Online SE
  - *SE and interpretation in lockstep*



# Concretization

- Parts of input space can be kept concrete
  - *Reduces complexity*
  - *Focuses search*
- Expressions can be concretized at runtime
  - *Avoid expressions outside of SMT solver theories (non-linear etc.)*
- Sound but incomplete

# Concretization (Example)

*true*

$$C(X) = 5$$

$$S(m) = X + 2 \quad C(m) = 7$$

$$S(\text{size}) = Y \quad C(\text{size}) = 256$$

```
if (m*m > size) {
```

```
...
```

# Concretization (Example)

*true*

$$C(X) = 5$$

$$S(m) = X + 2 \quad C(m) = 7$$

$$S(\text{size}) = Y \quad C(\text{size}) = 256$$

if ( $m * m > \text{size}$ ) {

...

$$(X + 2)(X + 2) > Y$$

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$$S(\text{size}) = Y \quad C(\text{size}) = 256$$

if ( $m*m > \text{size}$ ) {

...

$$(X + 2)(X + 2) > Y$$

$$(5 + 2)(5 + 2) > Y$$

# Concretization (Example)

*true*

$$C(X) = 5$$

$$S(m) = X + 2 \quad C(m) = 7$$

$$S(\text{size}) = Y \quad C(\text{size}) = 256$$

if ( $m*m > \text{size}$ ) {

...

$$(X + 2)(X + 2) > Y$$

$$49 > Y$$

# Concretization (Example)

*true*

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 256 \end{array}$$

$49 > Y$

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 48 \end{array}$$

if ( $m * m > \text{size}$ ) {

...

$$(X + 2)(X + 2) > Y$$

$$49 > Y$$

# Concretization (Example)

*true*

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 256 \end{array}$$

```
if (m*m > size) {  
  ...  
  if (m < 5) {  
    ...  
  }  
}
```

$49 > Y$

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 48 \end{array}$$

# Concretization (Example)

*true*

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 256 \end{array}$$

```
if (m*m > size) {
```

```
  ...  
  if (m < 5) {
```

```
    ...
```

$$X + 2 < 5$$

$49 > Y$

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 48 \end{array}$$



# Concretization (Example)

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$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 256 \end{array}$$

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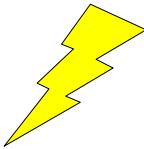
$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 48 \end{array}$$

```
if (m*m > size) {
```

```
  ...  
  if (m < 5) {
```

```
    ...
```

$X + 2 < 5$



**Solution diverges from expected path! (e.g.,  $X = 2$ )**

# Concretization (Example)

*true*

$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 256 \end{array}$$

```
if (m*m > size) {  
  ...  
  if (m < 5) {  
    ...  
  }  
}
```

## Concretization constraint

$$49 > Y \wedge X = 5$$

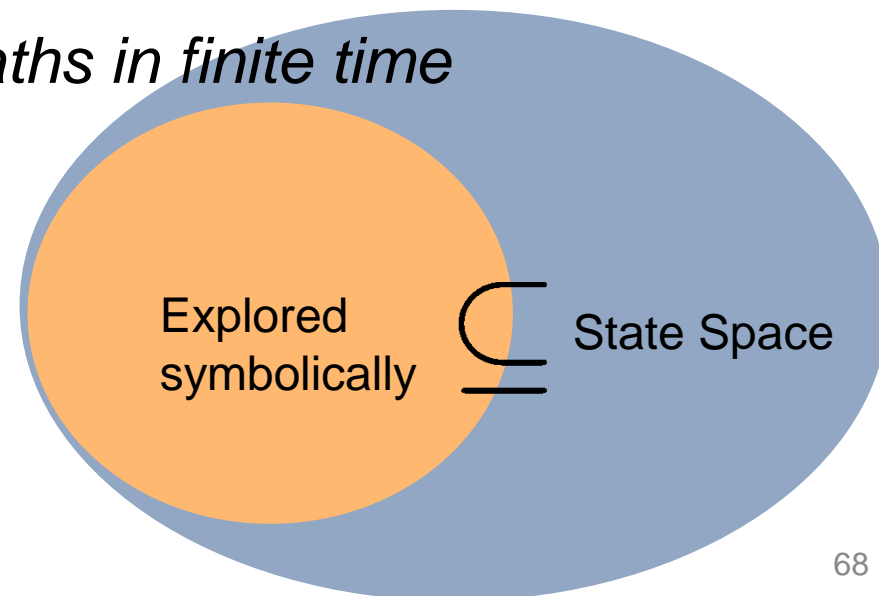
$$\begin{array}{ll} & C(X) = 5 \\ S(m) = X + 2 & C(m) = 7 \\ S(\text{size}) = Y & C(\text{size}) = 48 \end{array}$$

# Soundness & Completeness

- Conceptually, each path is exact
  - *Strongest postcondition in predicate transformer semantics*
  - *No over-approximation, no under-approximation*
- Globally, SE under-approximates
  - *Explores only subset of paths in finite time*
  - *“Eventual” completeness*

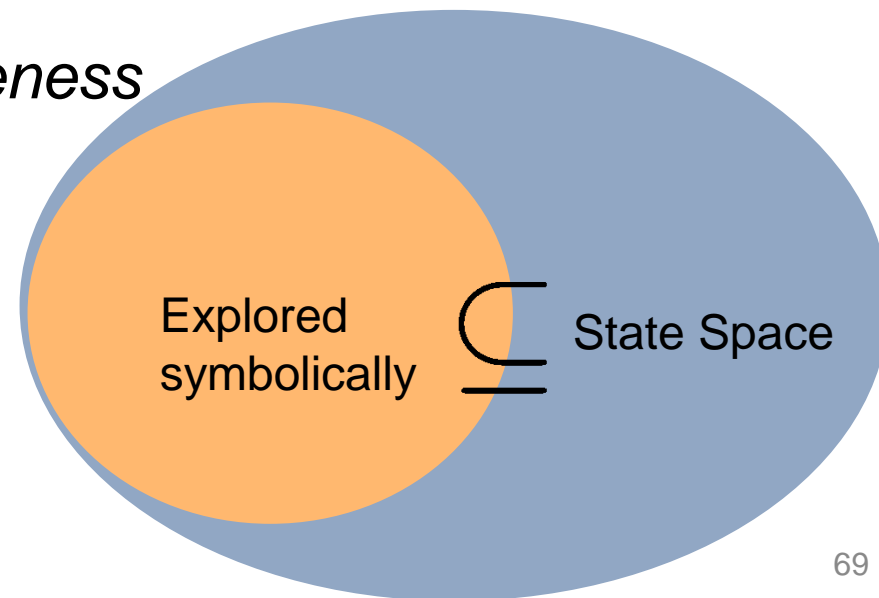
# Soundness & Completeness

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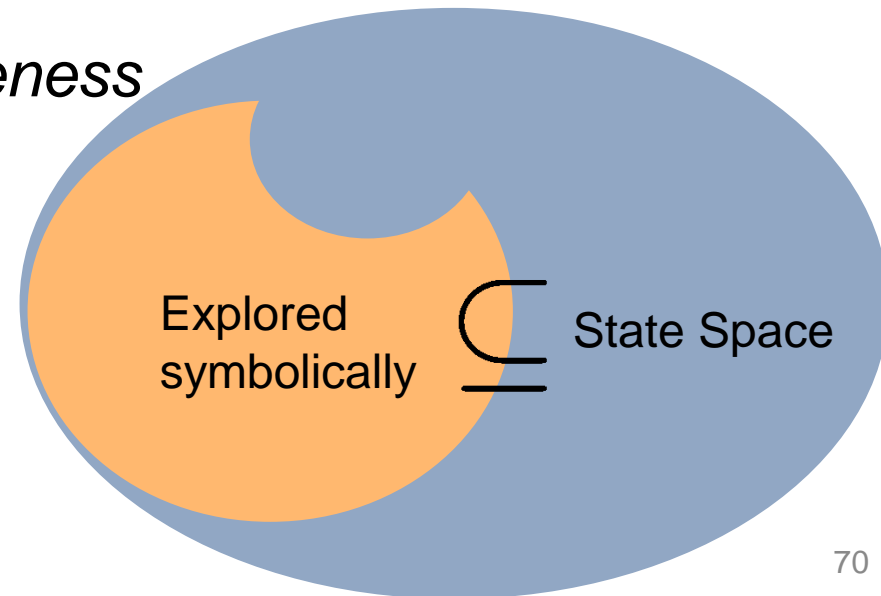
# Soundness & Completeness

- Symbolic Execution = Underapproximates
  - *Soundness = does not include infeasible behavior*
  - *Completeness = explores all behavior*
- Concretization restricts state covered by path
  - *Remains sound*
  - *Loses (eventual) completeness*



# Soundness & Completeness

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  - *Loses (eventual) completeness*



# Concretization

- Key strength of dynamic symbolic execution
- Enables external calls
  - *Concretize call arguments*
  - *Callee executes concretely*
- Concretization constraints can be omitted
  - *Sacrifices soundness (original DART)*
  - *Deal with divergences by random restarts*

# Outline

- Symbolic Execution for Testing
- State Merging – Fighting Path Explosion
- Interpreted High-Level Code



# “echo” Coreutil

```
void main(int argc, char **argv) {
    int r = 1, i = 1;

    if (i < argc) {
        if (argv[i][0] == 'n') {
            r = 0;
            ++i;
        }
    }

    for (; i < argc; ++i) {
        for (int j = 0; argv[i][j] != 0; ++j) {
            putchar(argv[i][j]);
        }
    }

    if (r) {
        putchar('\n');
    }
}
```

# “echo” Coreutil

```
void main(int argc, char **argv) {
    int r = 1, i = 1;

    if (i < argc) {
        if (argv[i][0] == 'n') {
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    }

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}
```

# Symbolic Execution

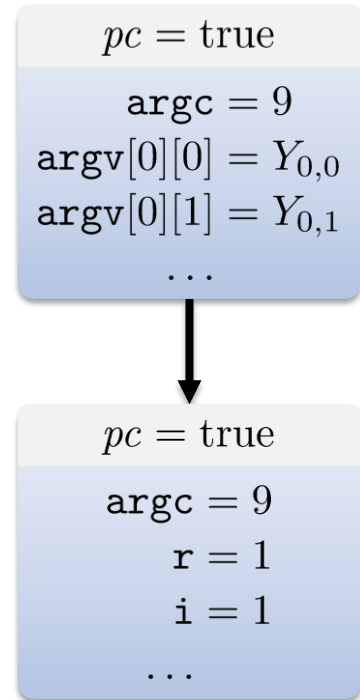
```
void main(int argc, char **argv) {  
    int r = 1, i = 1;  
  
    if (i < argc) {  
        if (argv[i][0] == 'n') {  
            r = 0;  
            ++i;  
        }  
    }  
  
    for (; i < argc; ++i) {  
        for (int j = 0; argv[i][j] != 0; ++j) {  
            putchar(argv[i][j]);  
        }  
    }  
  
    if (r) {  
        putchar('\n');  
    }  
}
```

*pc* = true

argc = 9  
argv[0][0] = Y<sub>0,0</sub>  
argv[0][1] = Y<sub>0,1</sub>  
...

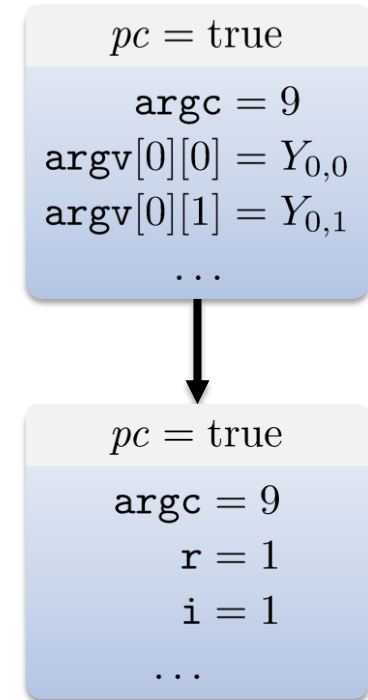
# Symbolic Execution

```
void main(int argc, char **argv) {  
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        }  
    }  
  
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    }  
}
```



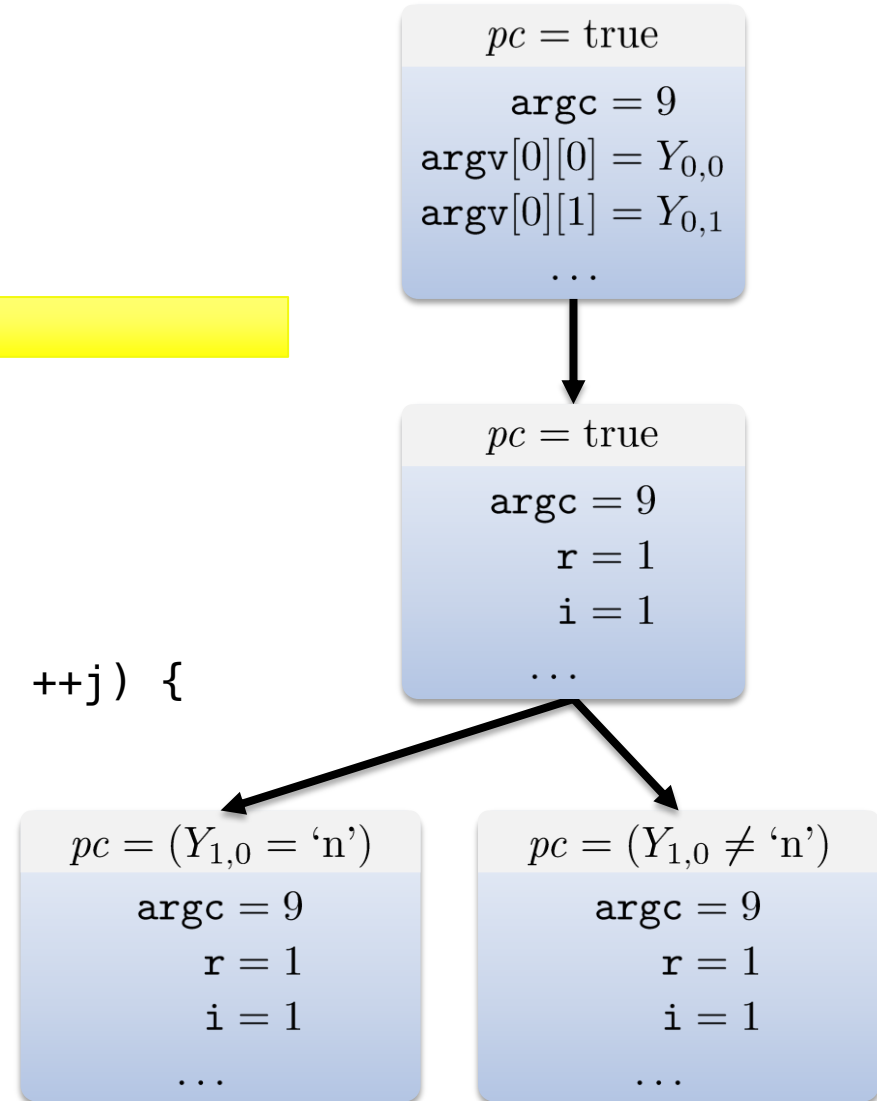
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        }  
    }  
  
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```



# Symbolic Execution

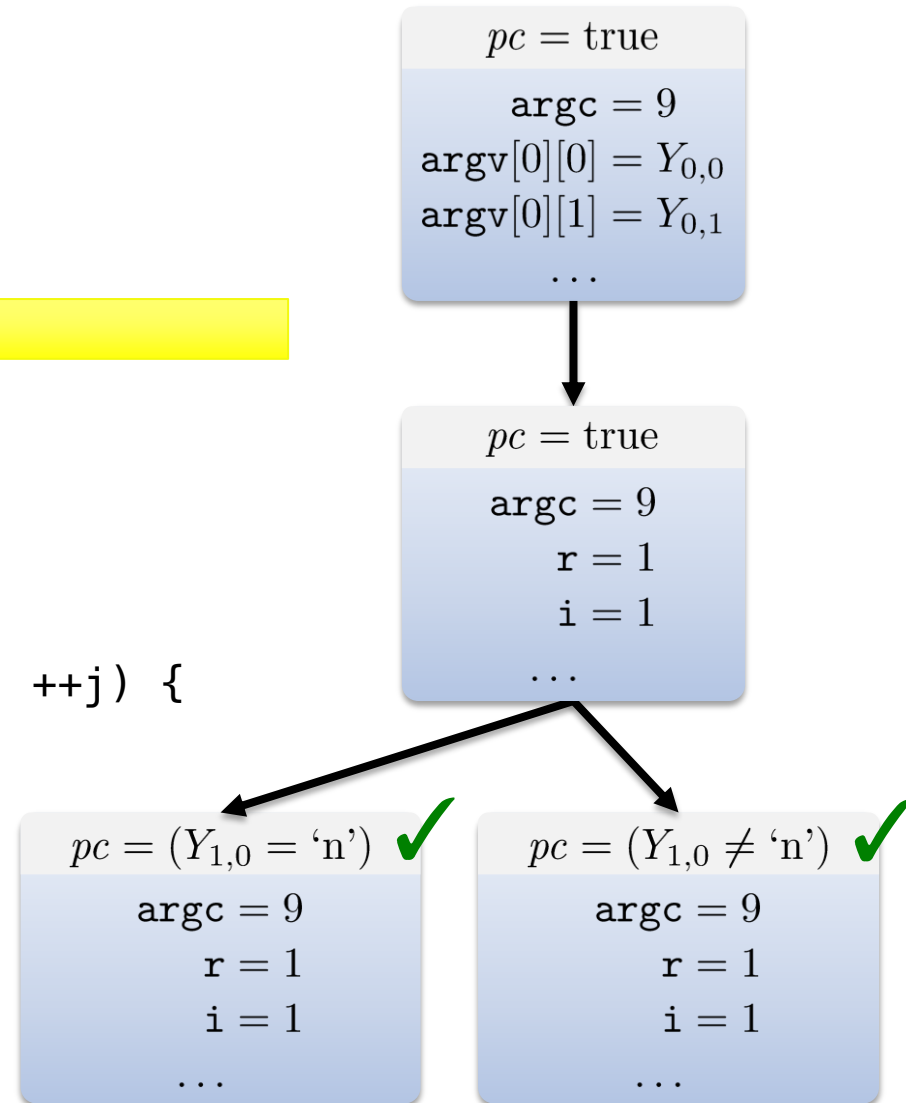
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    for (; i < argc; ++i) {  
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    }  
}
```





# Symbolic Execution

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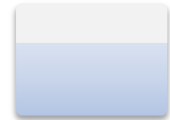
# Problem: Path Explosion

```
void main(int argc, char **argv) {
    int r = 1, i = 1;

    if (i < argc) {
        if (argv[i][0] == 'n') {
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```



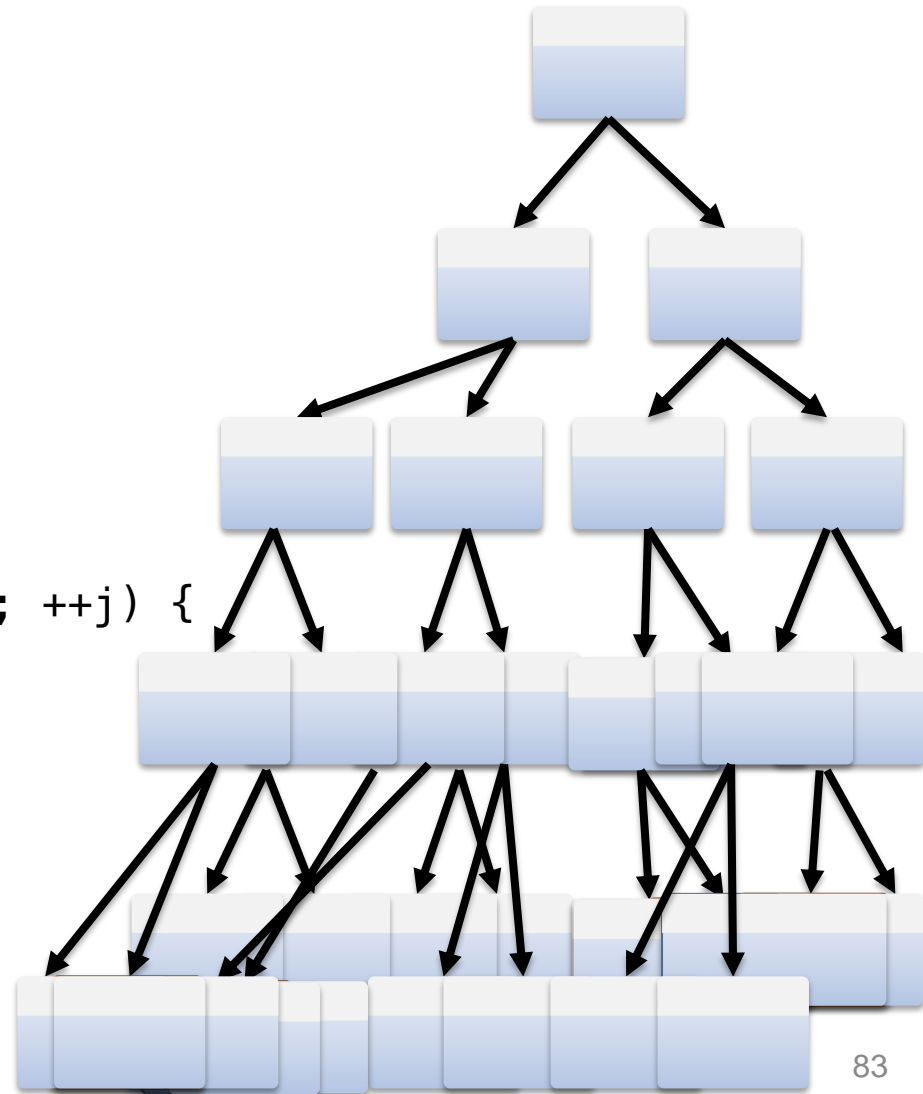
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            r = 0;
            ++i;
        }
    }

    for (; i < argc; ++i) {
        for (int j = 0; argv[i][j] != 0; ++j) {
            putchar(argv[i][j]);
        }
    }

    if (r) {
        putchar('\n');
    }
}
```



# Solution (?): State Merging

```
if (argv[i][0] == 'n') {  
    r = 0;  
    ++i;  
}
```

then

```
pc = ... ∧ (Y1,0 = 'n')  
    argc = 9  
        r = 0  
        i = 2  
        ...
```

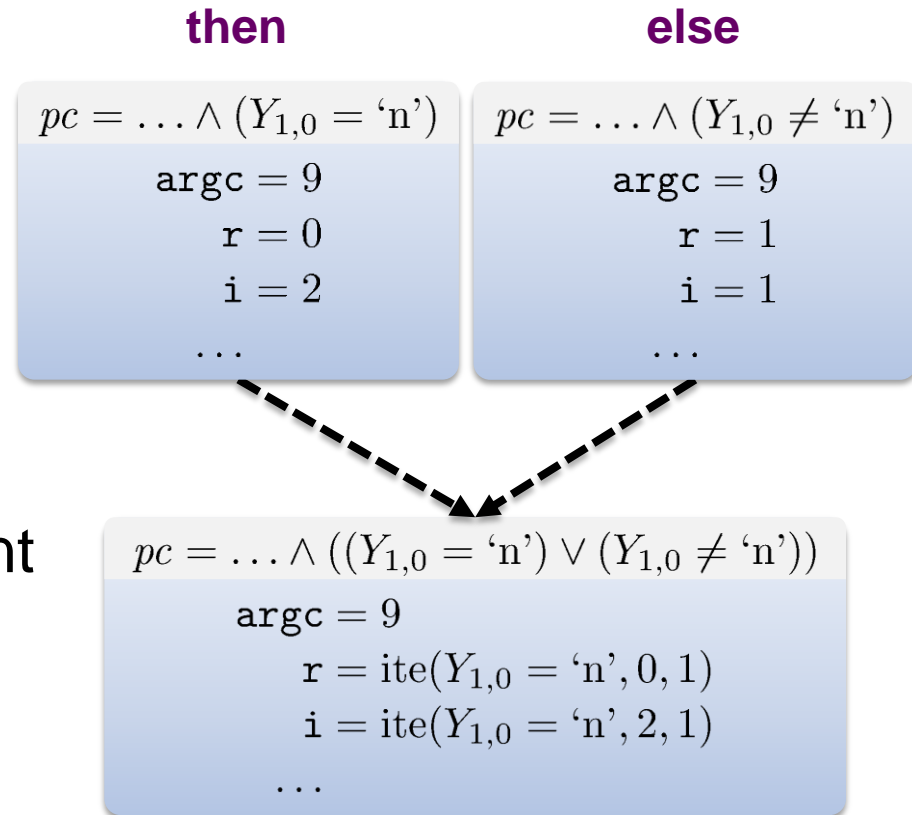
else

```
pc = ... ∧ (Y1,0 ≠ 'n')  
    argc = 9  
        r = 1  
        i = 1  
        ...
```

# Solution (?): State Merging

```
if (argv[i][0] == 'n') {  
    r = 0;  
    ++i;  
}
```

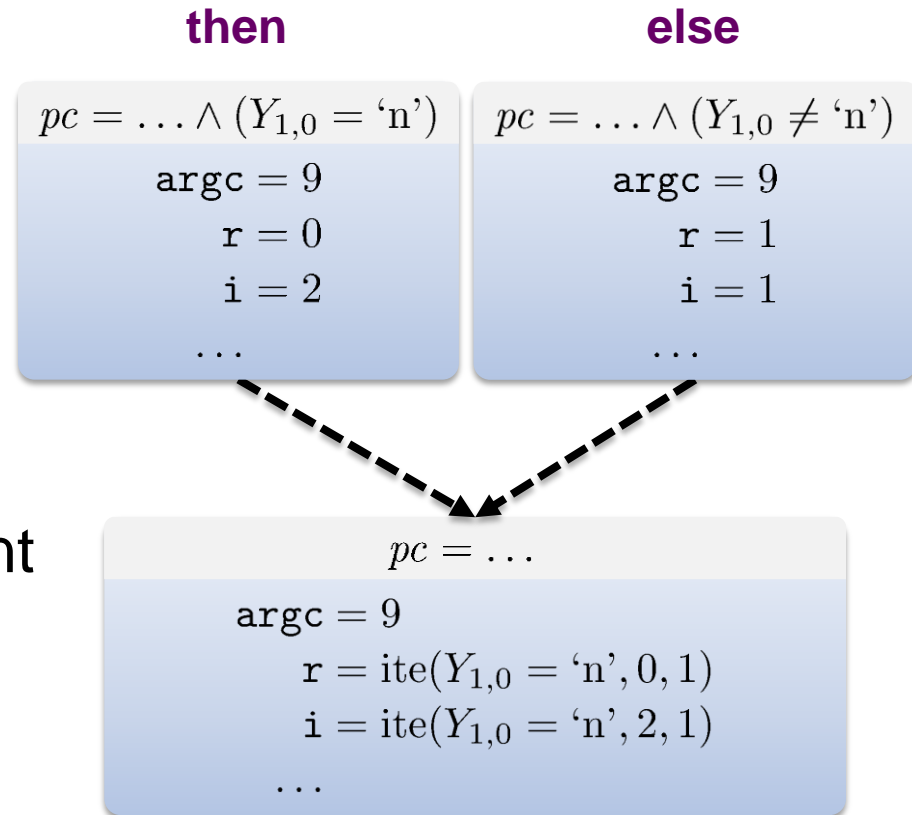
- Use disjunctions to represent state at join points
  - $\text{ite}(x, y, z)$  : if  $x$  then  $y$  else  $z$



# Solution (?): State Merging

```
if (argv[i][0] == 'n') {  
    r = 0;  
    ++i;  
}
```

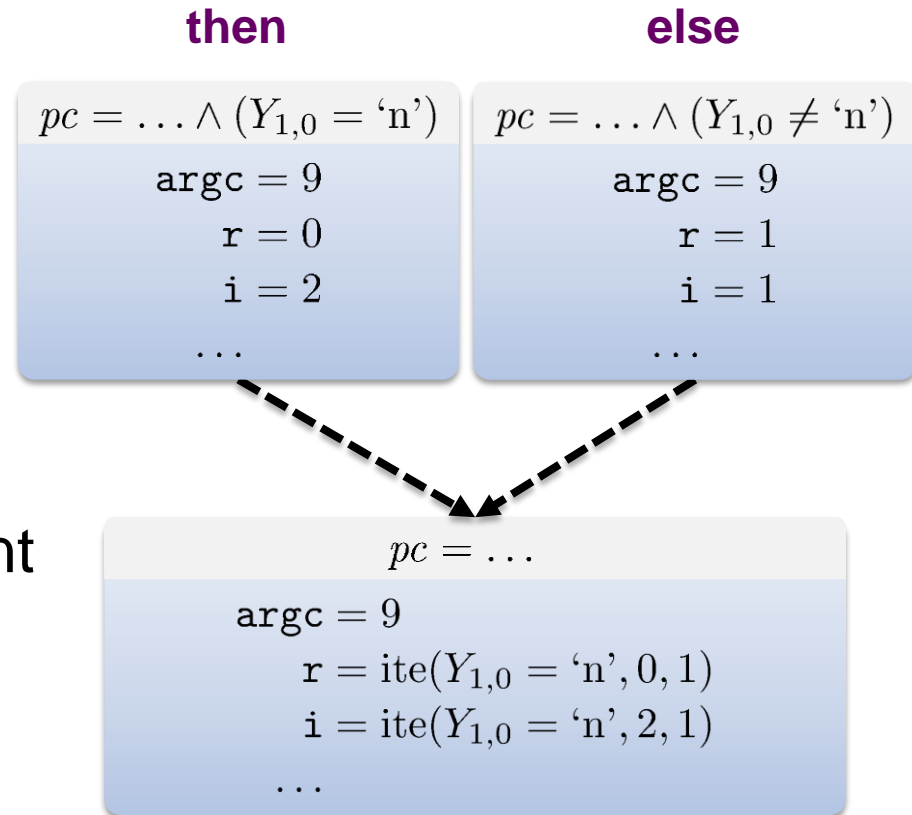
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# Solution (?): State Merging

```
if (argv[i][0] == 'n') {  
    r = 0;  
    ++i;  
}
```

- Use disjunctions to represent state at join points
  - $\text{ite}(x, y, z)$  : if  $x$  then  $y$  else  $z$
- SE tree becomes a DAG
  - *Whole program can be turned into one verification condition (BMC)*



# Symbolic Execution vs. BMC

- Complexity does not disappear
  - *Work moved from the SE engine to the solver*
  - *SE: set of conjunctive queries, BMC: 1 query with nested disjunctions*
- Complete merging sacrifices advantages of SE
  - *No dynamic mode*
  - *No continuous progress*
  - *No quick reaching of coverage goals*
- Try to get the best of both worlds



# Symbolic Execution

# Verification Condition Generation

**EXE (KLEE)**  
[Cadar et al., CCS'06]

**DART (SAGE)**  
[Godefroid, PLDI'05]

**F-Soft**  
[Ivancic et al., CAV'05]

**CBMC**  
[Clarke et al., TACAS'04]

1 formula / path

1 formula / CFG

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# Symbolic Execution

# Verification Condition Generation

Compositional SE /  
Summaries  
[Godefroid, POPL'07]

EXE (KLEE)  
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Compositional SE /  
Summaries  
[Godefroid, POPL'07]

BMC slicing  
[Ganai&Gupta, DAC'08]

Boogie  
[Barnett et al., FMCO'05]

F-Soft  
[Ivancic et al., CAV'05]

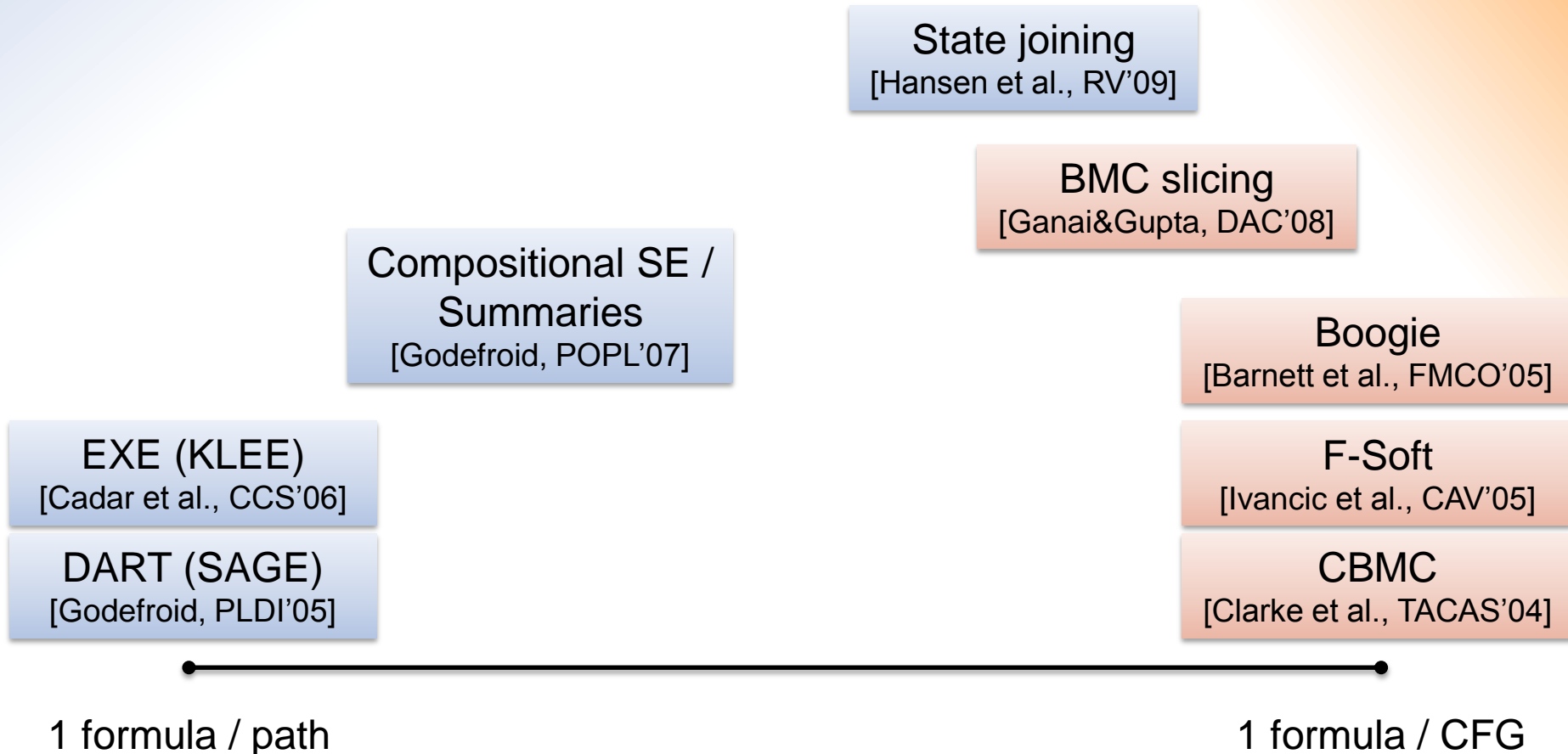
CBMC  
[Clarke et al., TACAS'04]

1 formula / path

1 formula / CFG

# Symbolic Execution

# Verification Condition Generation



Symbolic Execution

Verification Condition  
Generation

**Dynamic State Merging**

State joining  
[Hansen et al., RV'09]

BMC slicing  
[Ganai&Gupta, DAC'08]

Compositional SE /  
Summaries  
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EXE (KLEE)  
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Symbolic Execution

Verification Condition  
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**Query Count Estimation**

[KKBC PLDI'12]

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1 formula / path

1 formula / CFG

# Merging Increases Solving Cost

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void main(int argc, char **argv) {  
    int r = 1, i = 1;  
  
    if (i < argc) {  
        if (argv[i][0] == 'n') {  
            r = 0;  
            ++i;  
        }  
    }  
  
    for (; i < argc; ++i) {  
        for (int j = 0; argv[i][j] != 0; ++j) {  
            putchar(argv[i][j]);  
        }  
    }  
  
    if (r) {  
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```

*pc* = ...

argc = 9

i = ite( $Y_{1,0} = \text{'n'}$ , 2, 1)

...



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...  $\wedge$  ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  $\geq 9$   
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...  $\wedge$  ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  $< 9$   
argc = 9  
i = ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  
...

**Condition becomes symbolic, extra check required.**

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argc = 9  
i = ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  
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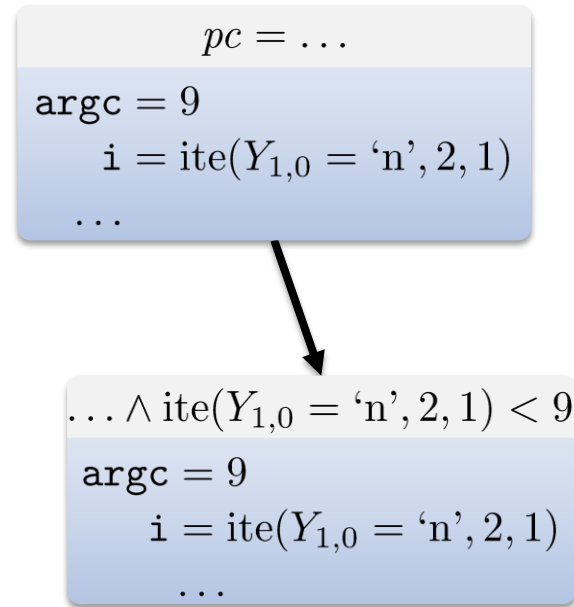
...  $\wedge$  ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  $\geq 9$  ✖  
argc = 9  
i = ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  
...

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**Condition becomes symbolic, extra check required.**

# Merging Increases Solving Cost

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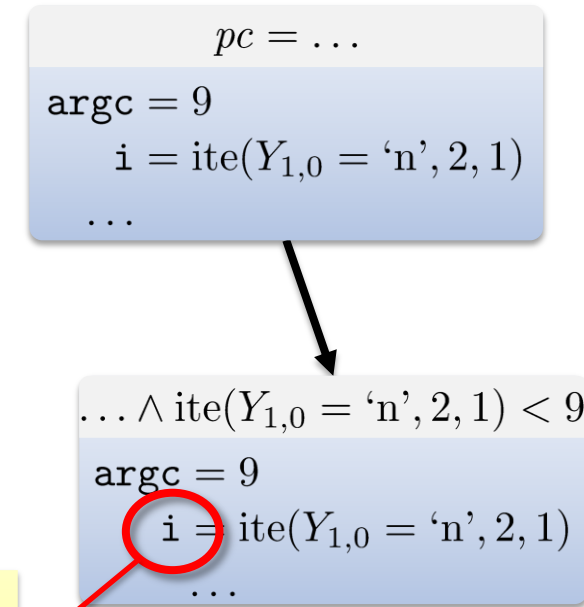
...  $\wedge$  ite( $Y_{1,0} = \text{'n'}, 2, 1$ ) < 9  
argc = 9  
i = ite( $Y_{1,0} = \text{'n'}, 2, 1$ )  
...

Query becomes more complex.

# Merging Increases Solving Cost

```
void main(int argc, char **argv) {  
    int r = 1, i = 1;  
  
    if (i < argc) {  
        if (argv[i][0] == 'n') {  
            r = 0;  
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        }  
    }  
  
    for (; i < argc; ++i) {  
        for (int j = 1; j < argc; ++j) {  
            putchar(argv[i][j]);  
        }  
    }  
  
    if (r) {  
        putchar('\n');  
    }  
}
```

Should not merge after  
checking 1<sup>st</sup> argument!



... becomes more complex.

# Query Count Estimation (QCE)

## *Intuition*

- Estimate the extra burden on the solver
- Merge only when merging amortizes extra cost

*Cost  $\approx$  number of solver queries*

# Applying QCE

1. Estimate query counts from each program location
  - *Total number of queries  $Q_t(\ell)$  on all paths*
  - *For each variable, number of dependent queries  $Q_{add}(\ell, v)$*



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2. Determine “hot” variables

$$H(\ell) = \{v \in V \mid Q_{add}(\ell, v) > \alpha \cdot Q_t(\ell)\}$$

# Applying QCE

Static

1. Estimate query counts from each program location
  - *Total number of queries  $Q_t(\ell)$  on all paths*
  - *For each variable, number of dependent queries  $Q_{add}(\ell, v)$*

2. Determine “hot” variables

$$H(\ell) = \{v \in V \mid Q_{add}(\ell, v) > \alpha \cdot Q_t(\ell)\}$$

3. Symbolic Execution

- *Do not merge two candidate states if they differ in hot variables*
- *Avoids creating ite expressions*

Dynamic

# Merging not Beneficial

```
void main(int argc, char **argv) {  
    int r = 1, i = 1;  
  
    if (i < argc) {  
        if (argv[i][0] == 'n') {  
            r = 0;  
            ++i;  
        }  
    }  
}
```

$pc = \dots \wedge (Y_{1,0} = \text{'n'})$

argc = 9

r = 0

i = 2

...

$pc = \dots \wedge (Y_{1,0} \neq \text{'n'})$

argc = 9

r = 1

i = 1

...

```
for (; i < argc; ++i) {  
    for (int j = 0; argv[i][j] != 0; ++j) {  
        putchar(argv[i][j]);  
    }  
}
```

$$H(\ell) = \{i\}$$

*i* is “hot”, leads to many extra queries

```
if (r) {  
    putchar('\n');  
}
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# Merging not Beneficial

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void main(int argc, char **argv) {  
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r = 1

i = 1

...

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for (; i < argc; ++i) {  
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$$H(\ell) = \{i\}$$

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$pc = \dots \wedge (Y_{1,0} = \text{'n'})$   
argc = 9  
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...

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...

$$H(\ell) = \{i\}$$

*i* is “hot”, leads to many extra queries

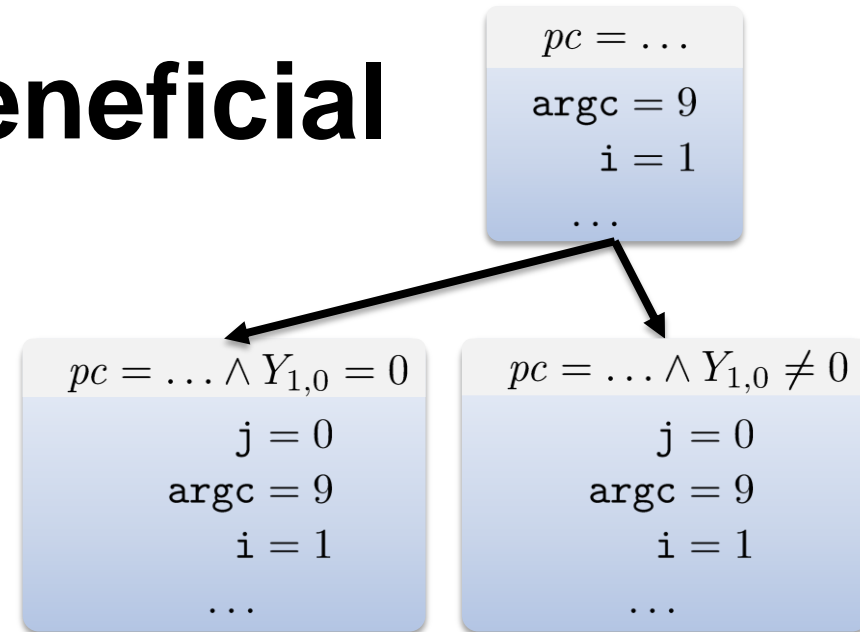
# Merging Beneficial

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  ...
```

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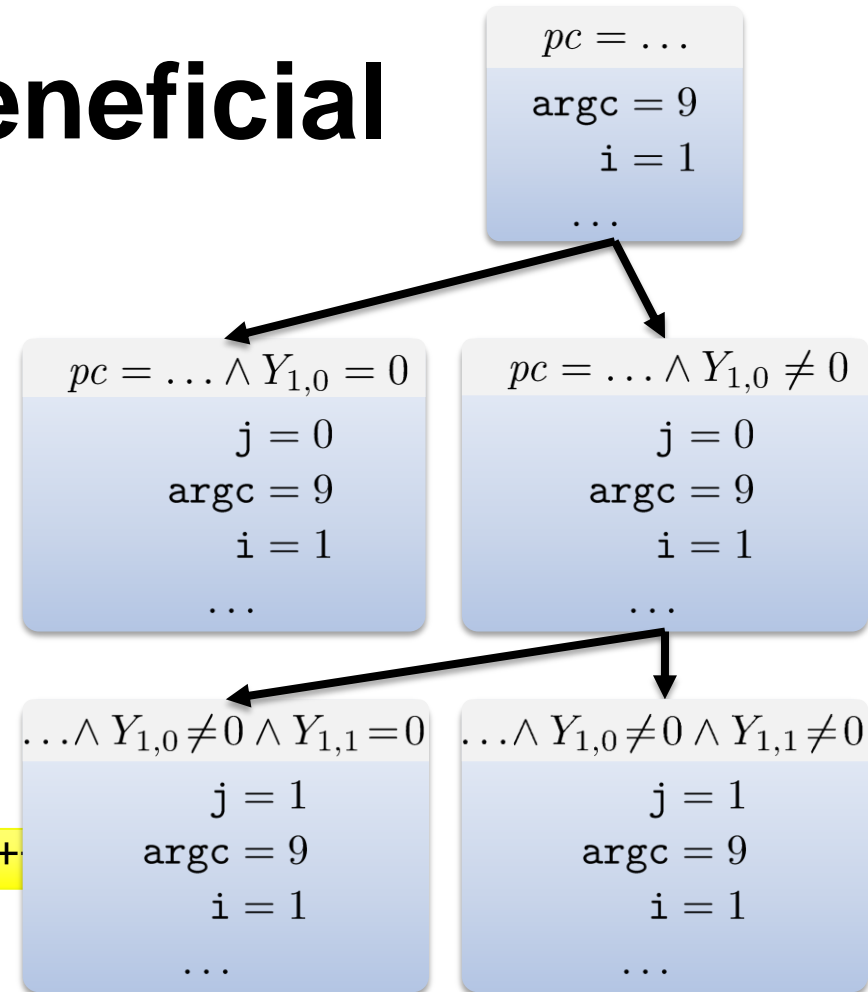
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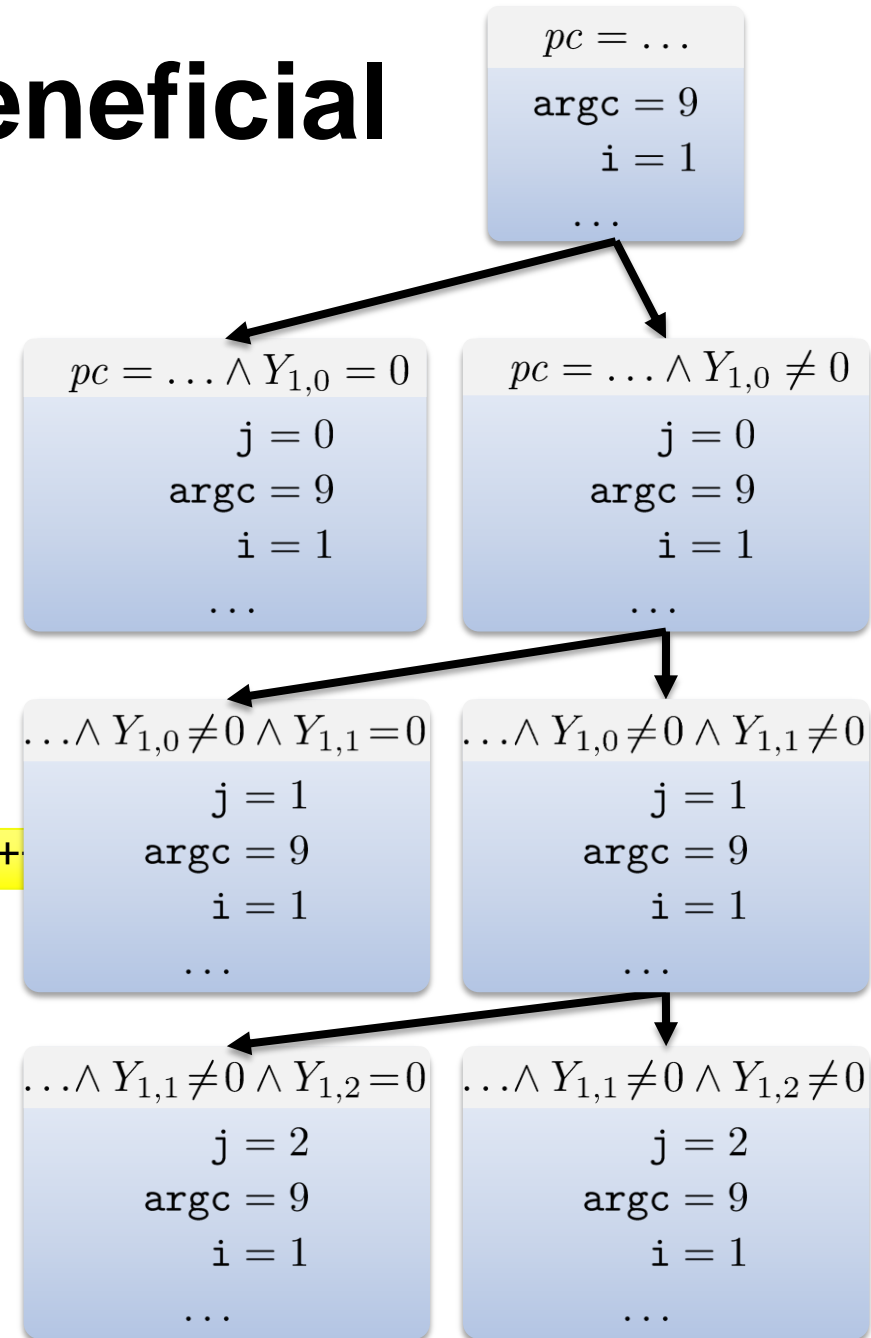
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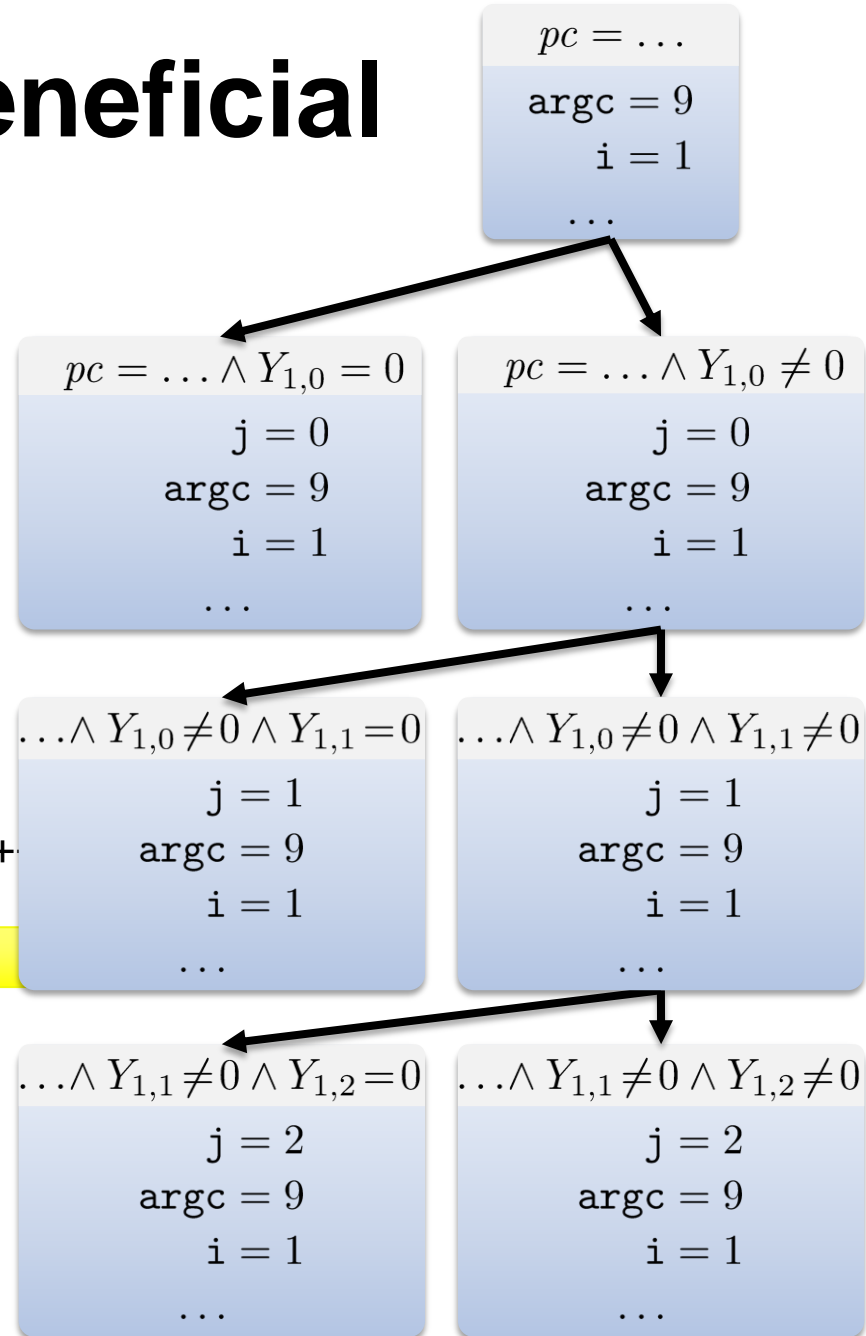
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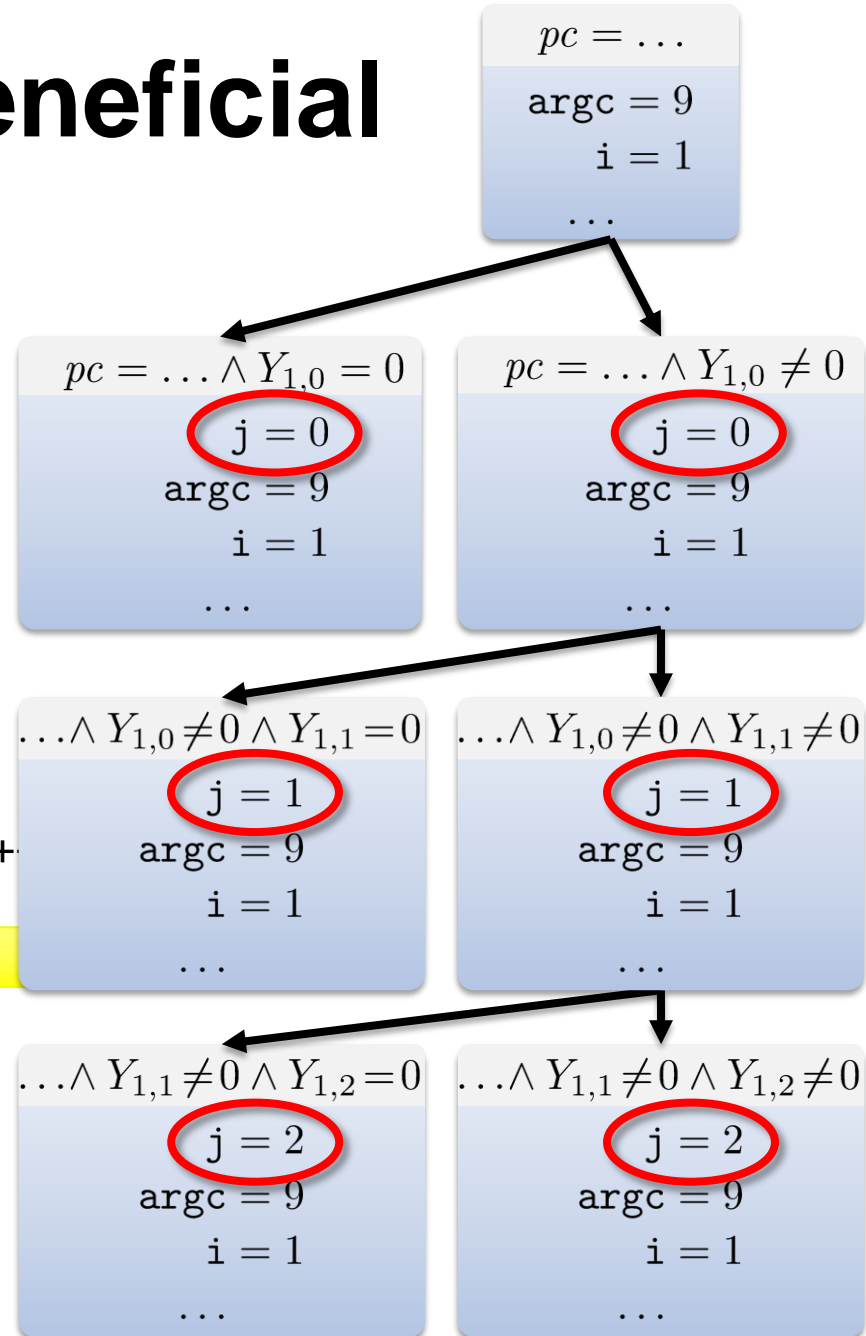
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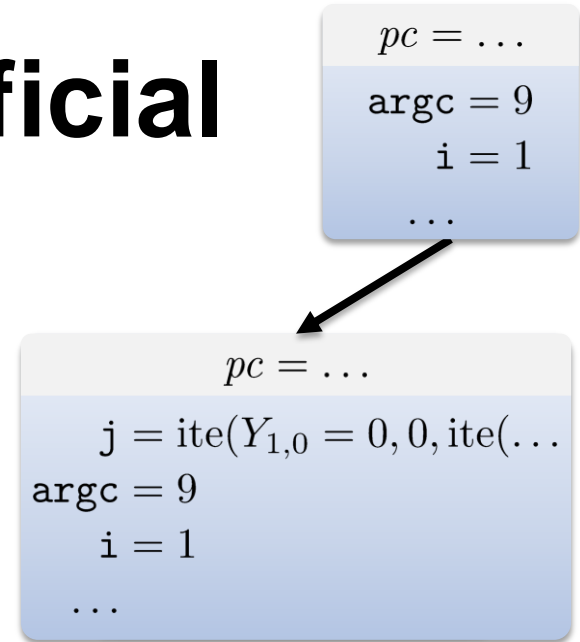
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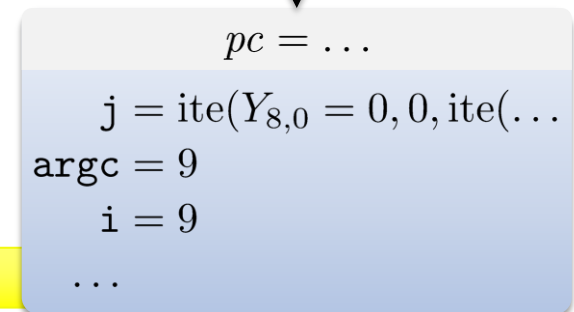
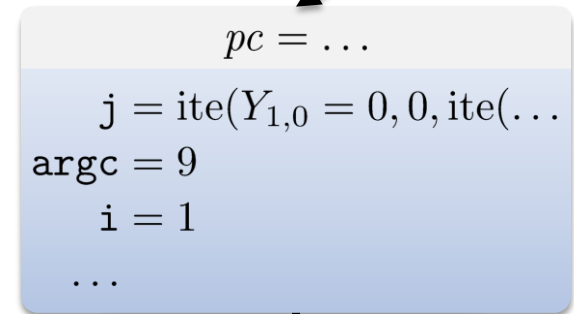
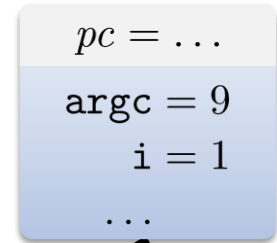
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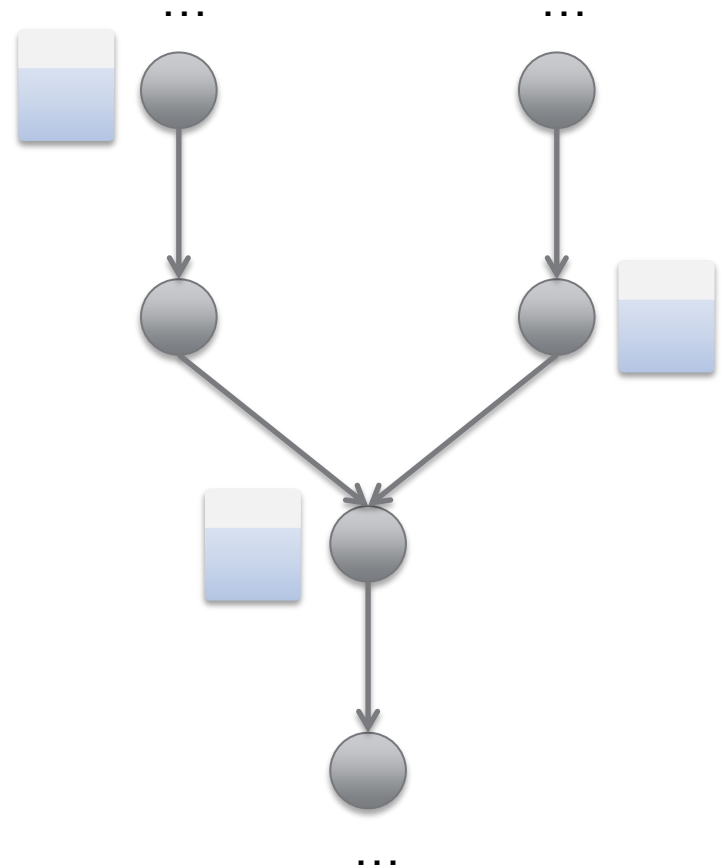
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```



**$L^{\text{argc}}$  states reduced to 1**  
(L: maximum argument length)

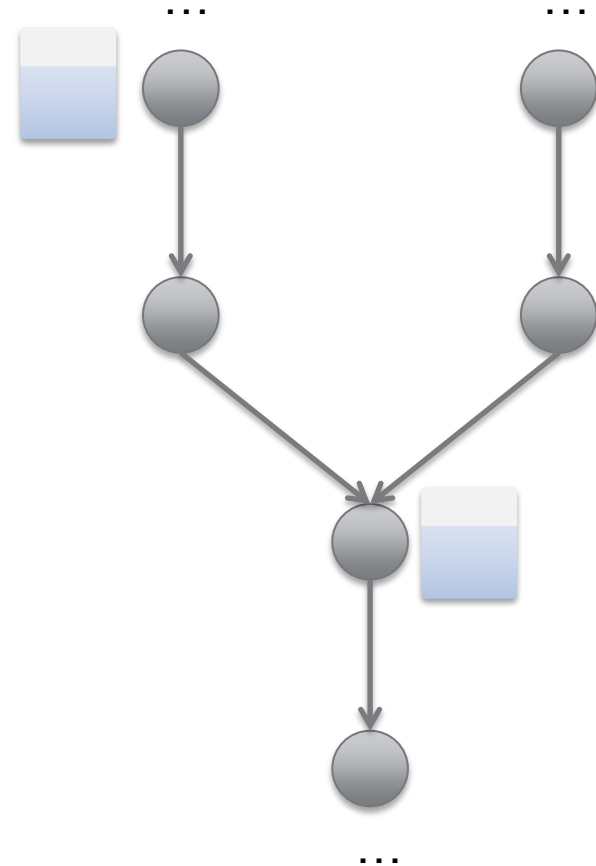
# Search Strategies

- SE usually incomplete
  - *100% path coverage is impractical*
- Uses *search strategy* to reach a coverage goal
- Search strategy chooses states from a worklist



# Search Strategies

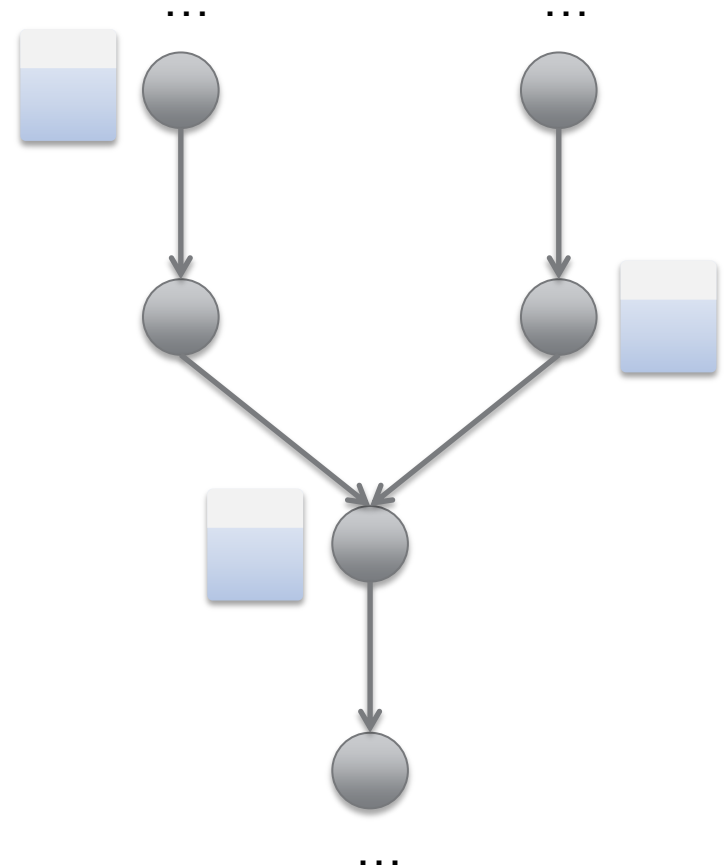
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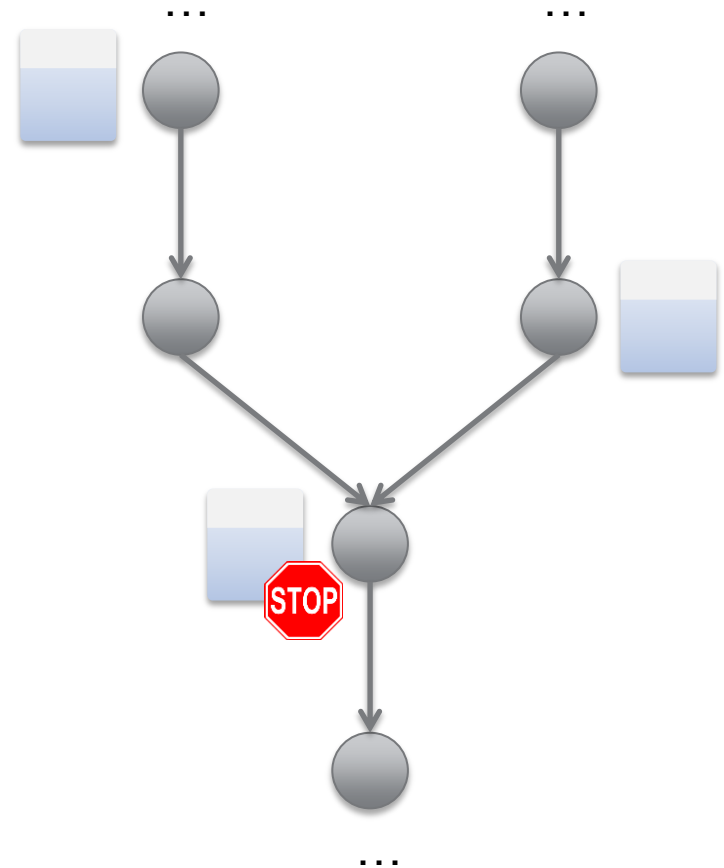
# Merging Breaks Search Strategies

- Naïve state merging blocks states at join points
- Allows earlier states to “catch up”
- Thwarts strategy in reaching its goal!



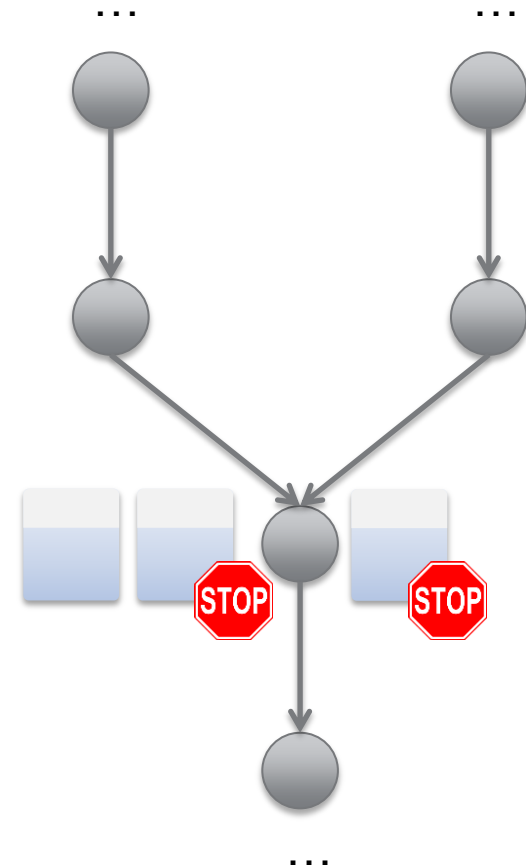
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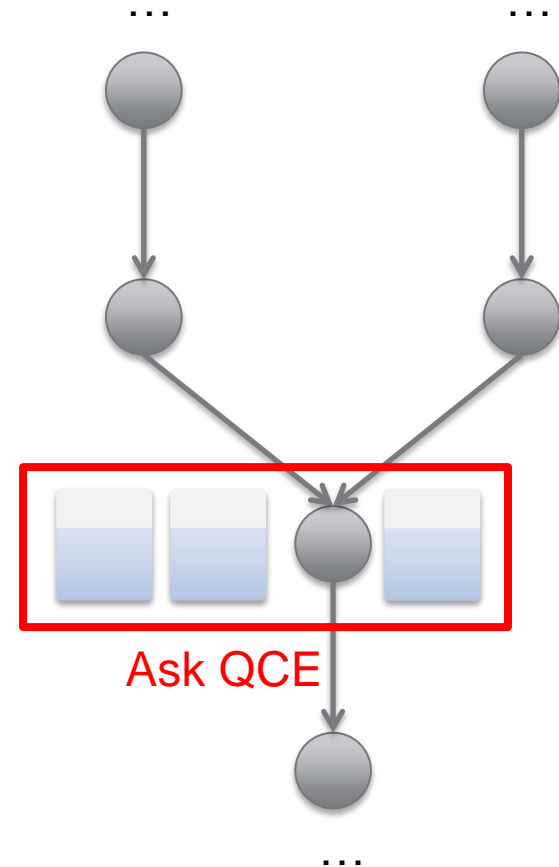
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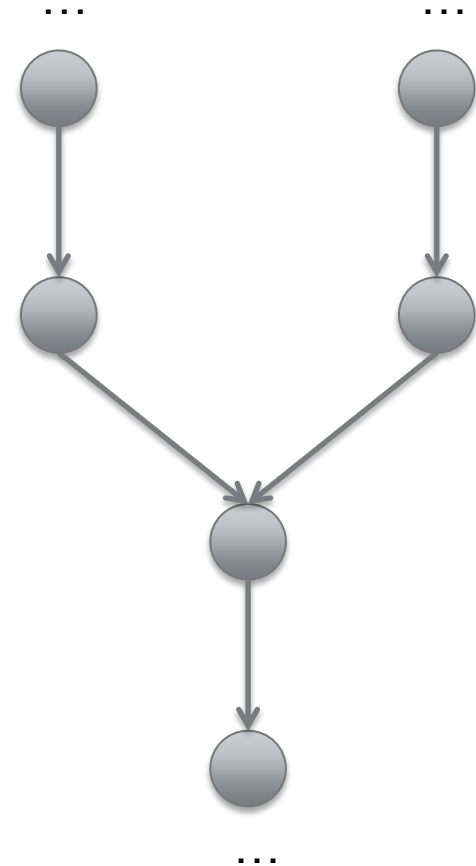
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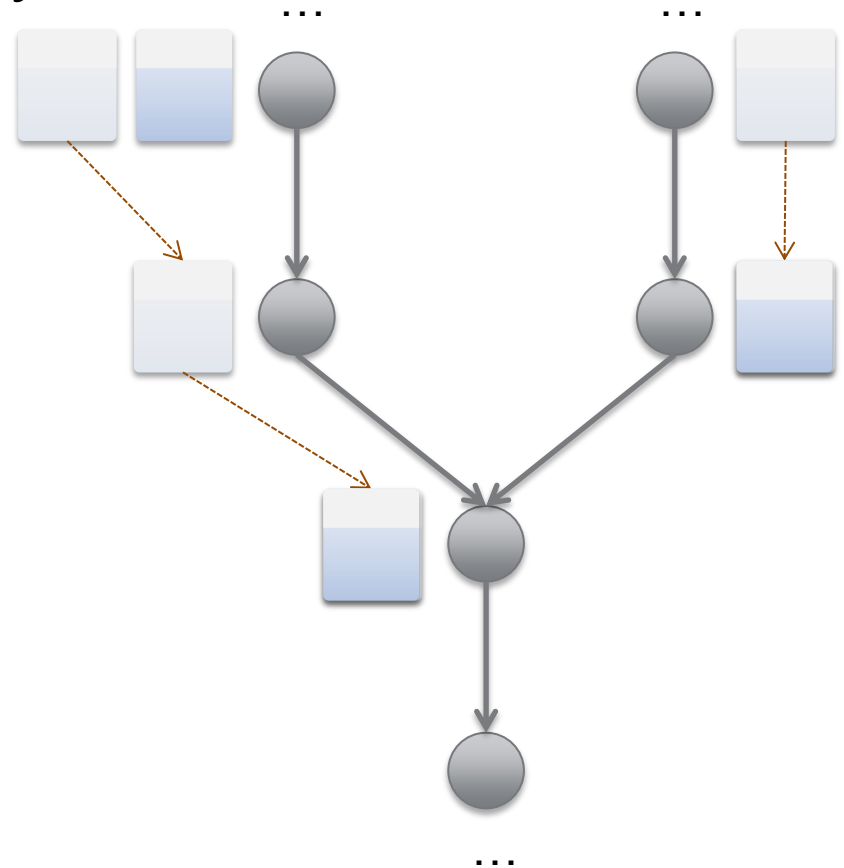
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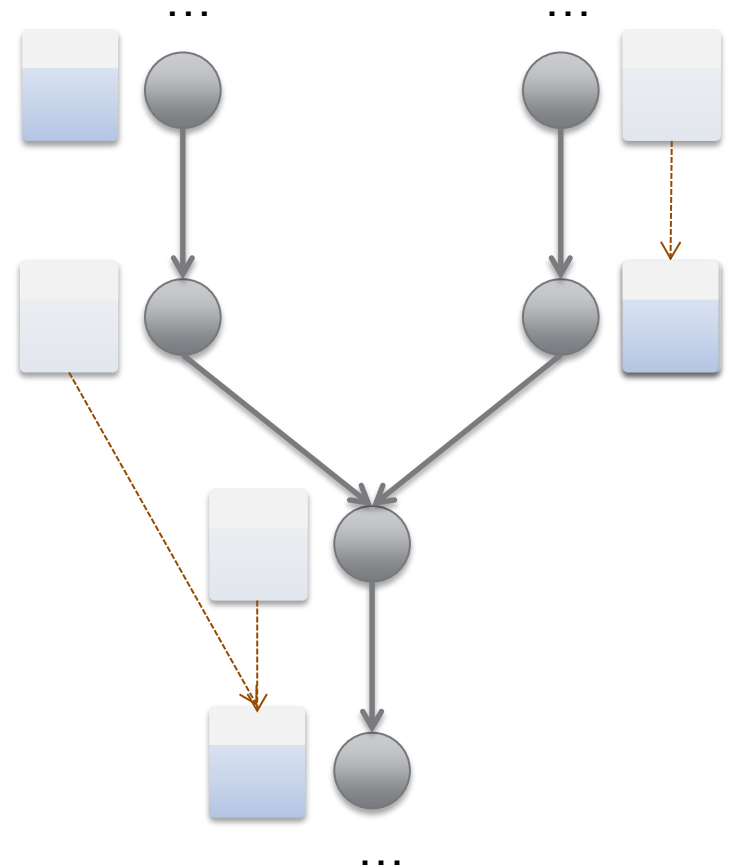
# Dynamic State Merging

- Maintain bounded history of predecessor states



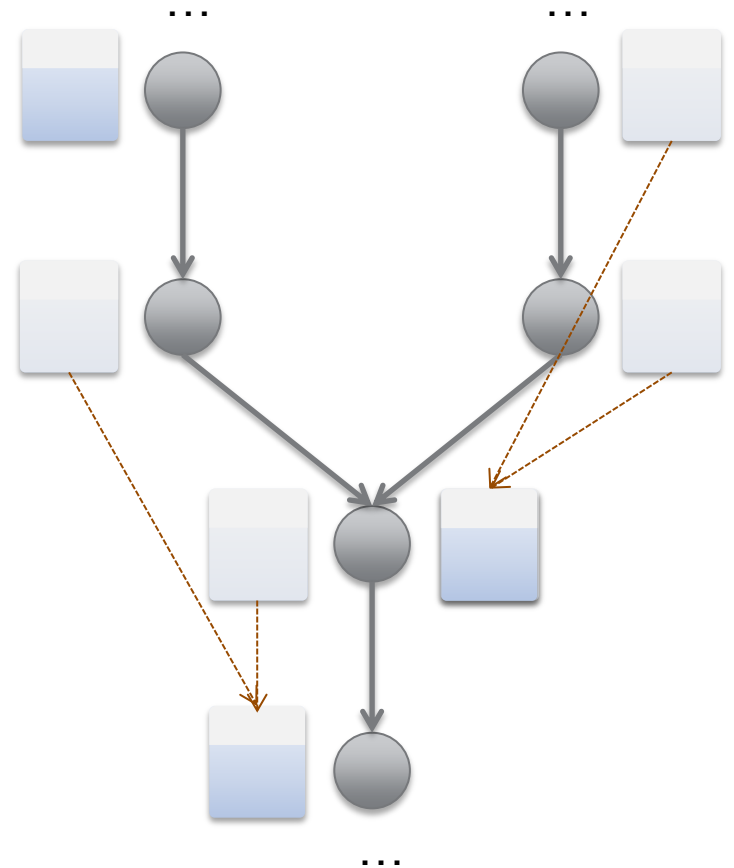
# Dynamic State Merging

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# Dynamic State Merging

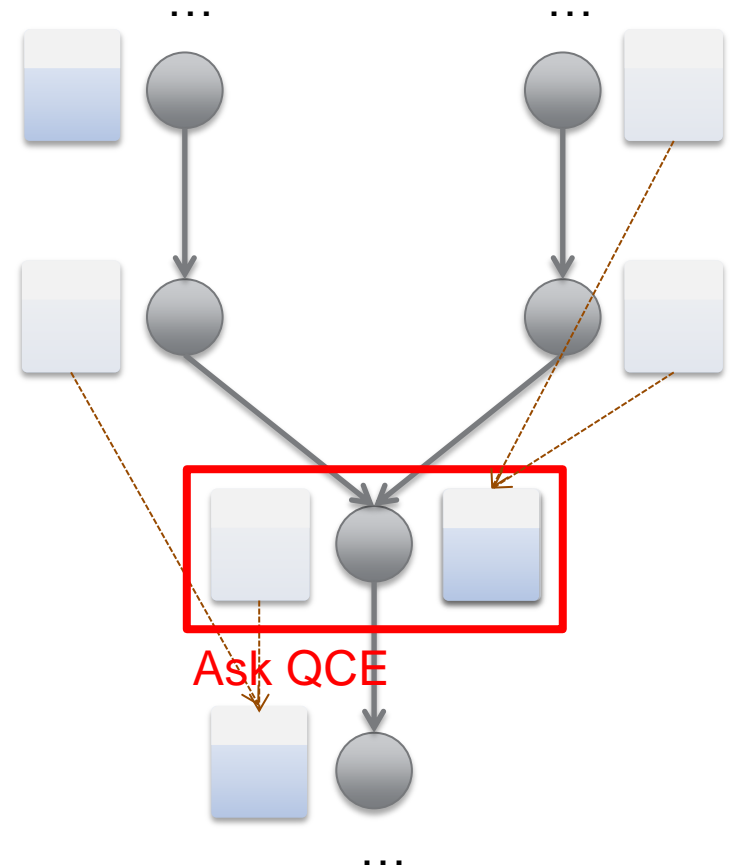
- Maintain bounded history of predecessor states





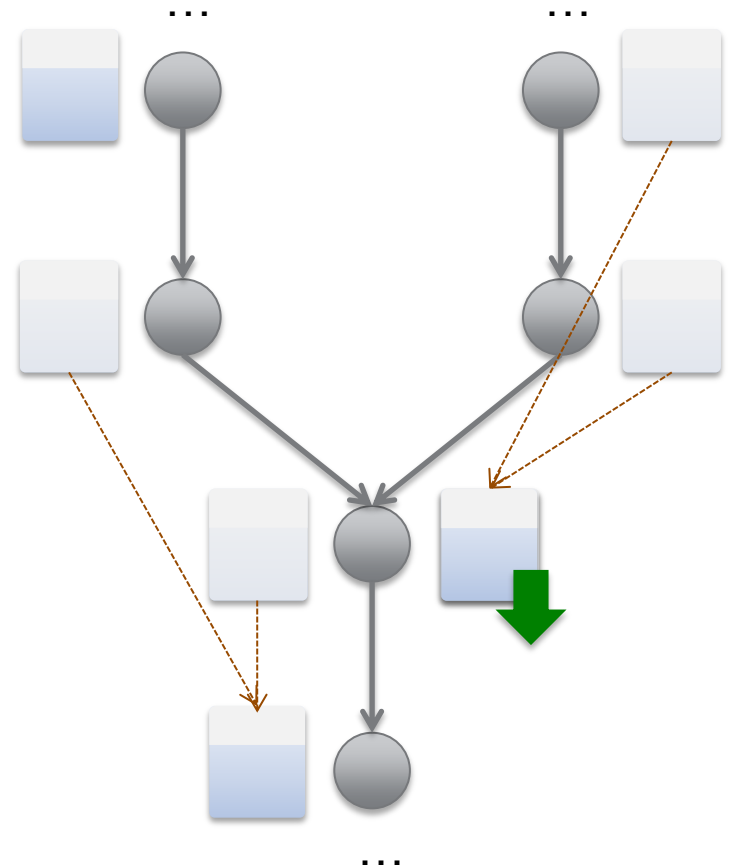
# Dynamic State Merging

- Maintain bounded history of predecessor states
- QCE compares a state to predecessors of others



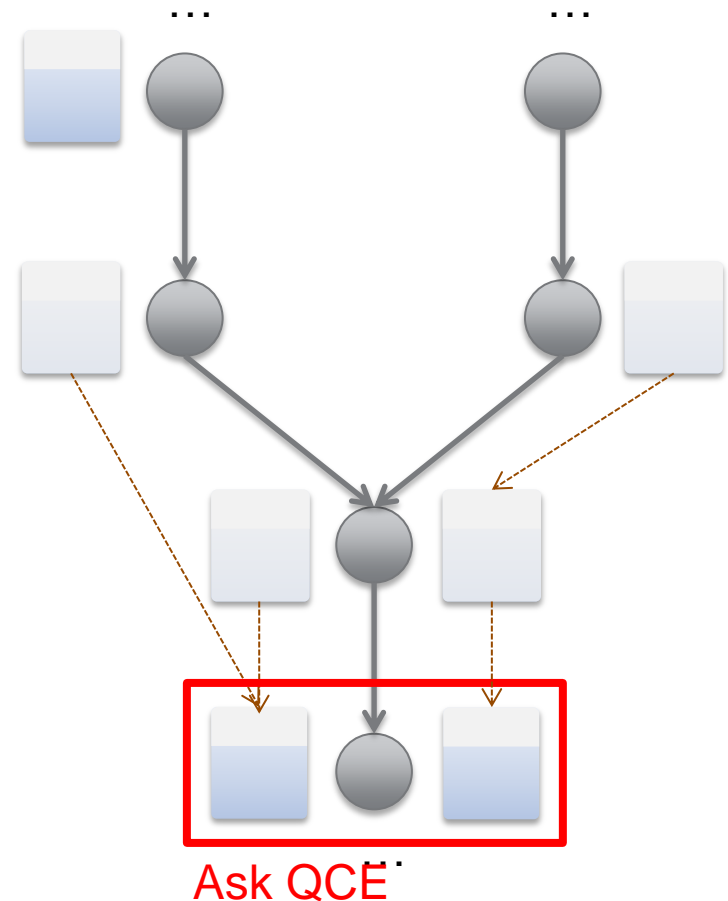
# Dynamic State Merging

- Maintain bounded history of predecessor states
- QCE compares a state to predecessors of others
- Matching states are prioritized
- Original search strategy controls remaining worklist



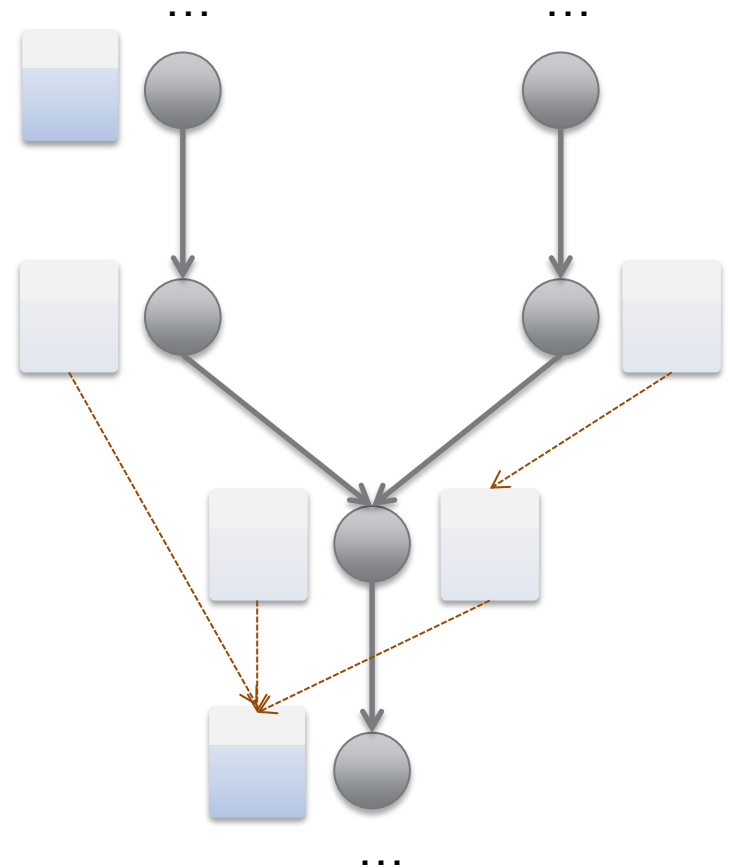
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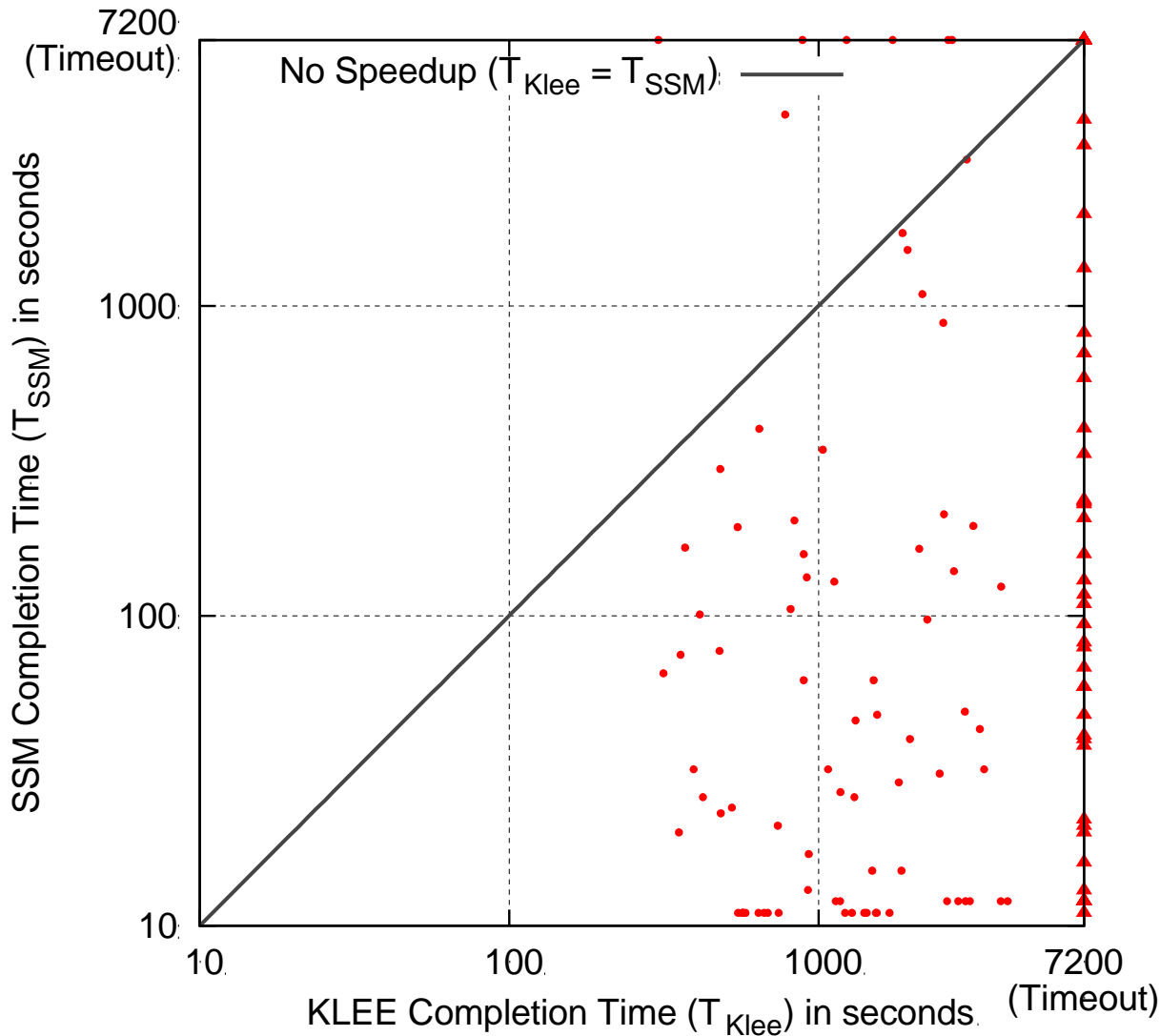
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# Evaluation

- Our prototype
  - *Based on state-of-the-art engine KLEE*
  - *QCE implemented in LLVM – static analysis completes in seconds*
- Analysis Targets
  - *96 GNU Coreutils (echo, ls, dd, who, ...)*
  - *2'000 – 10'000 executable lines of code per tool*
  - *72 KLOC in total*

# Time for Exhaustive Exploration



Triangle: KLEE time-out (> 2h)

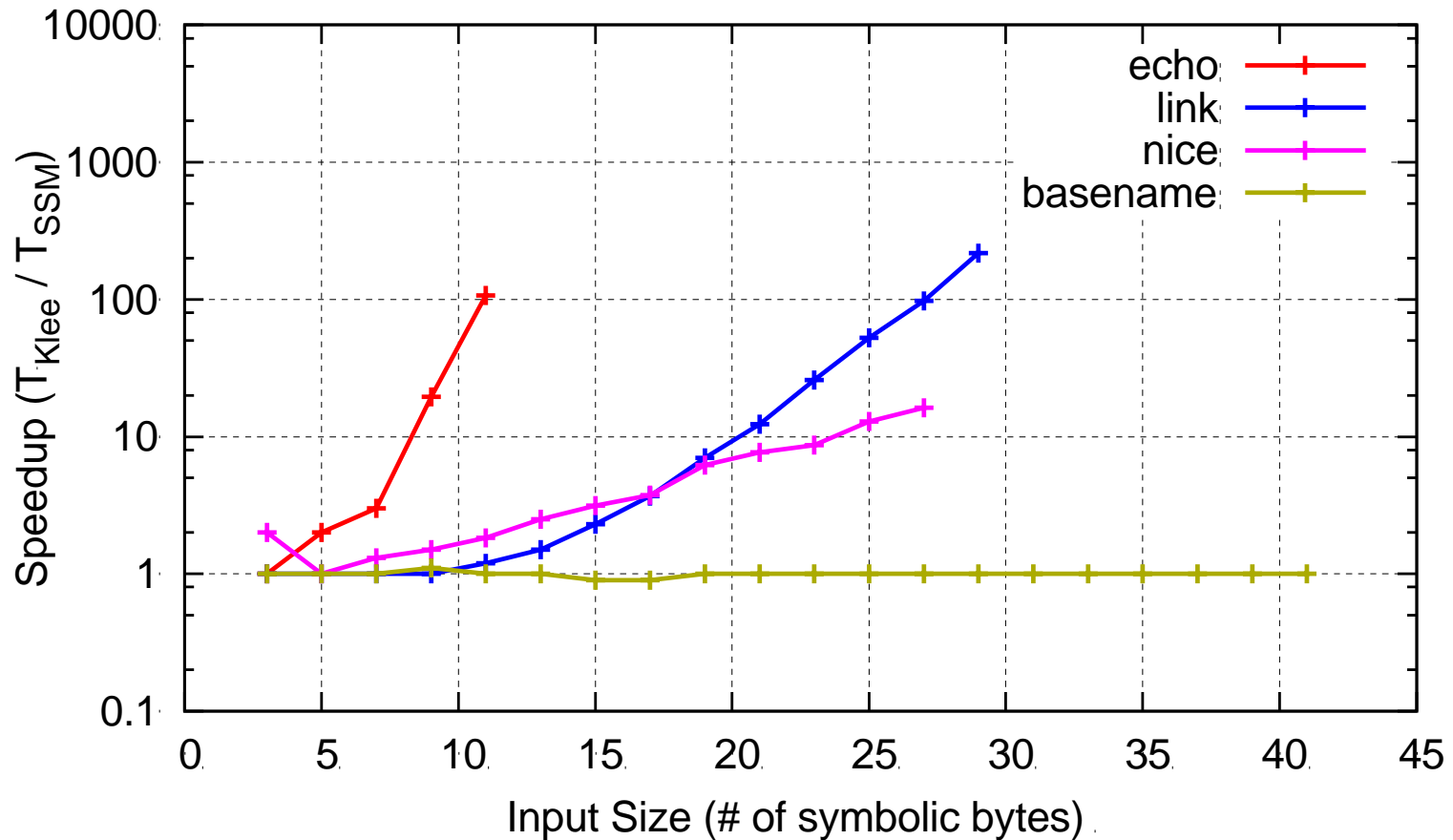
QCE + SSM vs. KLEE.

Static state merging (SSM) follows topological order.

**Consistent speedups**

# Speedup vs. Input-Size (Exhaustive)

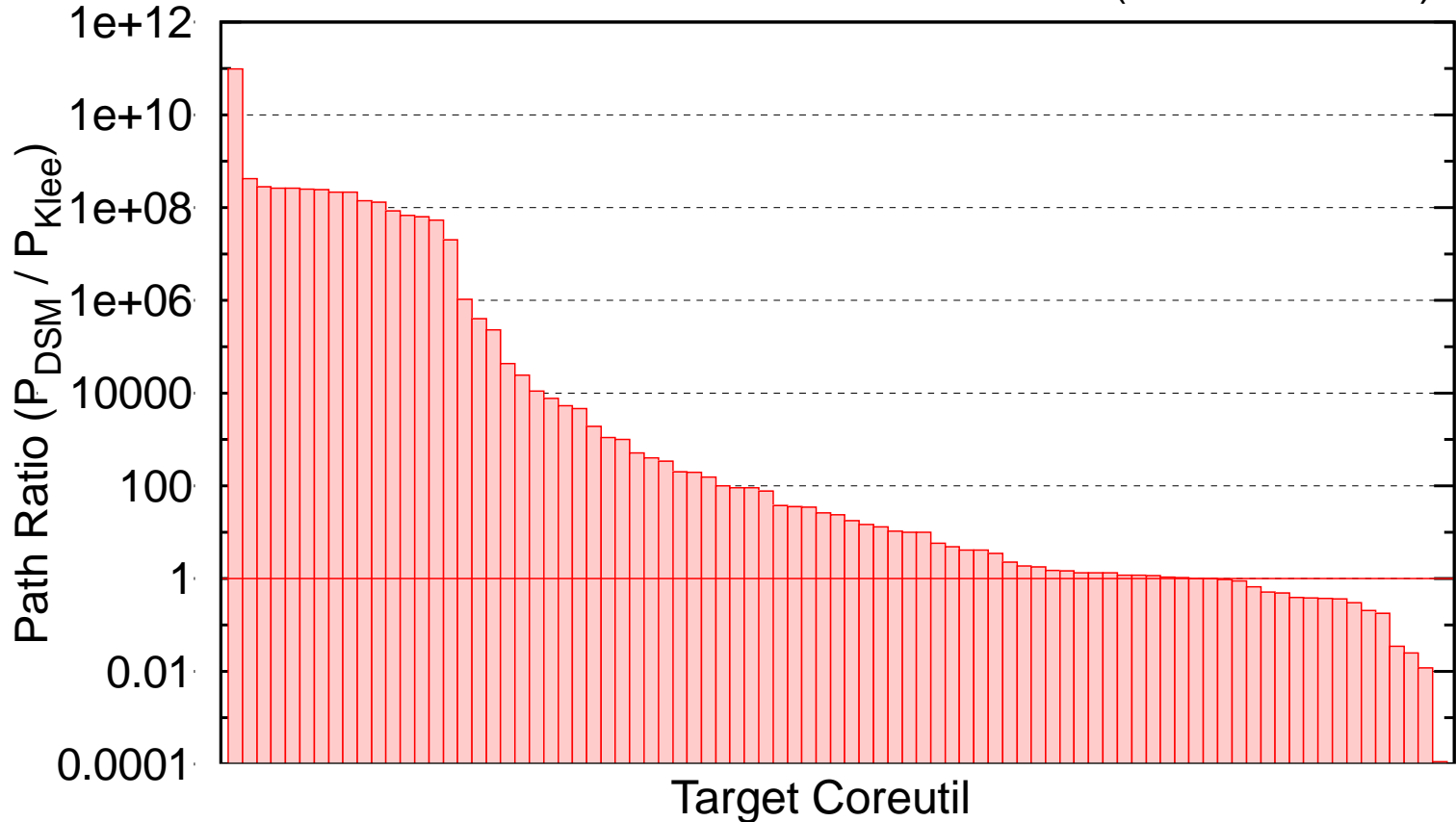
QCE + SSM vs. KLEE.



**Exponential speedups in symbolic input size**

# # Paths in Incomplete Exploration

QCE + DSM vs. KLEE (1h time bound).



**Up to 11 orders of magnitude more paths explored**



# Combating Path Explosion

- Dynamic merging (DSM + QCE)
- Static merging of small structures [Avgerinos et al., ICSE'14]
- Procedure summaries [Godefroid, POPL'07]
- Parallelization [Bucur et al, EuroSys'11]

# Outline

- Symbolic Execution for Testing
- State Merging – Fighting Path Explosion
- Interpreted High-Level Code

Programming  
Languages

Symbolic Execution  
Engines

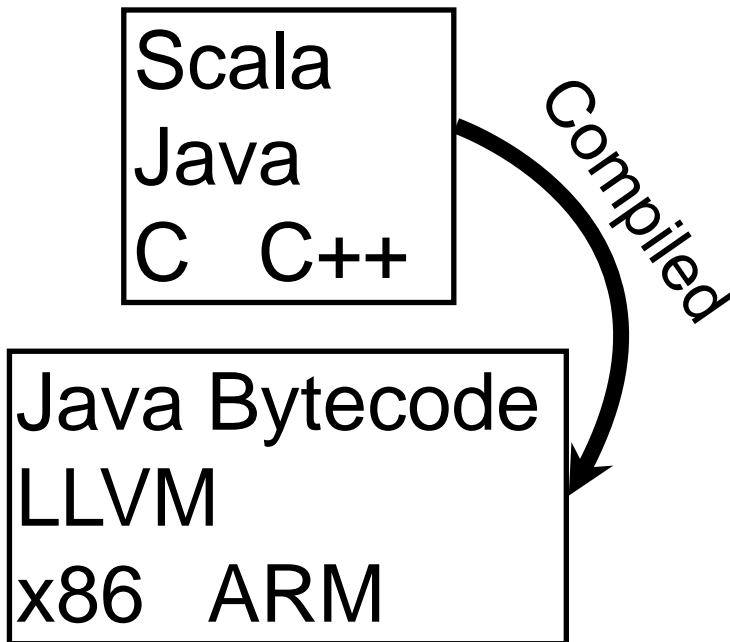
Programming  
Languages

Symbolic Execution  
Engines

Scala  
Java  
C C++

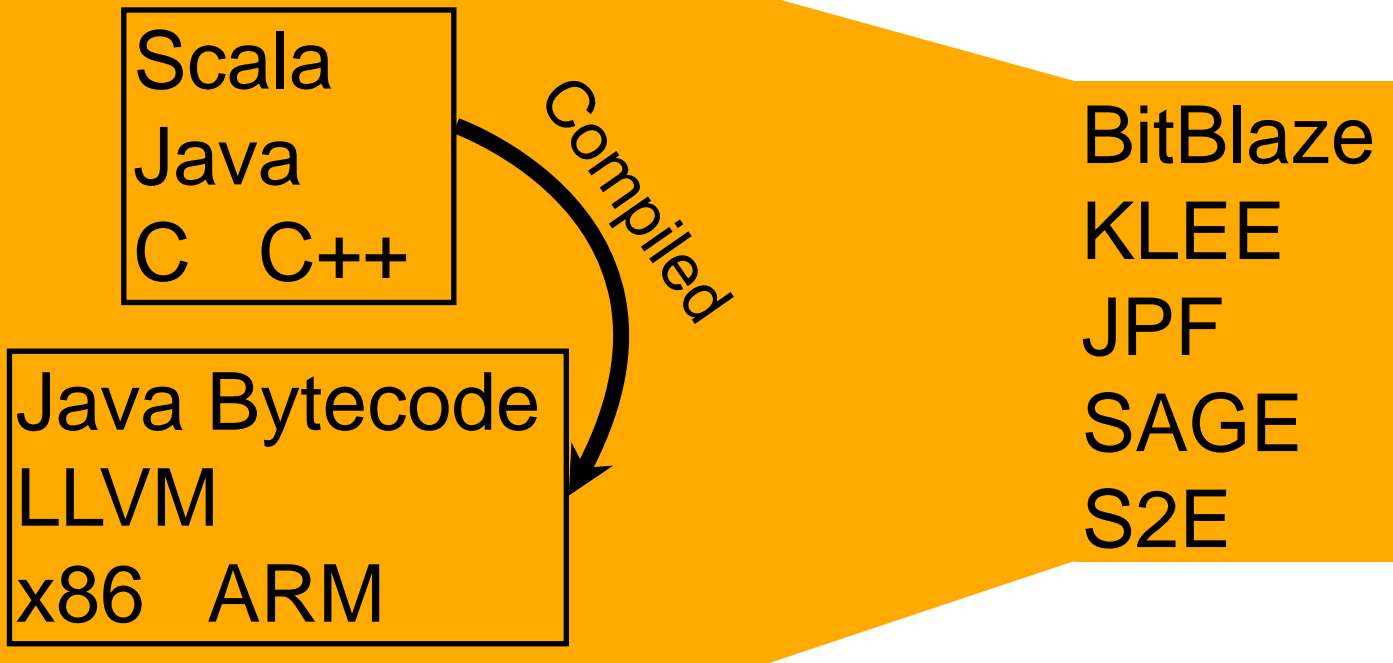
Programming  
Languages

Symbolic Execution  
Engines



## Programming Languages

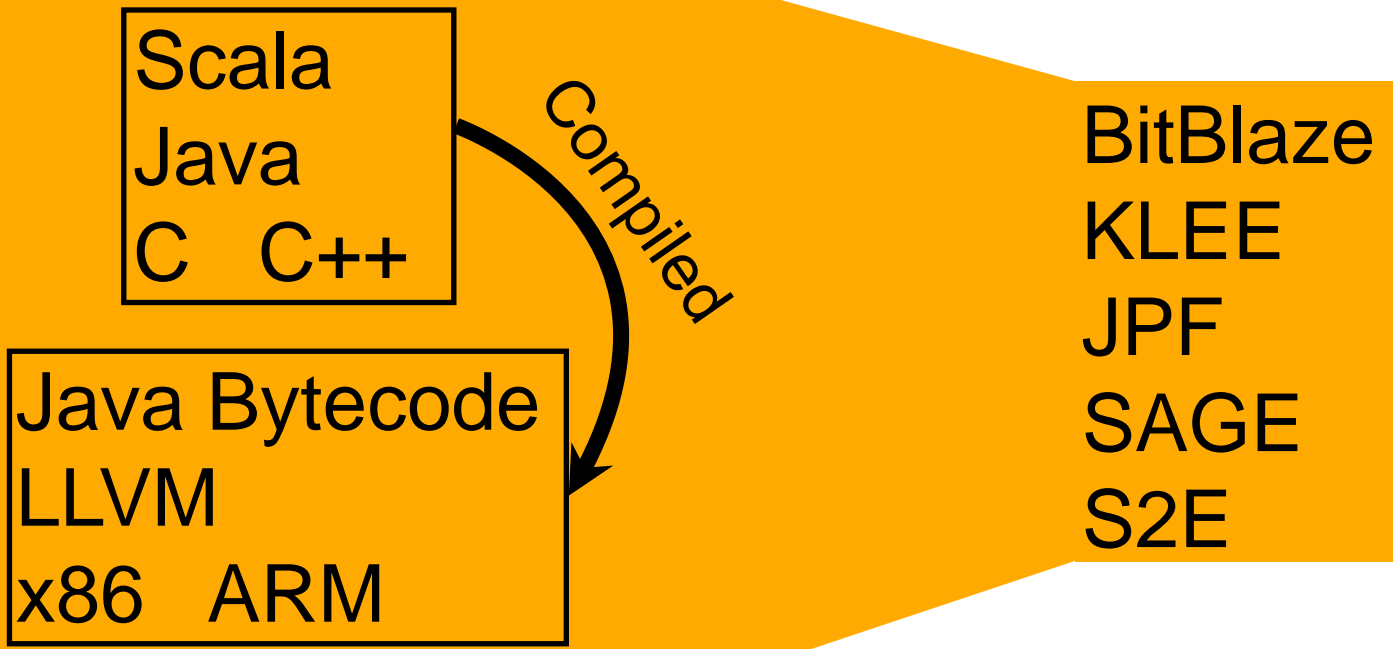
## Symbolic Execution Engines



## Programming Languages

Python Ruby  
Lua JavaScript  
Bash Perl

## Symbolic Execution Engines



## Programming Languages

## Symbolic Execution Engines

Python Ruby  
Lua JavaScript  
Bash Perl

?

Scala  
Java  
C C++

Java Bytecode  
LLVM  
x86 ARM

Compiled

BitBlaze  
KLEE  
JPF  
SAGE  
S2E



# Interpreted Languages

```
def parse_file(file_name):  
  
    with open(file_name, "r") as f:  
  
        data = f.read()  
  
    return json.loads(data, encoding="utf-8")
```

# Interpreted Languages

```
def parse_file(file_name):
```

Since Python 2.5 `with` `open(file_name, "r") as f:`

```
    data = f.read() Complete  
           File Read
```

```
    return json.loads(data, encoding="utf-8") Incomplete  
                                                Specification
```

Complex semantics

+

Ambiguity in specifications

+

Evolving language

+

Large standard library

+

Widespread native methods

# Interpreted Languages

```
def parse_file(file_name):
```

Since Python 2.5 `with` `open(file_name, "r") as f:`

```
    data = f.read() Complete  
           File Read
```

```
    return json.loads(data, encoding="utf-8") Incomplete  
                                                Specification
```

Too much work

Complex semantics  
+  
Ambiguity in specifications  
+  
Evolving language  
+  
Large standard library  
+  
Widespread native methods

*“Consequently, if you were coming from Mars and tried to re-implement Python from this document alone, you might have to **guess things** and in fact you would probably end up **implementing quite a different language.**”*

- The Python Language Reference

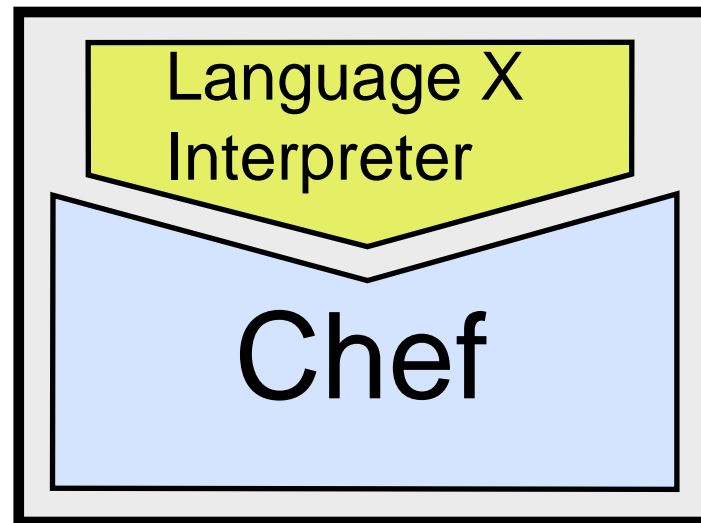
How can we **efficiently** obtain  
a **correct** symbolic execution engine?

## **Key idea:**

Use the language interpreter  
as executable specification

## Key idea:

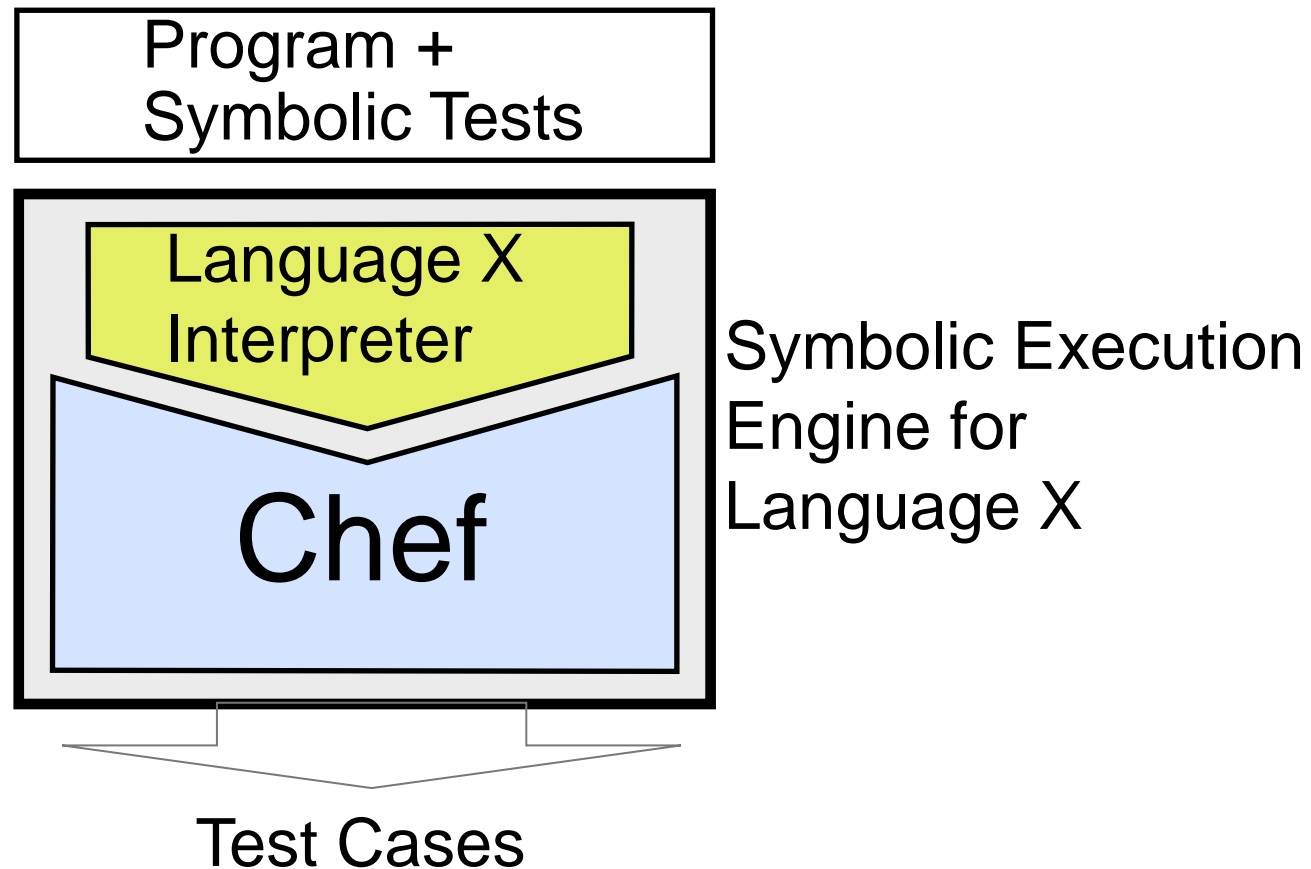
Use the language interpreter  
as executable specification



Symbolic Execution  
Engine for  
Language X

## Key idea:

Use the language interpreter  
as executable specification





# Chef Overview

- Built on top of the S2E symbolic execution engine for x86
- Relies on lightweight interpreter instrumentation + optimizations
- Prototyped engines for Python and Lua in 5 + 3 person-days

# Testing Interpreted Programs

Naive approach: Run interpreter in stock SE engine

# Testing Interpreted Programs

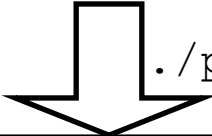
Naive approach: Run interpreter in stock SE engine

```
def validateEmail(email):  
    pos = email.find("@")  
    if pos < 1:  
        raise InvalidEmailError()  
    if email.rfind(".") < pos:  
        raise InvalidEmailError()
```

# Testing Interpreted Programs

Naive approach: Run interpreter in stock SE engine

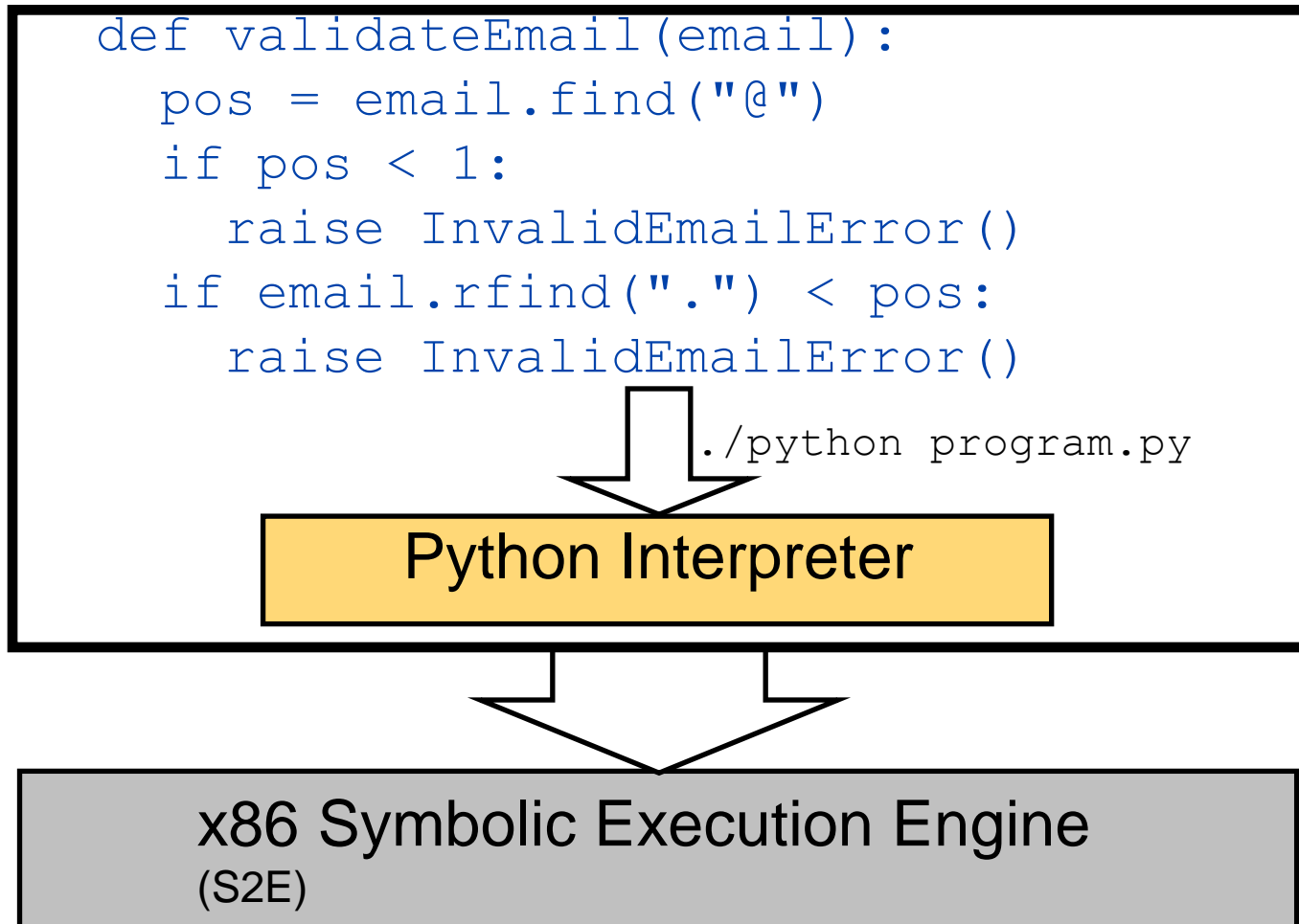
```
def validateEmail(email):  
    pos = email.find("@")  
    if pos < 1:  
        raise InvalidEmailError()  
    if email.rfind(".") < pos:  
        raise InvalidEmailError()
```

 ./python program.py

**Python Interpreter**

# Testing Interpreted Programs

Naive approach: Run interpreter in stock SE engine



# Naive approach:

## Run interpreter in stock symbolic execution engine

```
pos = email.find("@")
```

```
{
```

```
    unsigned long mask;
```

```
    Py_ssize_t skip, count = 0;
```

```
    Py_ssize_t i, j, mlast, w;
```

```
    w = n - m;
```

```
    if (w < 0 || (mode == FAST_COUNT && maxcount == 0))  
        return -1;
```

```
    /* look for special cases */
```

```
    if (m <= 1) {
```

```
        if (m <= 0)
```

```
            return -1;
```

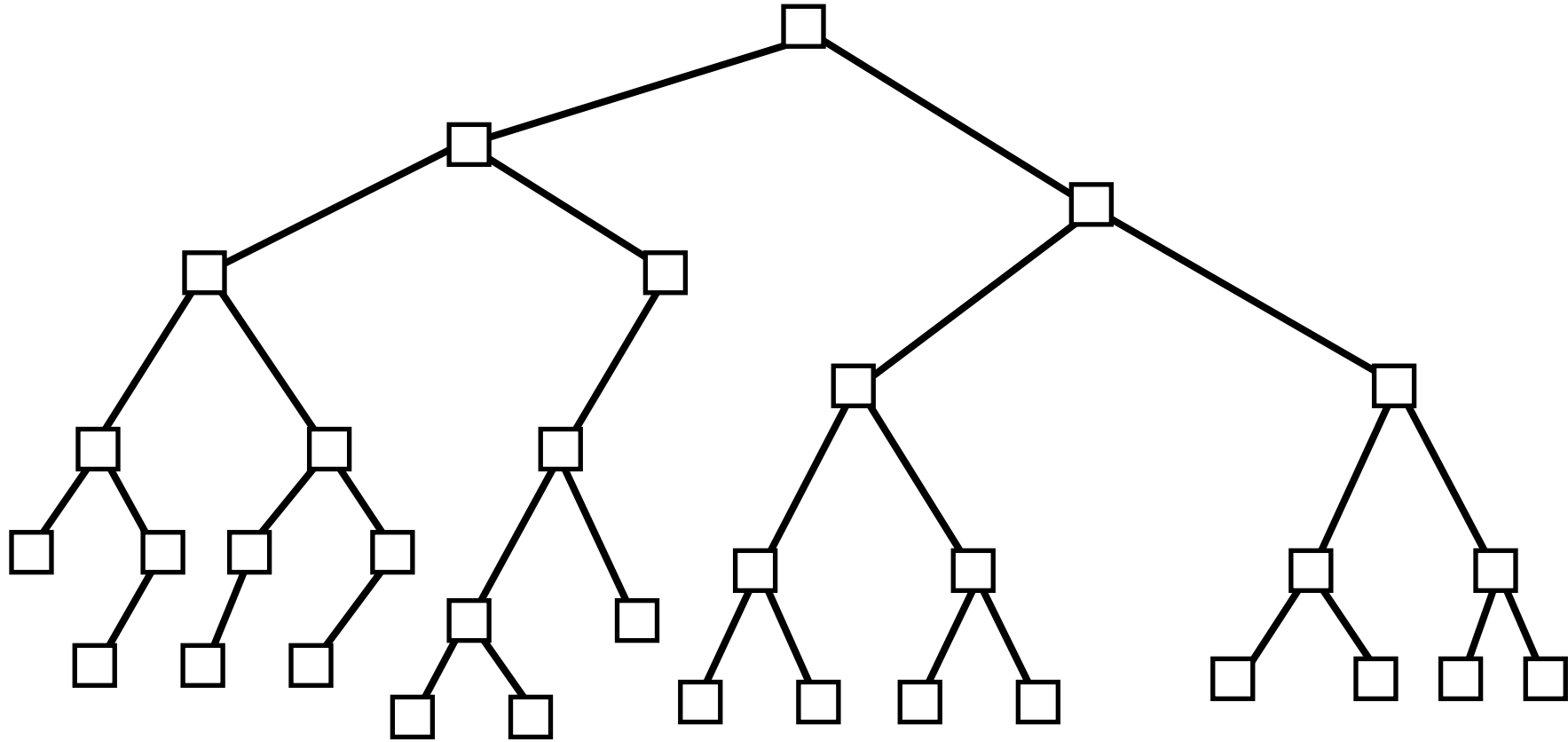
```
        /* use special case for 1-character strings */
```

```
        if (mode == FAST_COUNT) {
```

Naive approach:

Run interpreter in stock symbolic execution engine

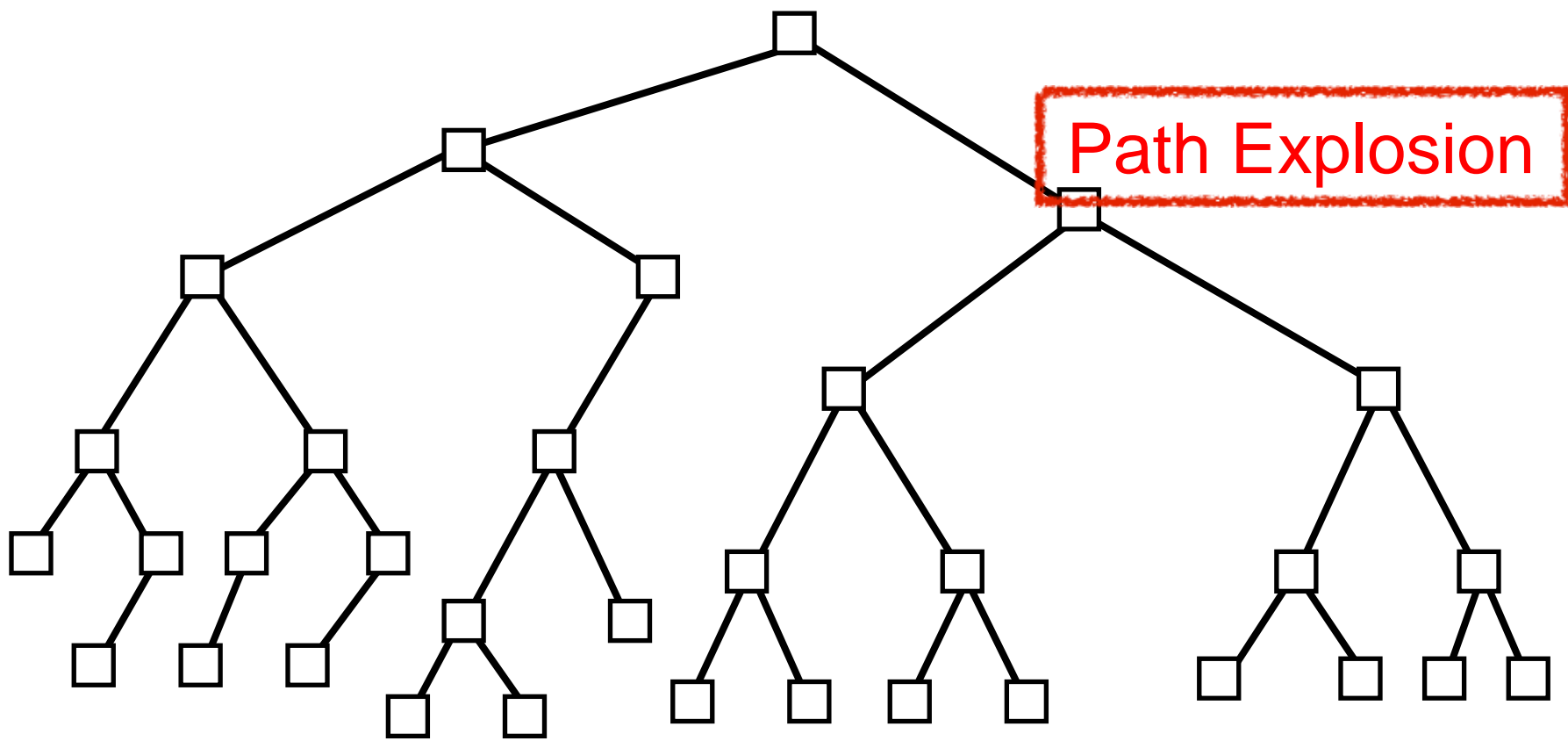
```
pos = email.find("@")
```



Naive approach:

Run interpreter in stock symbolic execution engine

```
pos = email.find("@")
```



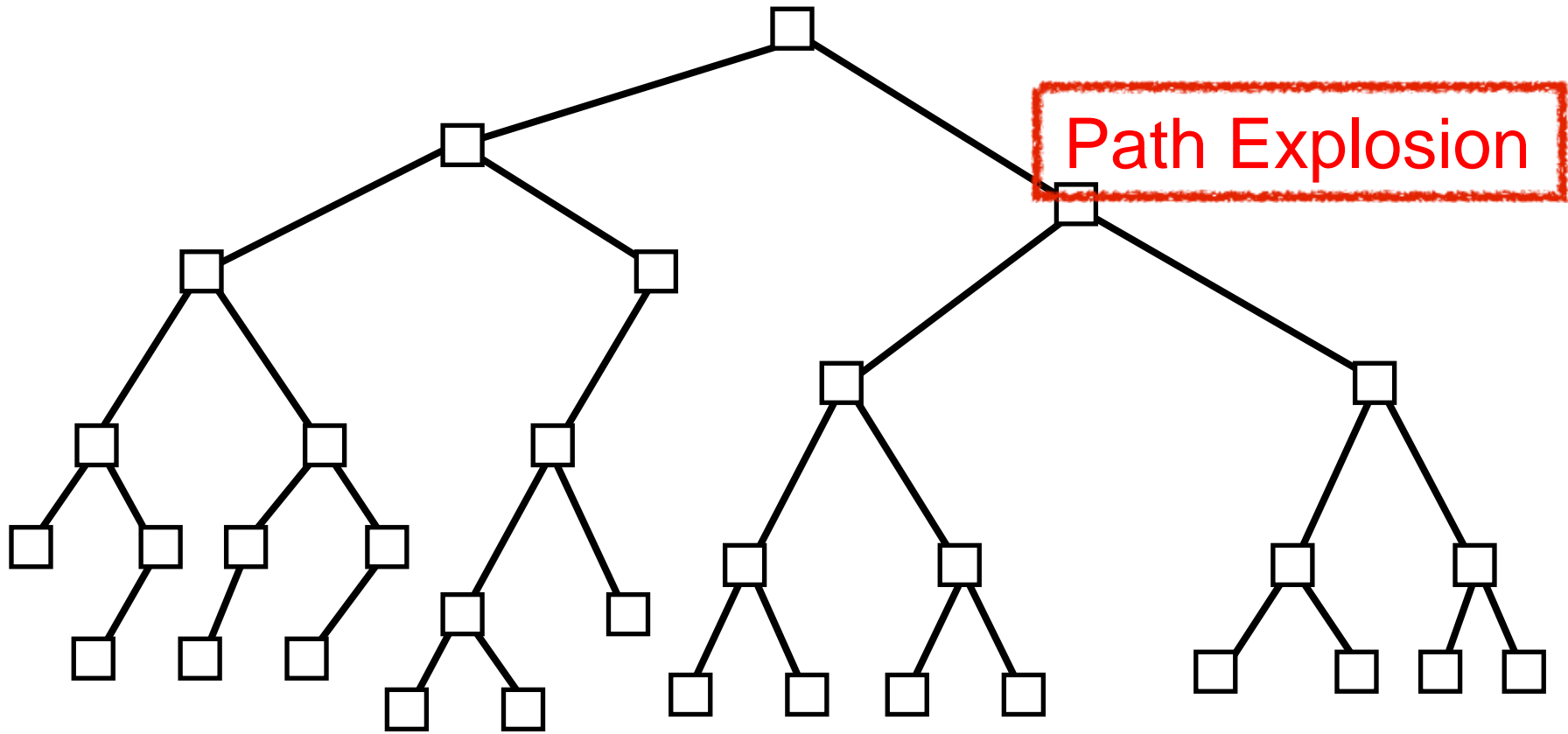


Naive approach:

~~Run interpreter in stock symbolic execution engine~~

Gets lost in the details of the implementation

```
pos = email.find("@")
```



# High-level Execution Paths

```
def validate_email(email):
```

```
    pos = email.find("@")
```

```
    if pos < 1:
```

```
        raise
```

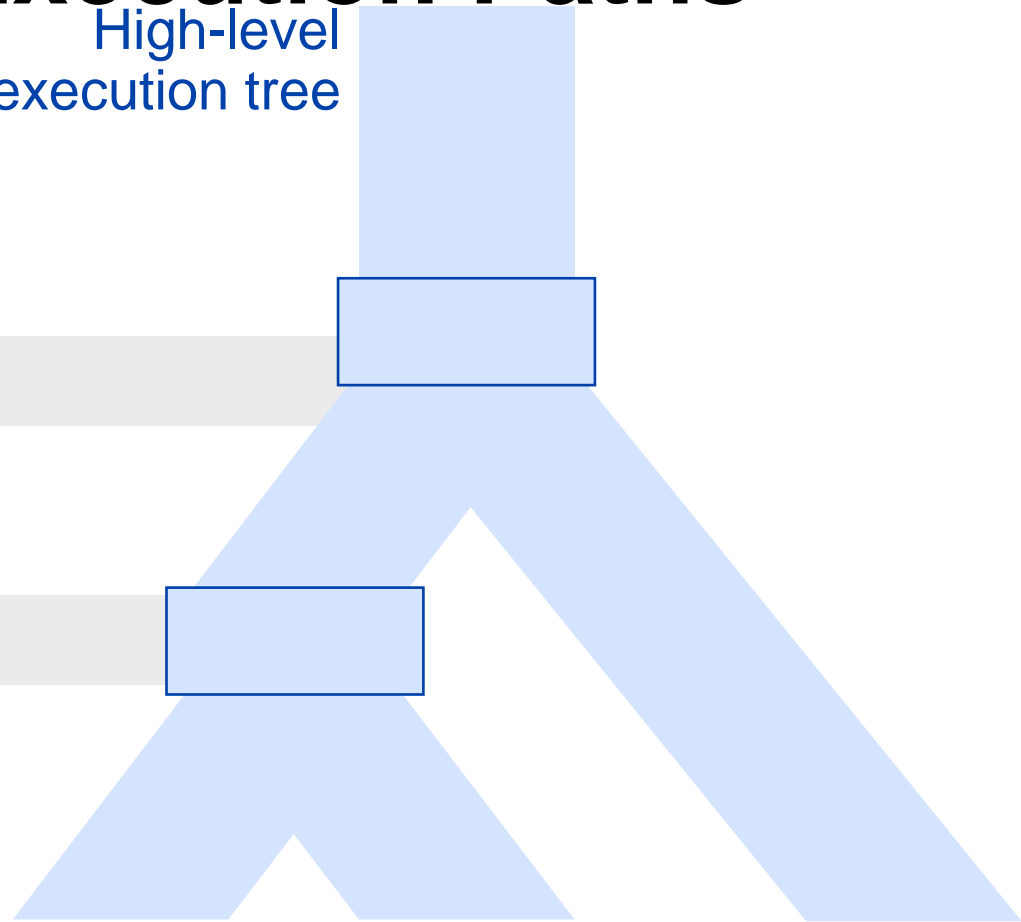
```
        InvalidEmailError()
```

```
    if email.rfind(".") < pos:
```

```
        raise
```

```
        InvalidEmailError()
```

High-level  
execution tree



# High-level Execution Paths

```
def validate_email(email):
```

```
    pos = email.find("@")
```

```
    if pos < 1:
```

```
        raise
```

```
    InvalidEmailError()
```

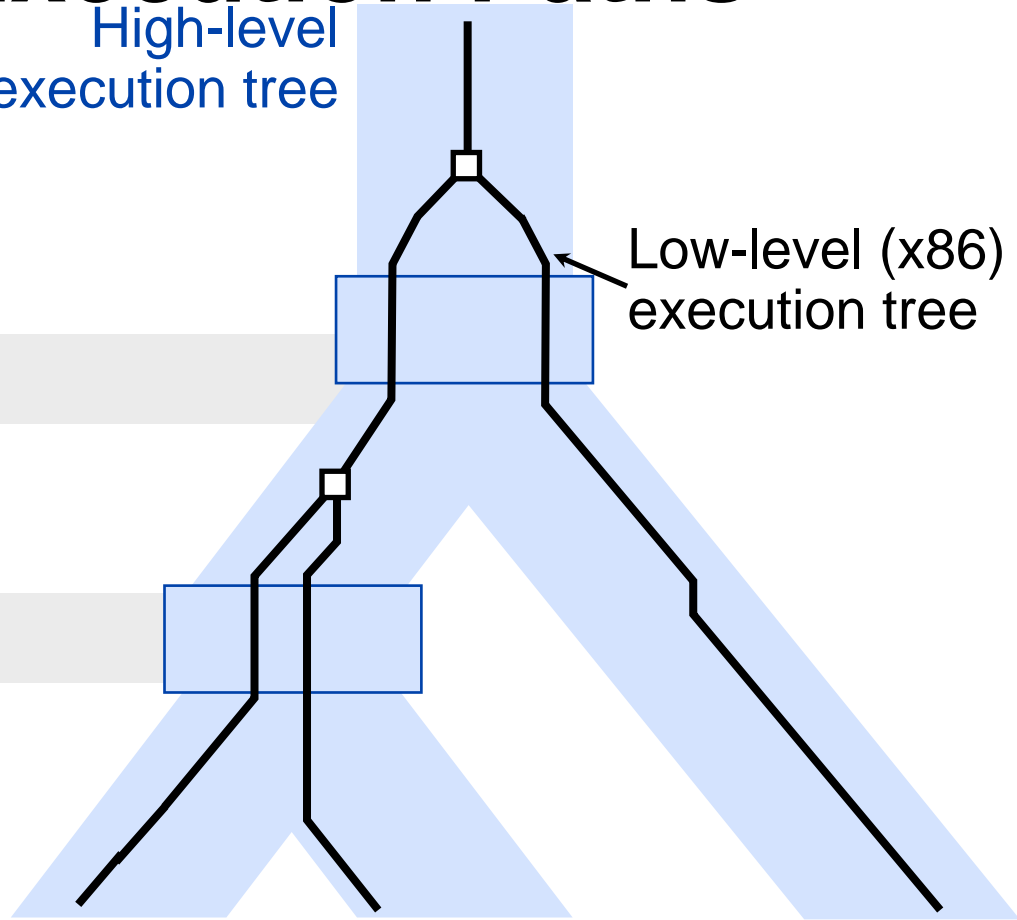
```
    if email.rfind(".") < pos:
```

```
        raise
```

```
    InvalidEmailError()
```

High-level  
execution tree

Low-level (x86)  
execution tree



# High-level Execution Paths

```
def validate_email(email):
```

```
    pos = email.find("@")
```

```
    if pos < 1:
```

```
        raise
```

```
        InvalidEmailError()
```

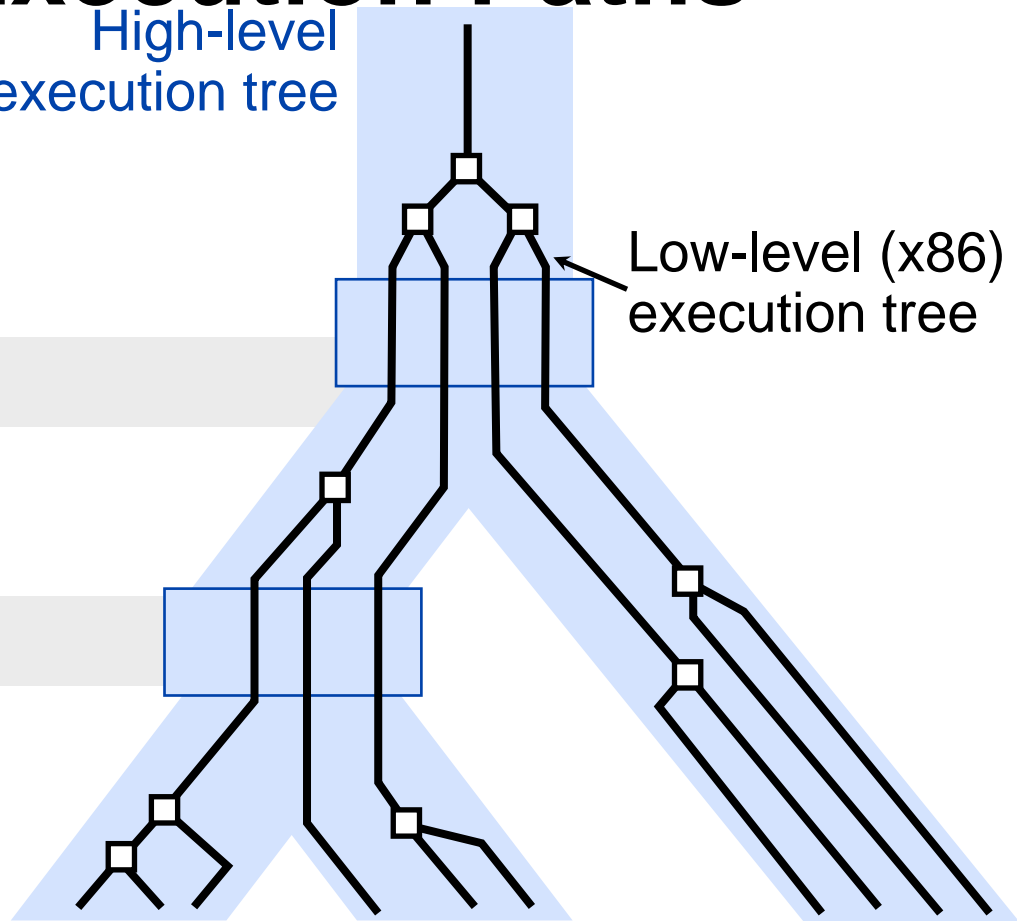
```
    if email.rfind(".") < pos:
```

```
        raise
```

```
        InvalidEmailError()
```

High-level  
execution tree

Low-level (x86)  
execution tree

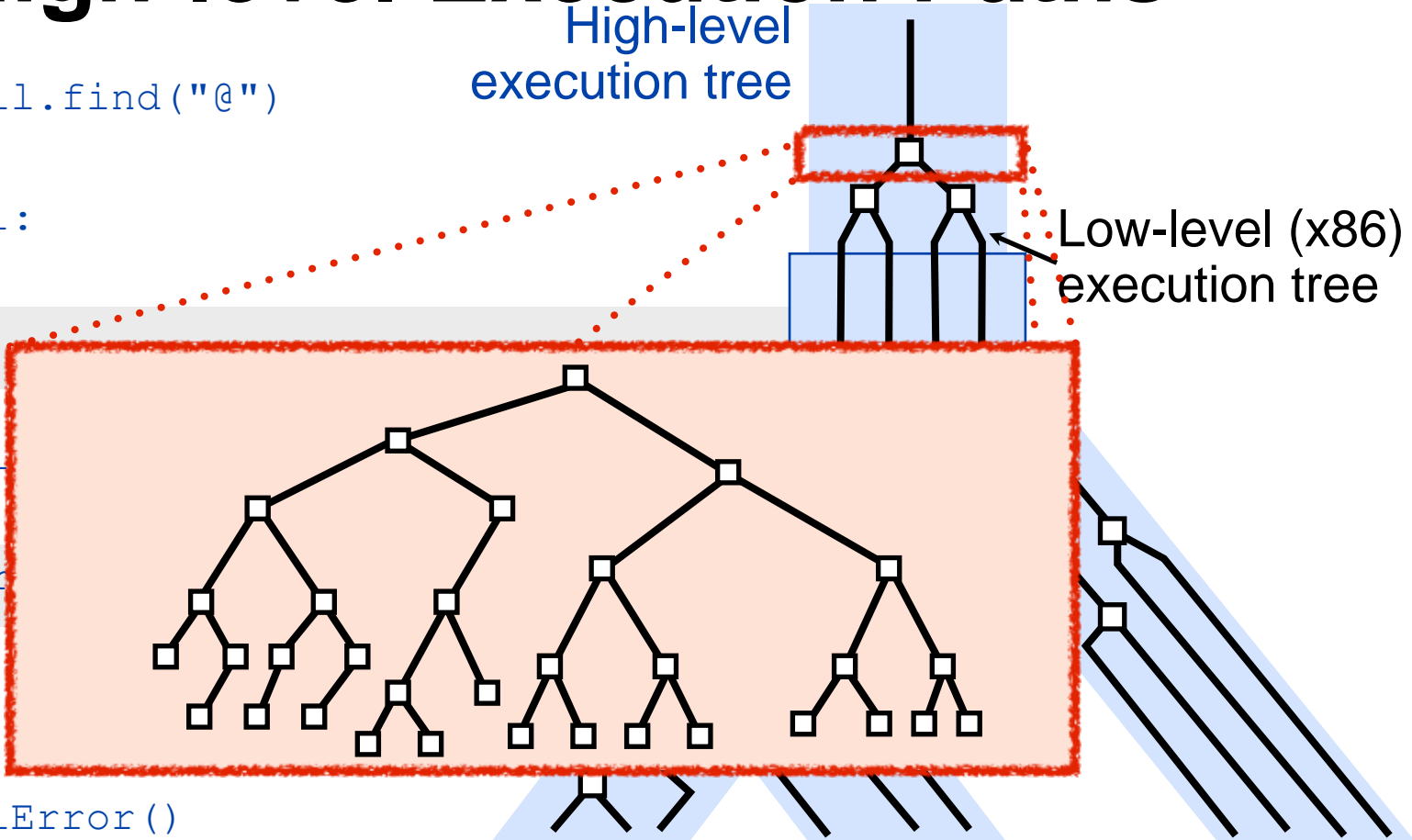


# High-level Execution Paths

```
def validate_email(email):  
    pos = email.find("@")  
  
    if pos < 1:  
        raise  
        InvalidEmail  
  
    if email.r  
        raise  
        InvalidEmailError()
```

High-level  
execution tree

Low-level (x86)  
execution tree



# High-level Execution Paths

```
def validate_email(email):
```

```
    pos = email.find("@")
```

```
    if pos < 1:
```

```
        raise
```

```
    InvalidEmail
```

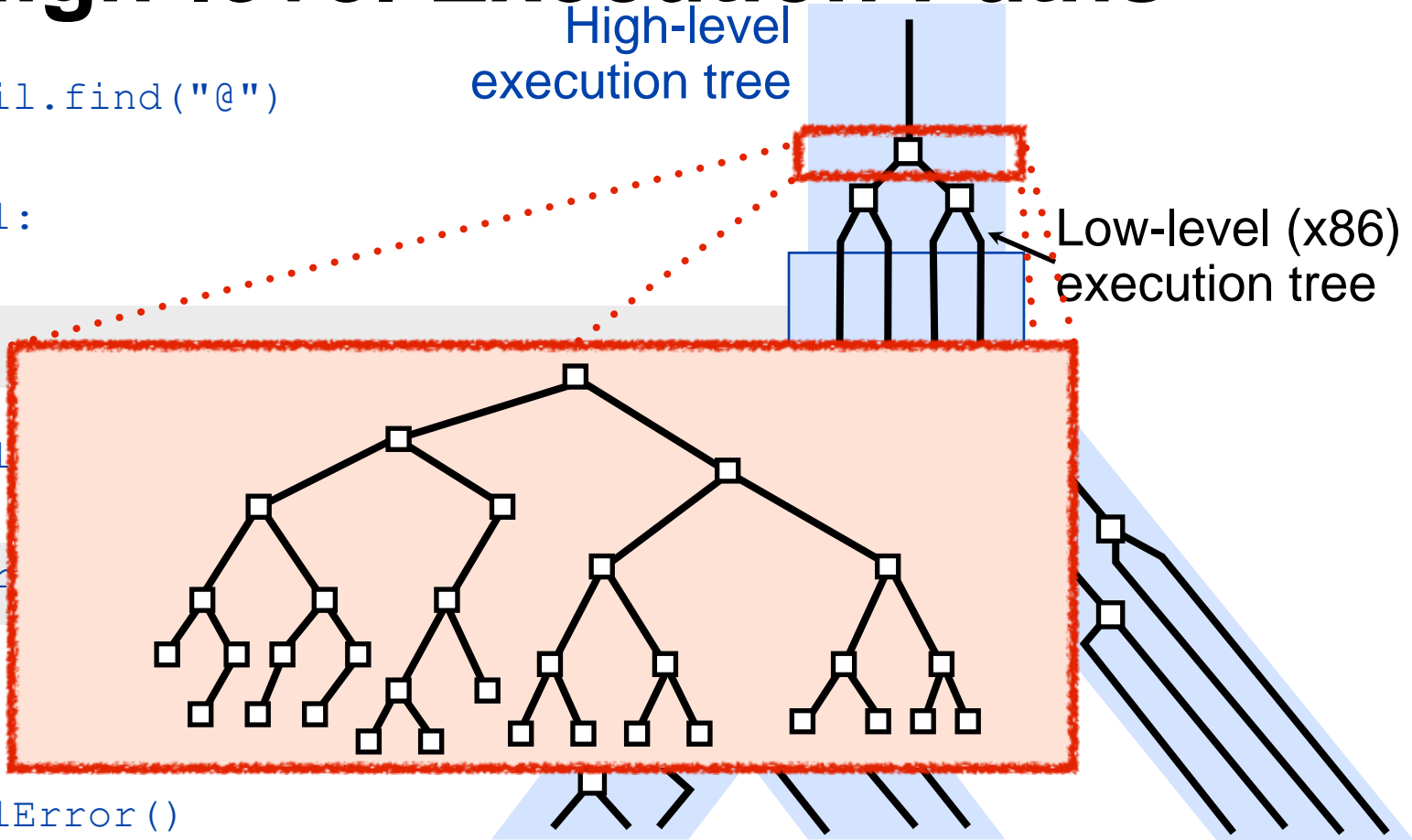
```
    if email.r
```

```
        raise
```

```
    InvalidEmailError()
```

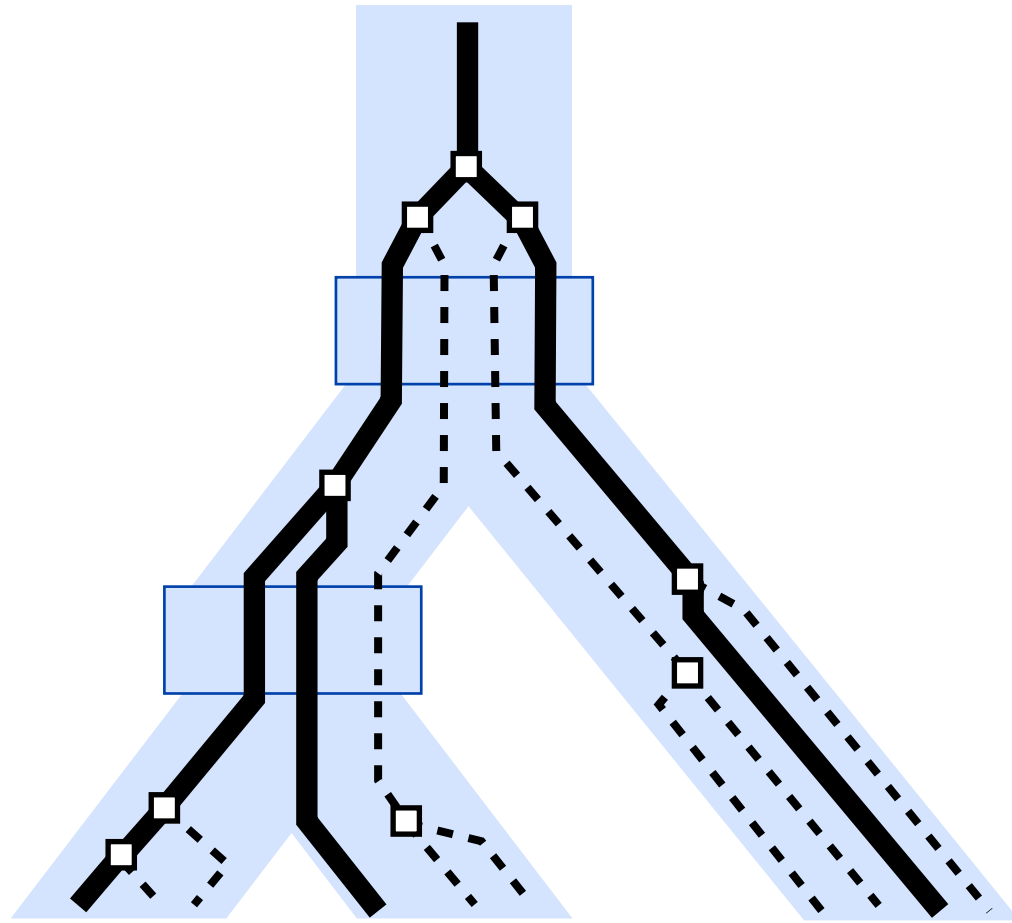
High-level  
execution tree

Low-level (x86)  
execution tree



3 HL paths  
10 LL paths

HL/LL path ratio is low  
due to path explosion

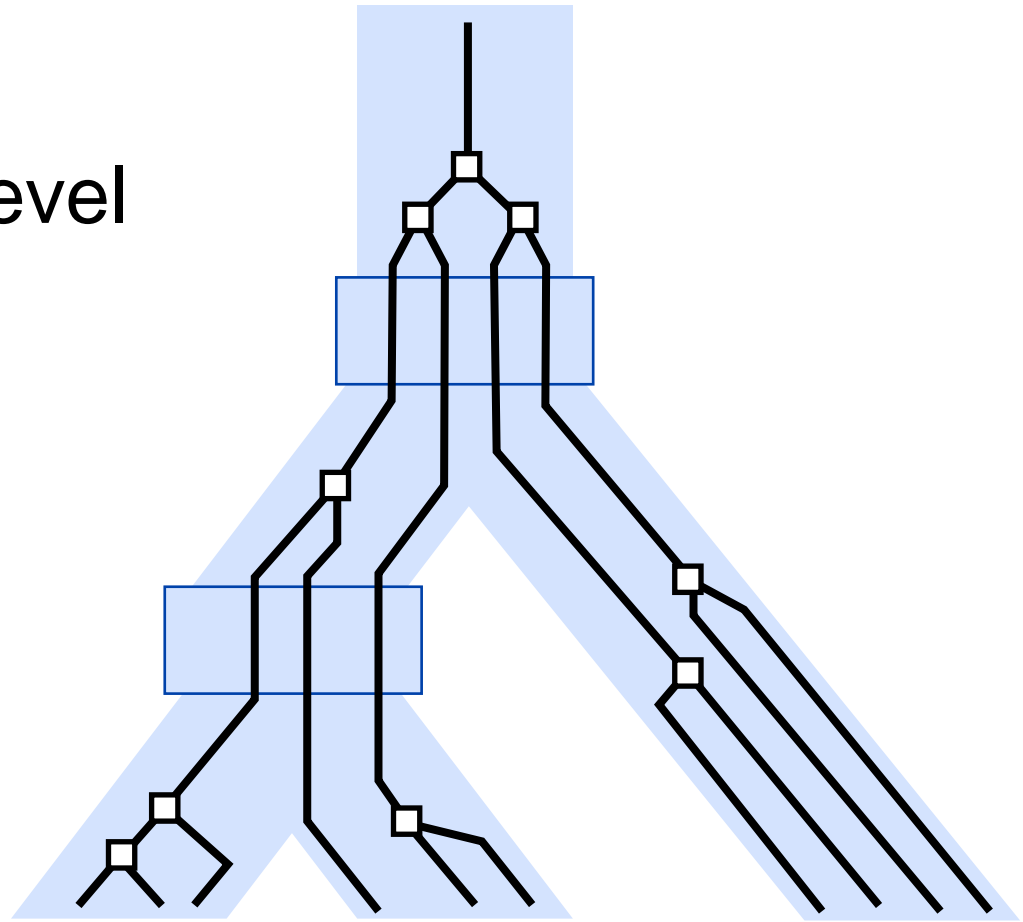


Goal:

Prioritize the low-level paths  
that maximize the HL/LL path ratio.

# High-level Execution Paths

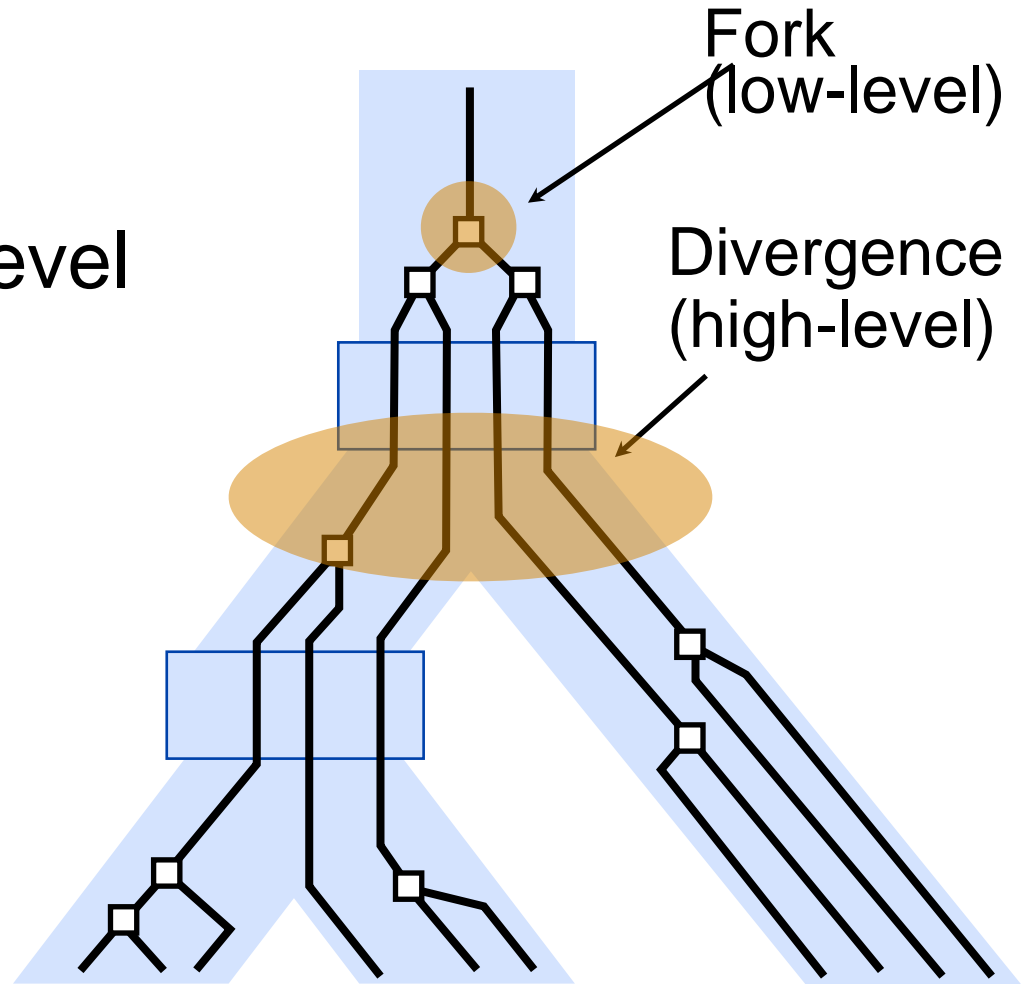
Alternative approach:  
Select states at high-level  
branches





# High-level Execution Paths

Alternative approach:  
Select states at high-level  
branches

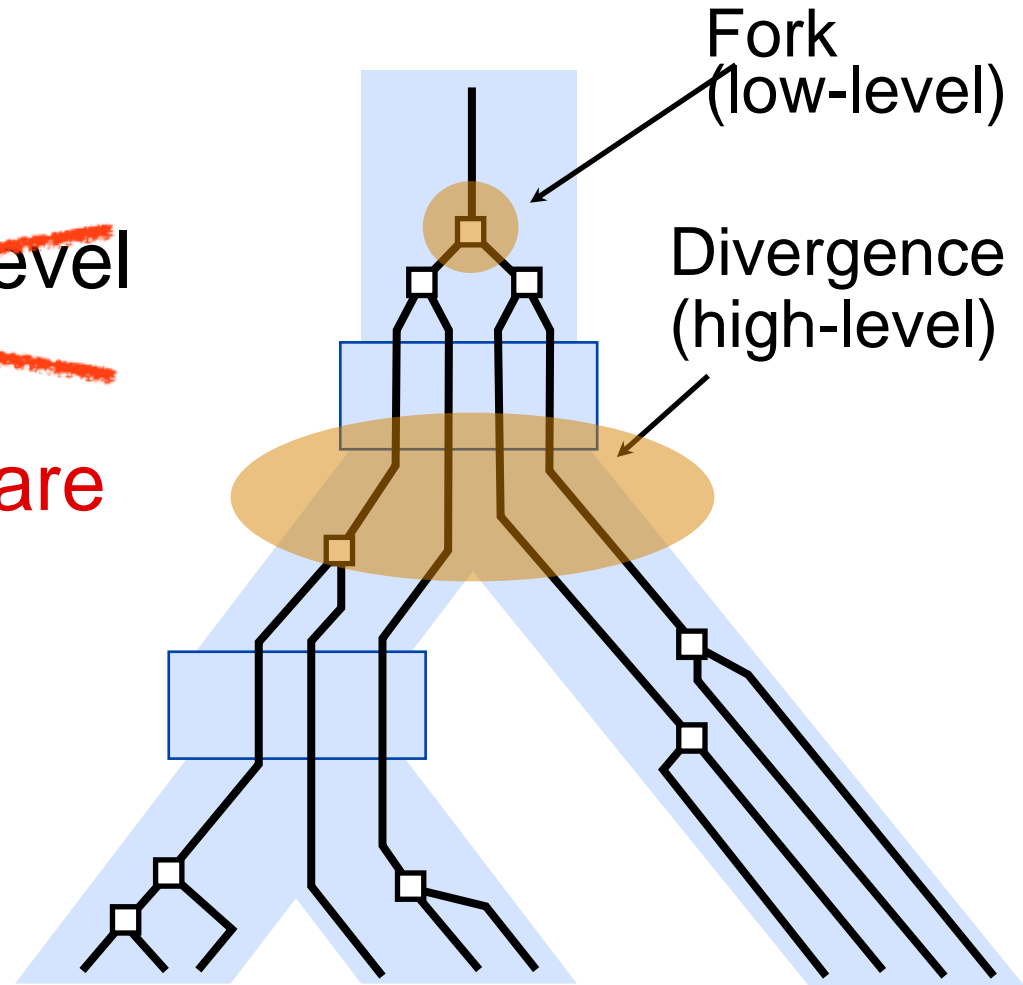


# High-level Execution Paths

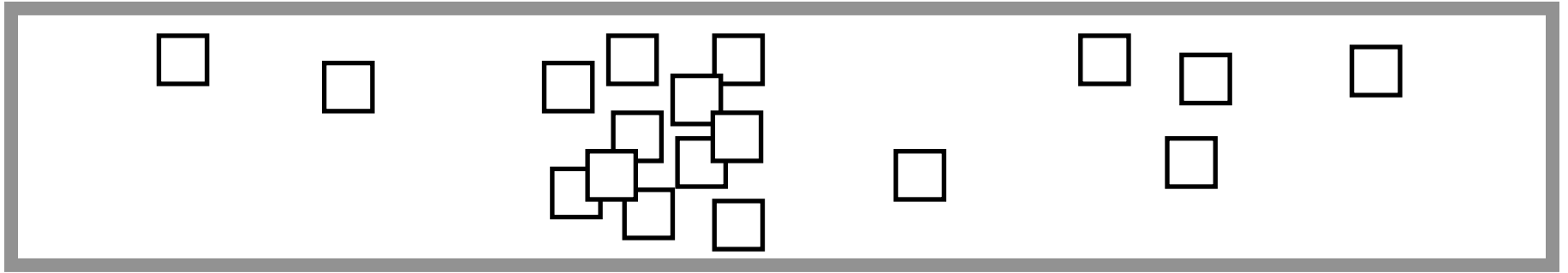
Alternative approach:

~~Select states at high-level branches~~

High-level fork points are unpredictable

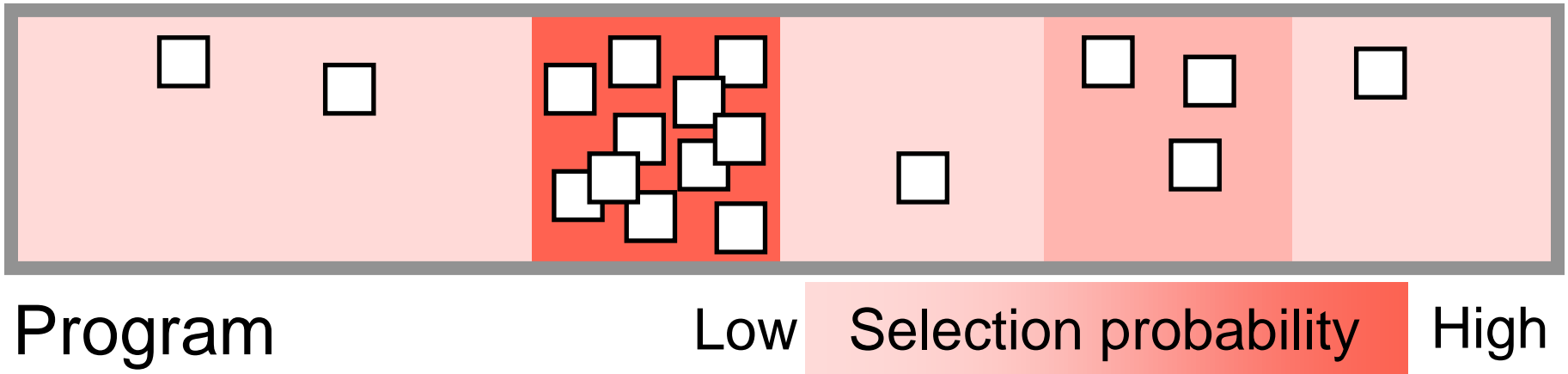


# Reducing Path Explosion



Program

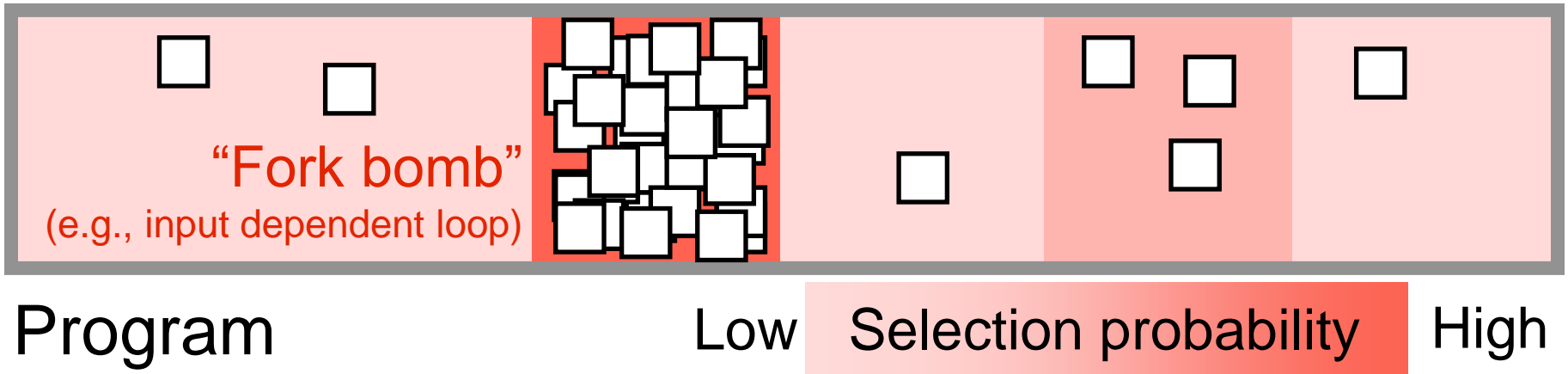
# Reducing Path Explosion



Fork points clustered in hot spots

# Reducing Path Explosion

Global DFS / BFS / randomized strategy

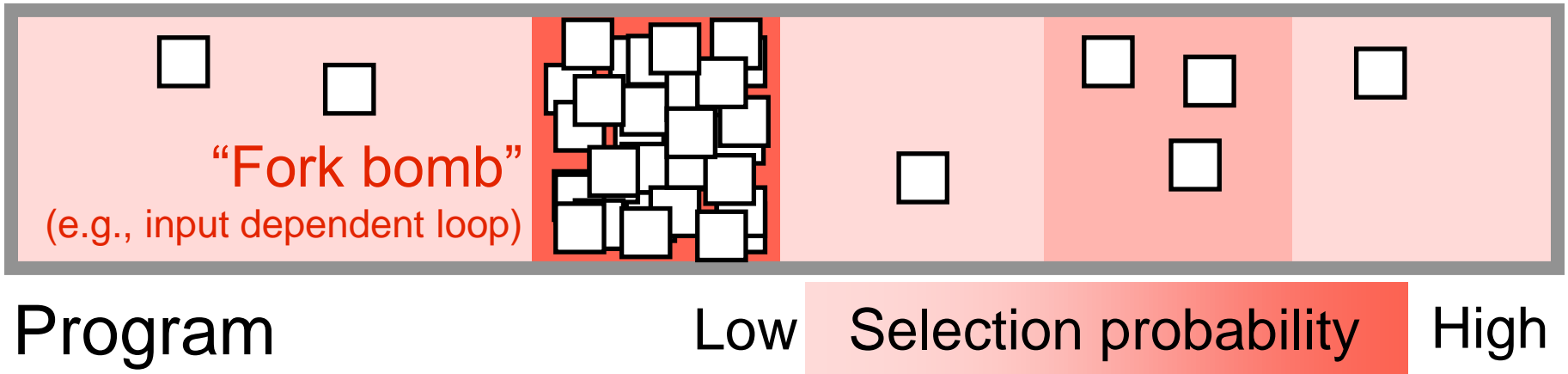


Fork points clustered in hot spots

Clusters grow bigger  $\Rightarrow$  Slower overall progress

# Reducing Path Explosion

Global DFS / BFS / randomized strategy



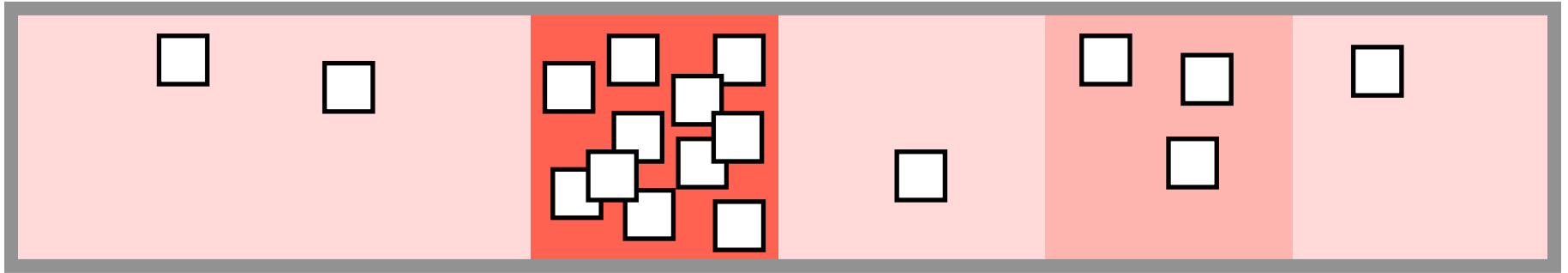
Fork points clustered in hot spots

Clusters grow bigger  $\Rightarrow$  Slower overall progress

Reduced state diversity

# Class-Uniform Path Analysis

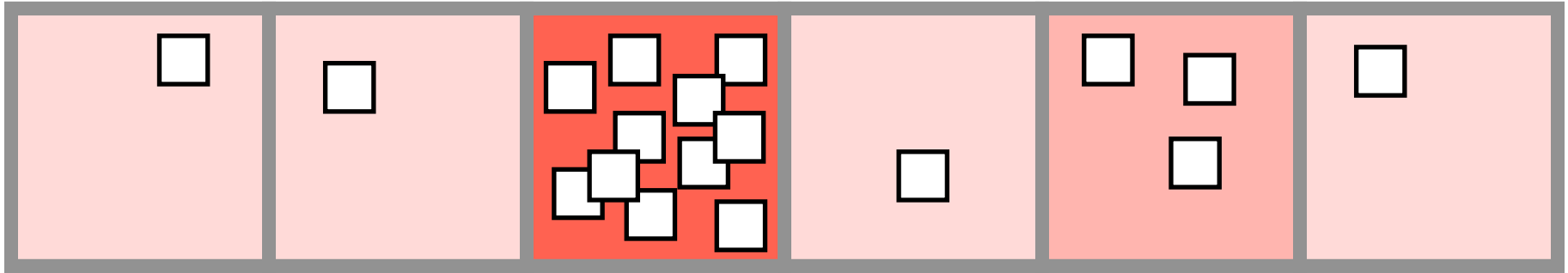
**Idea:** Partition the state space into groups



Program

# Class-Uniform Path Analysis

**Idea:** Partition the state space into groups

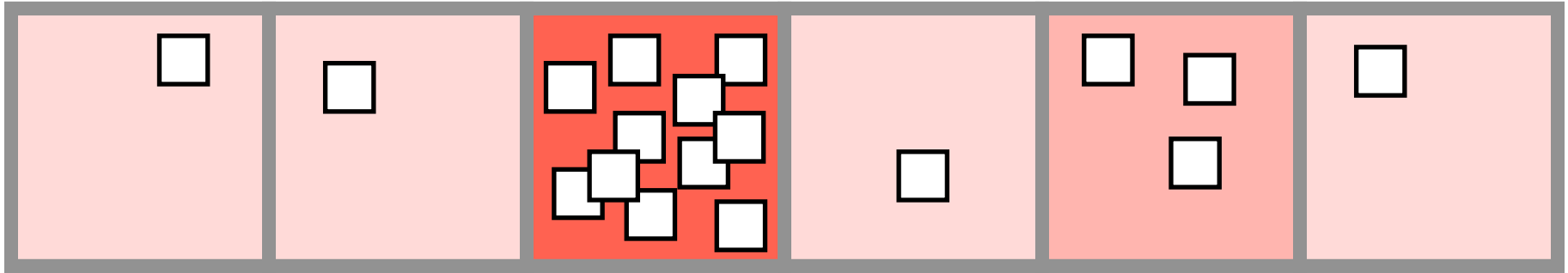


Program

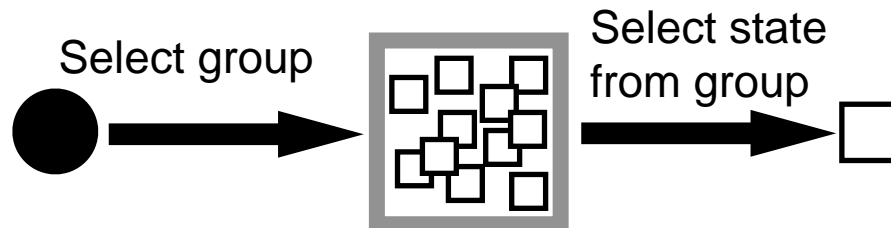


# Class-Uniform Path Analysis

**Idea:** Partition the state space into groups

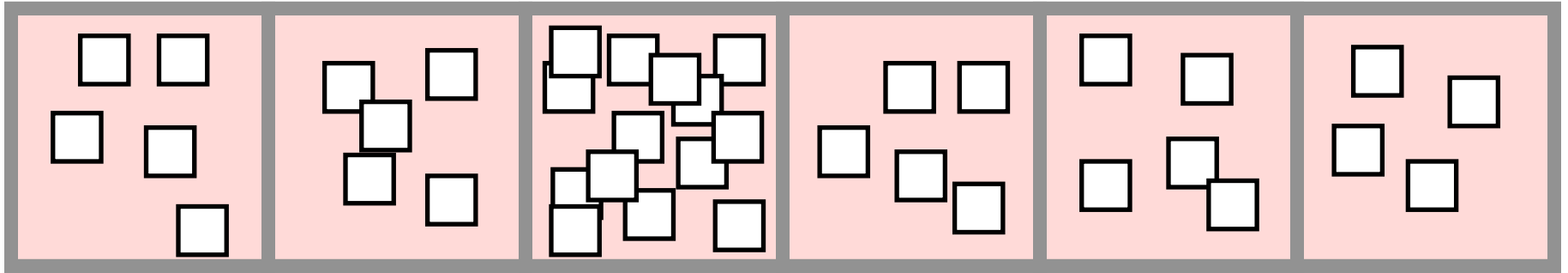


Program

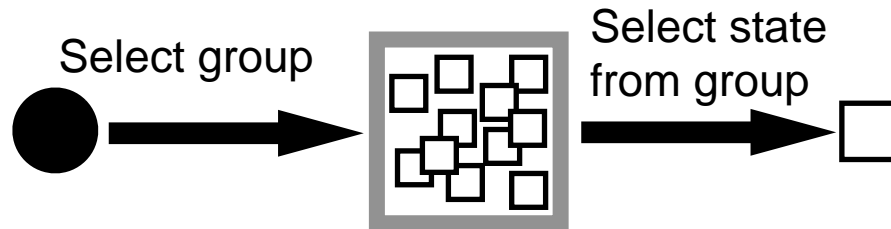


# Class-Uniform Path Analysis

**Idea:** Partition the state space into groups



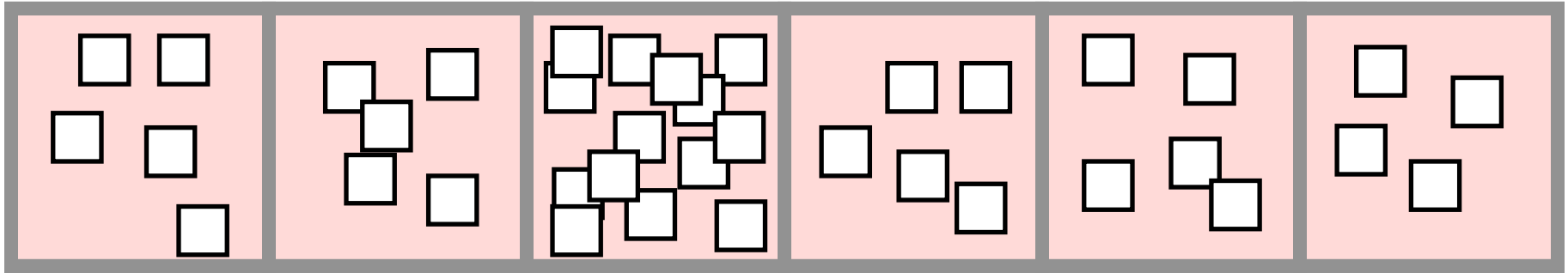
Program



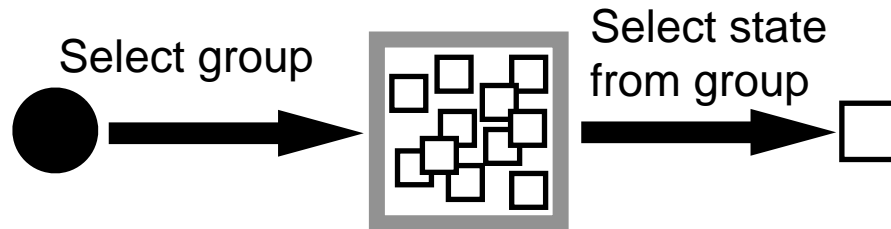
**Faster progress across all groups**

# Class-Uniform Path Analysis

**Idea:** Partition the state space into groups



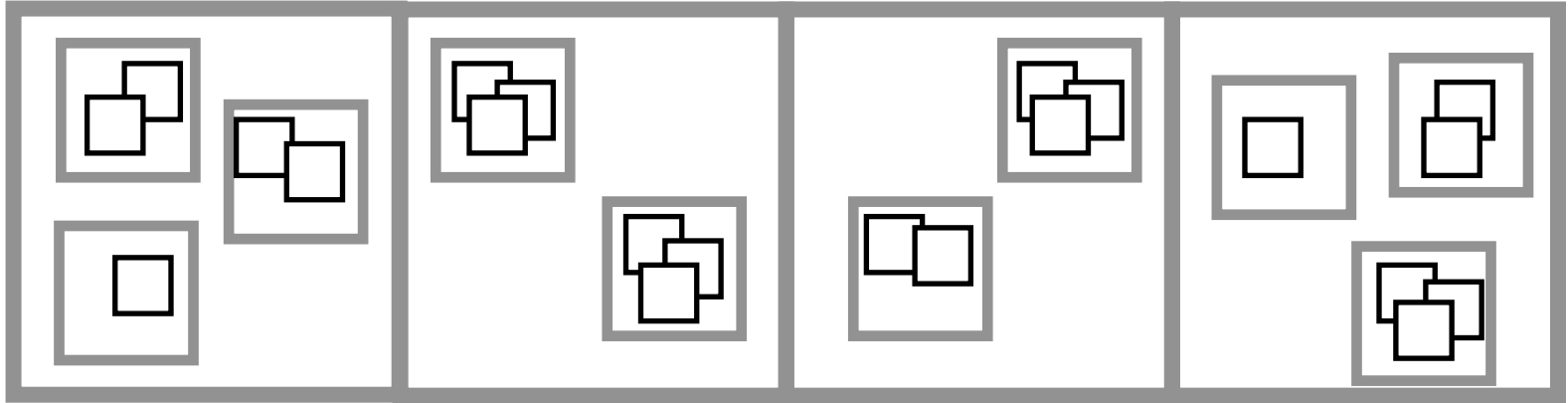
Program



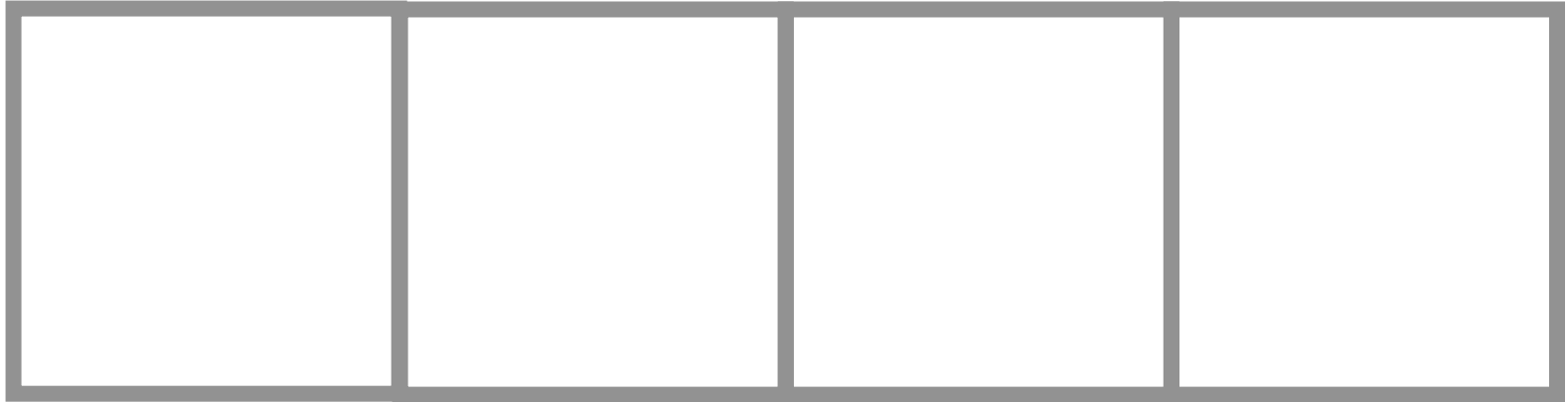
Faster progress across all groups

Increased state diversity

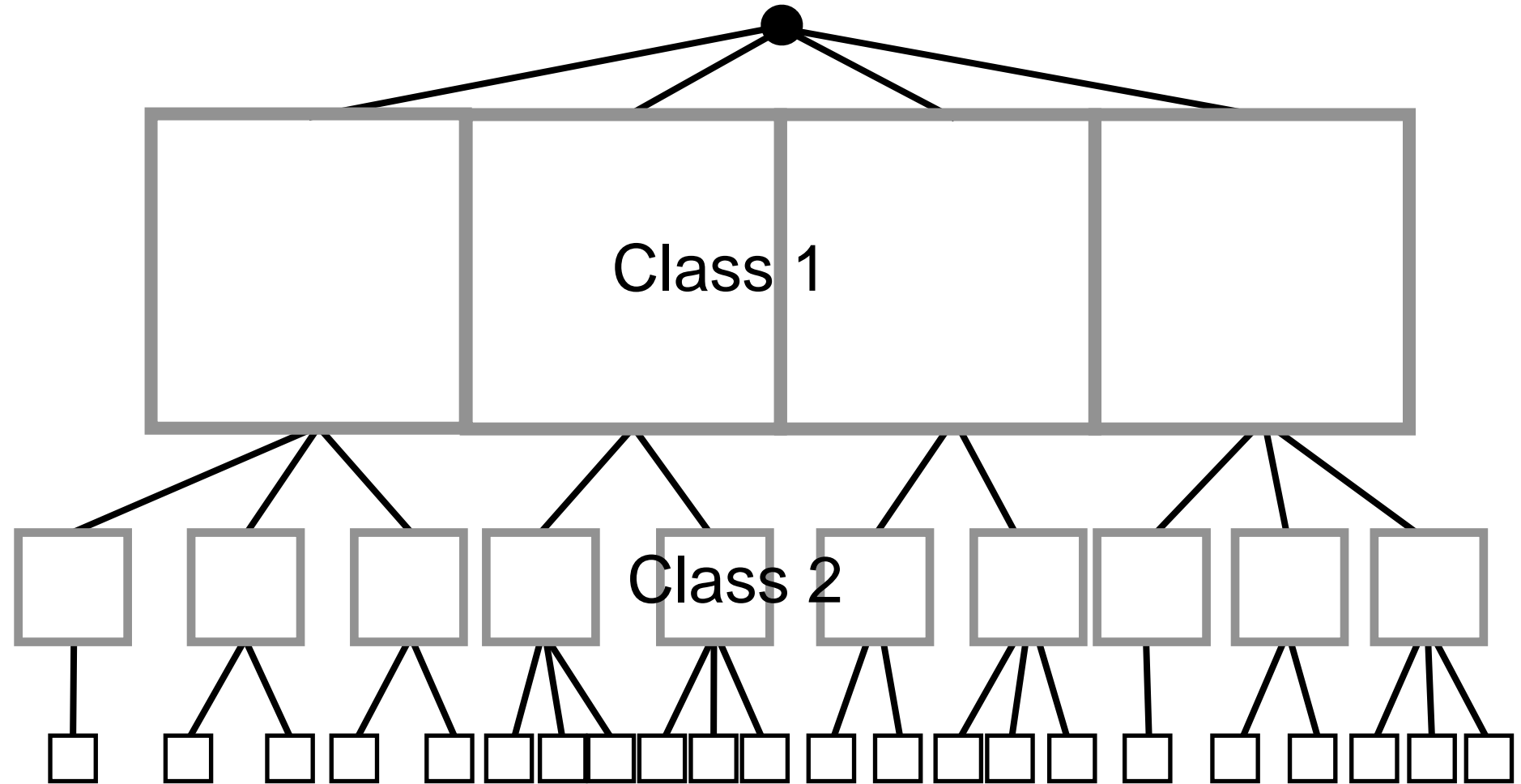
# Class-Uniform Path Analysis



# Class-Uniform Path Analysis

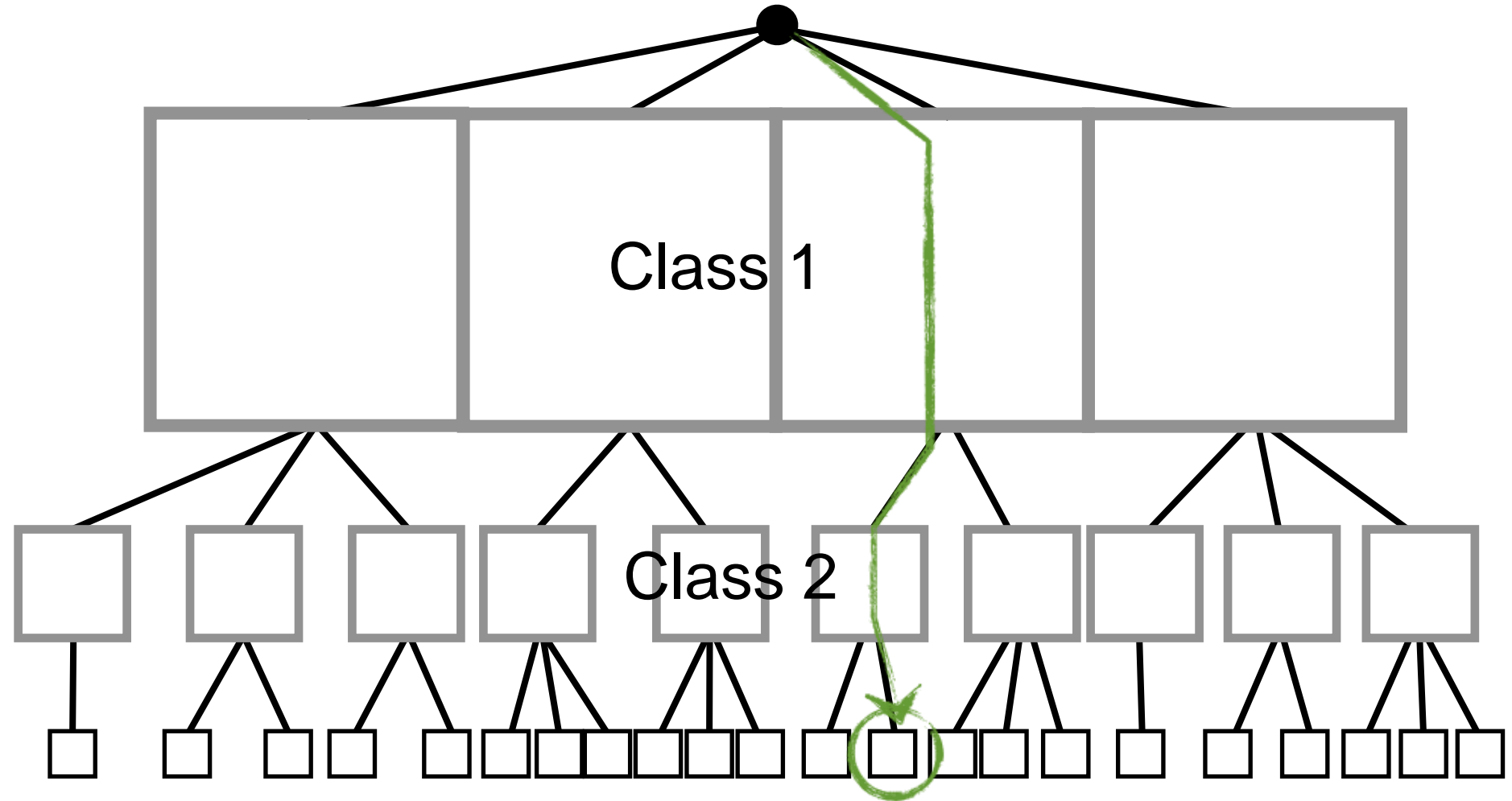


# Class-Uniform Path Analysis



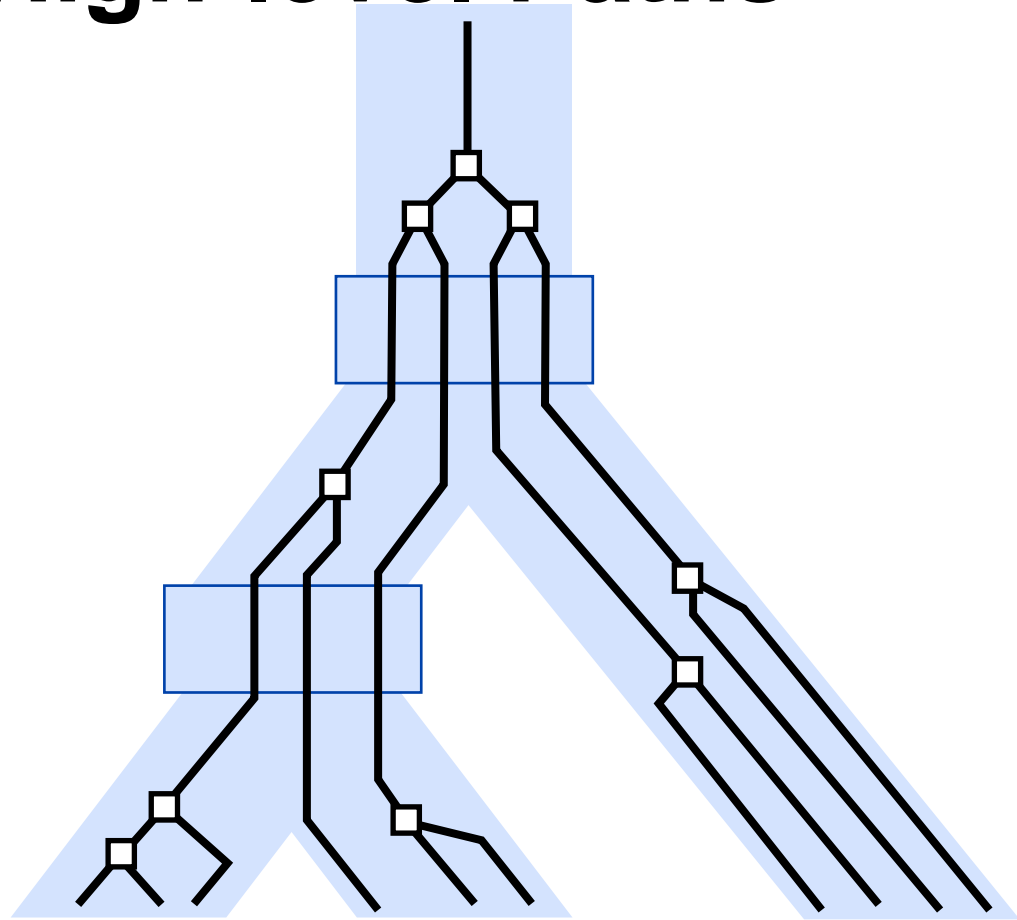
States arranged in a class hierarchy

# Class-Uniform Path Analysis



States arranged in a class hierarchy

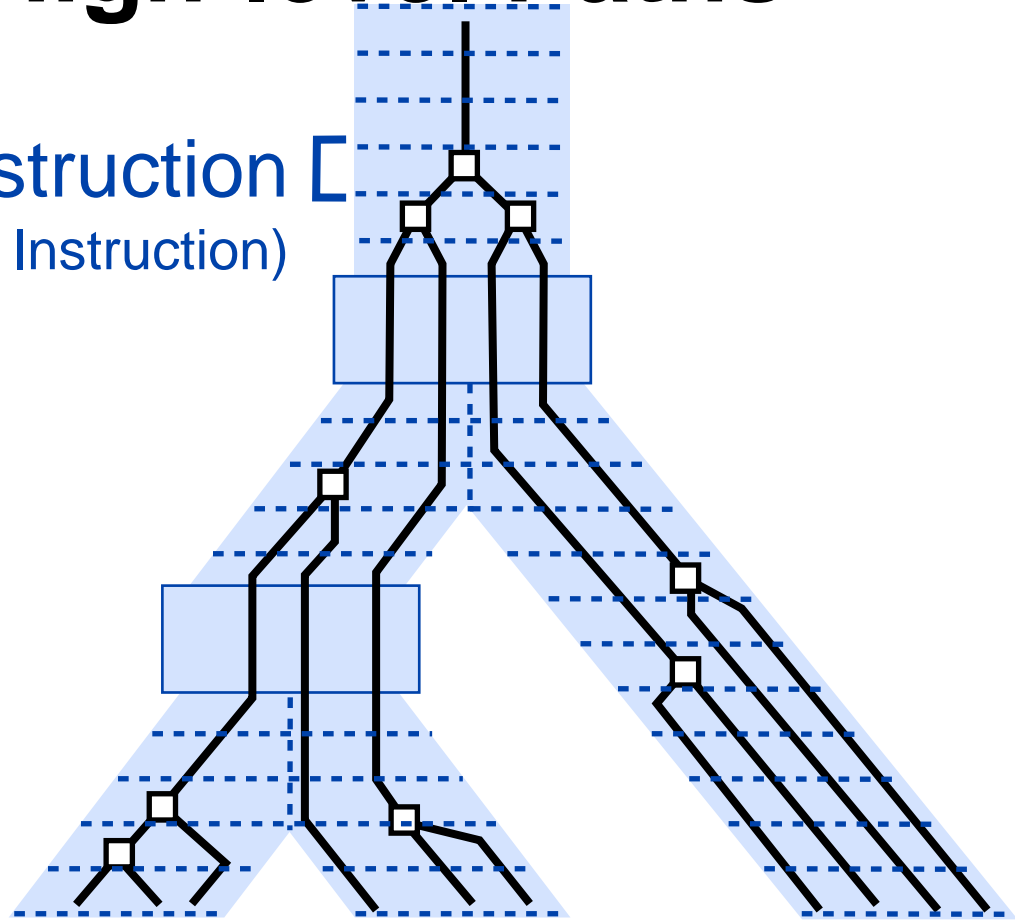
# Partitioning High-level Paths





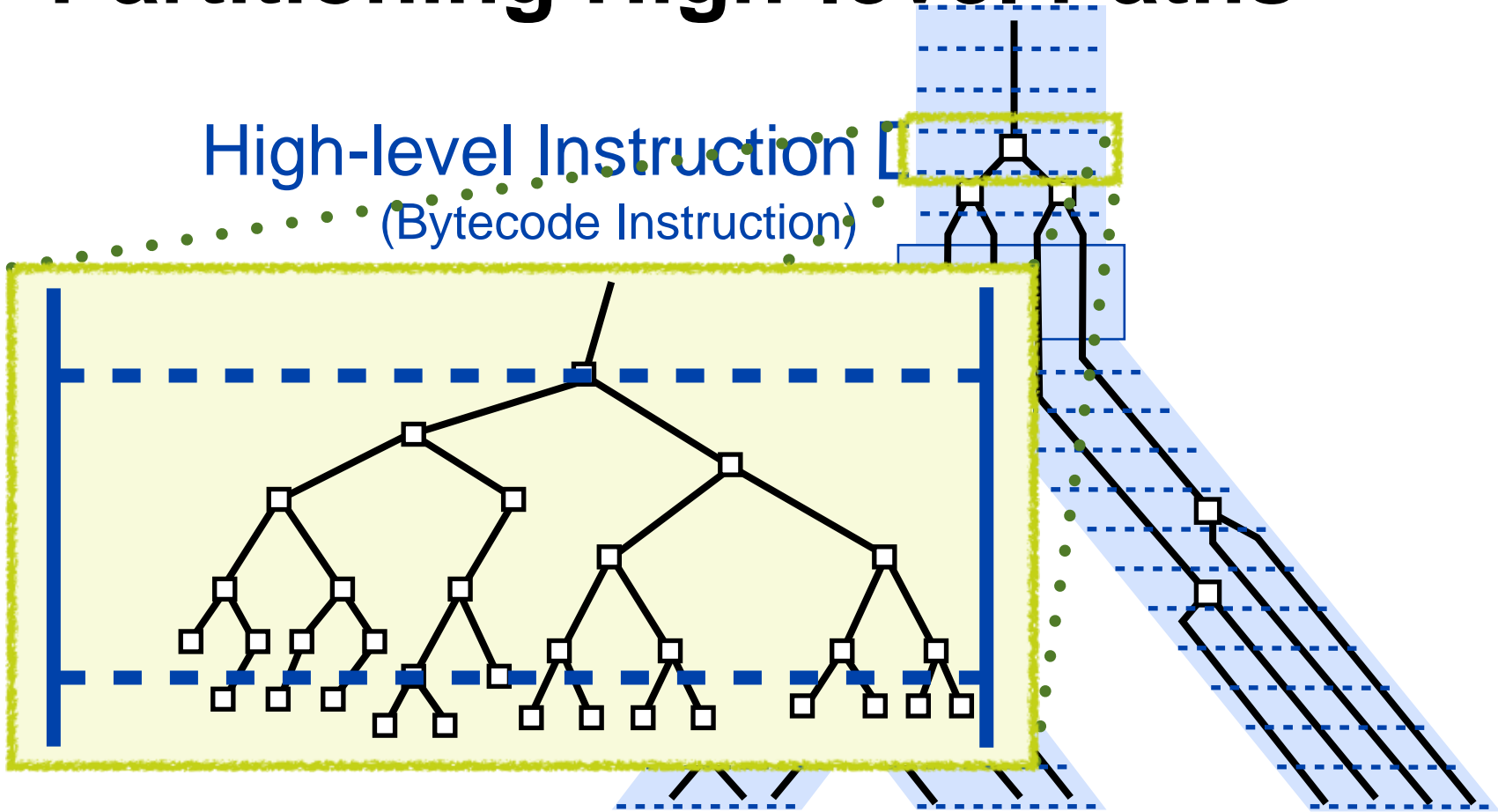
# Partitioning High-level Paths

High-level Instruction [ ]  
(Bytecode Instruction)

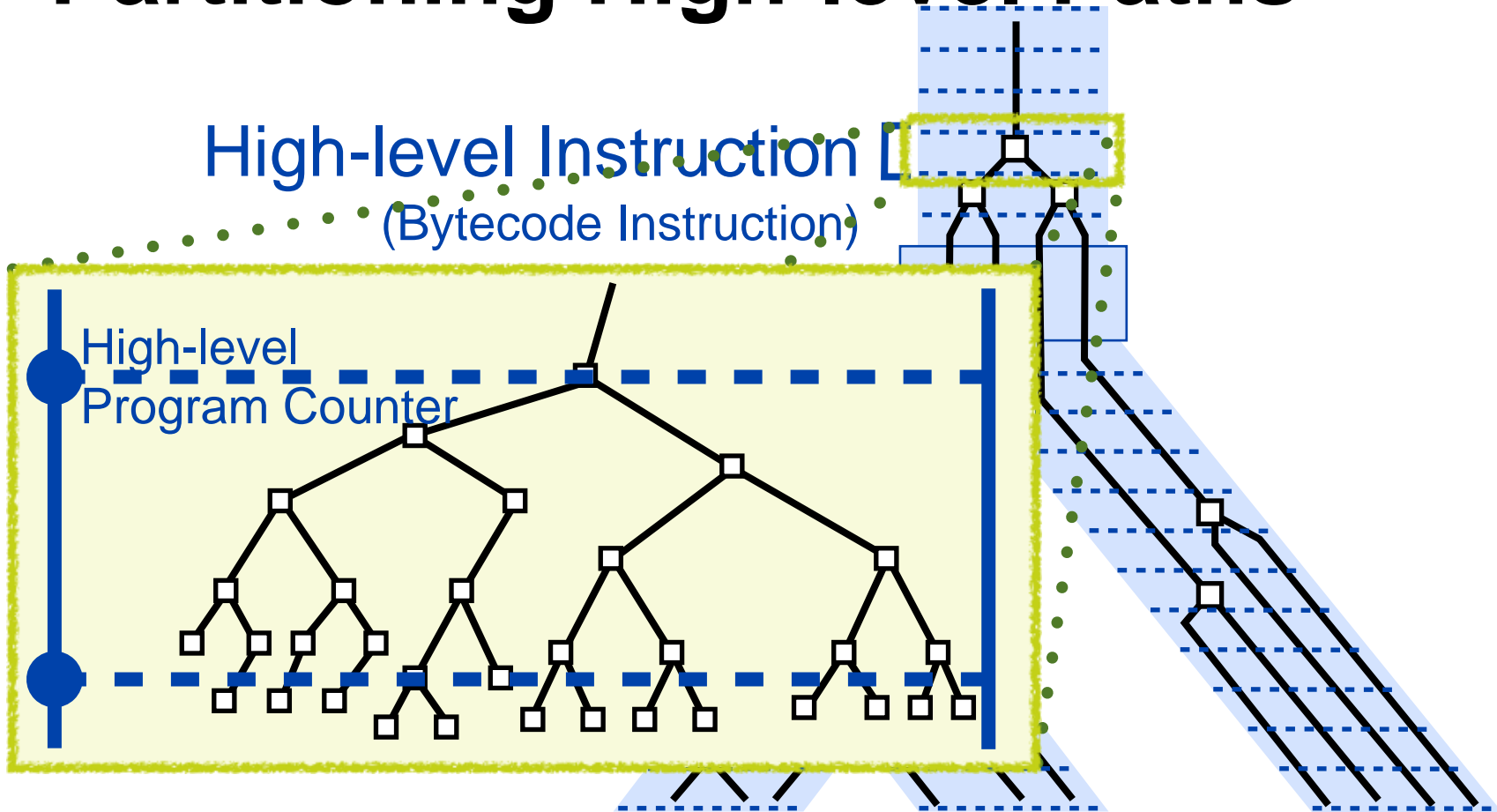


# Partitioning High-level Paths

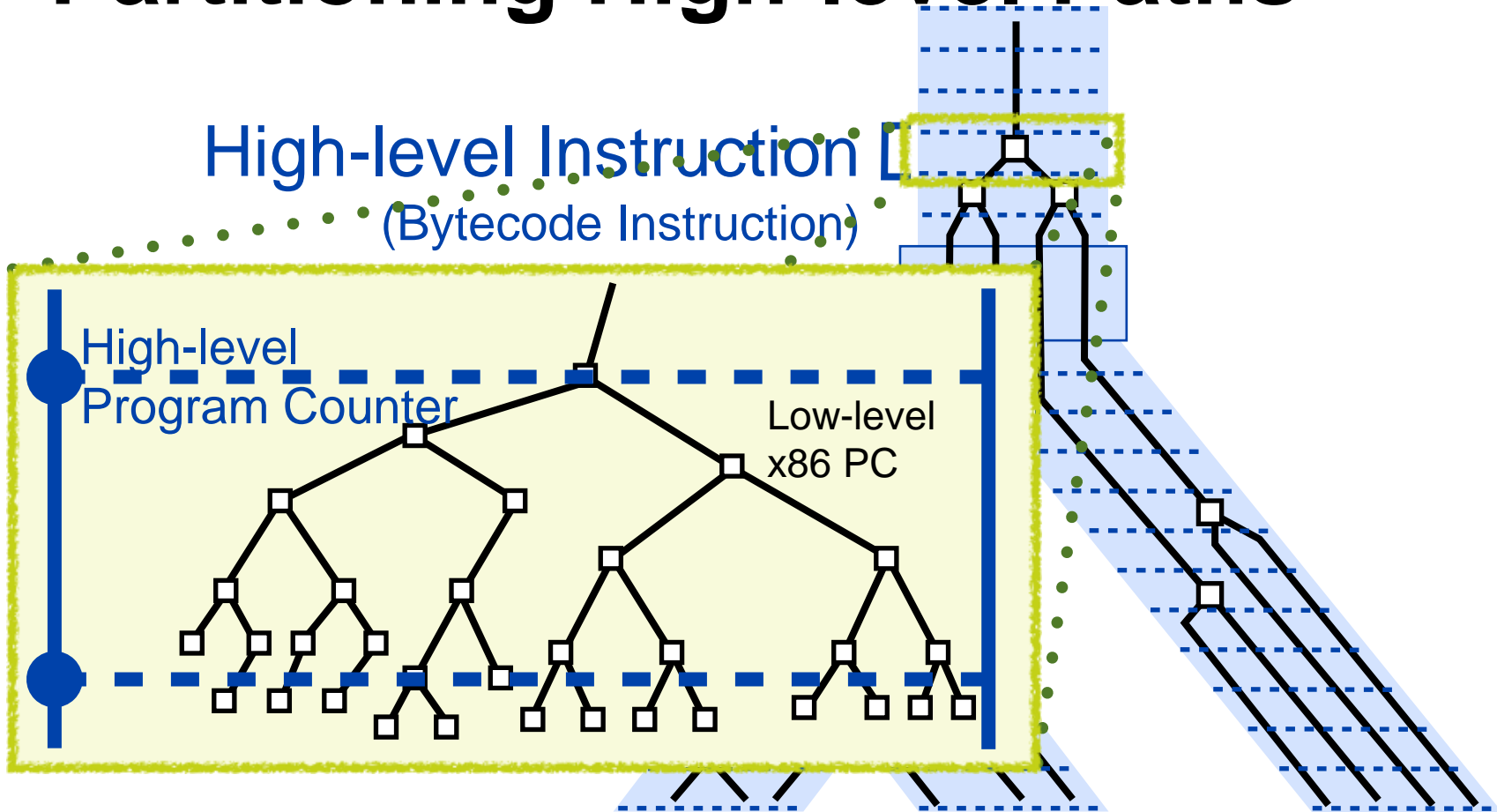
High-level Instruction [ ]  
(Bytecode Instruction)



# Partitioning High-level Paths



# Partitioning High-level Paths



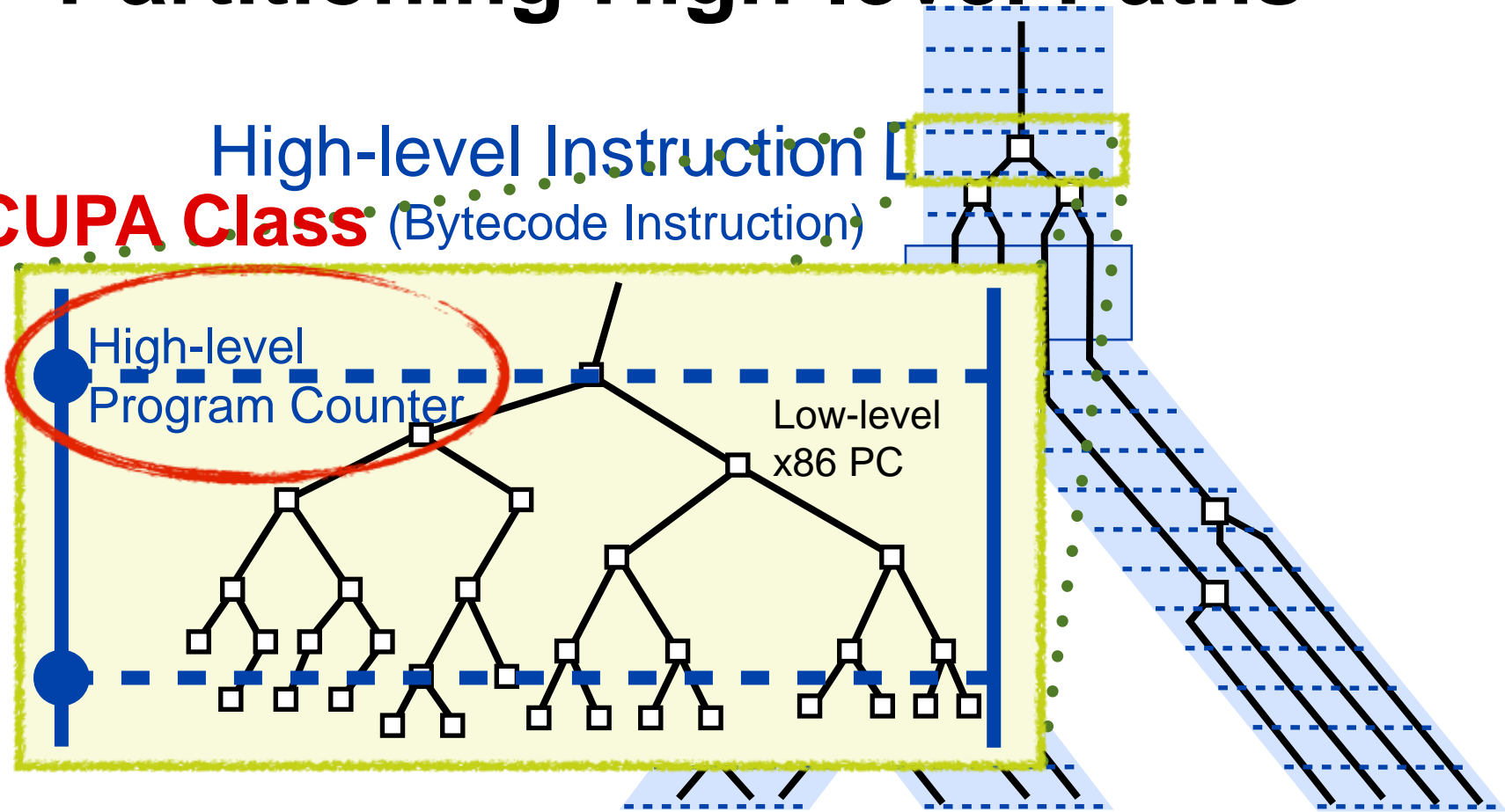
# Partitioning High-level Paths

High-level Instruction

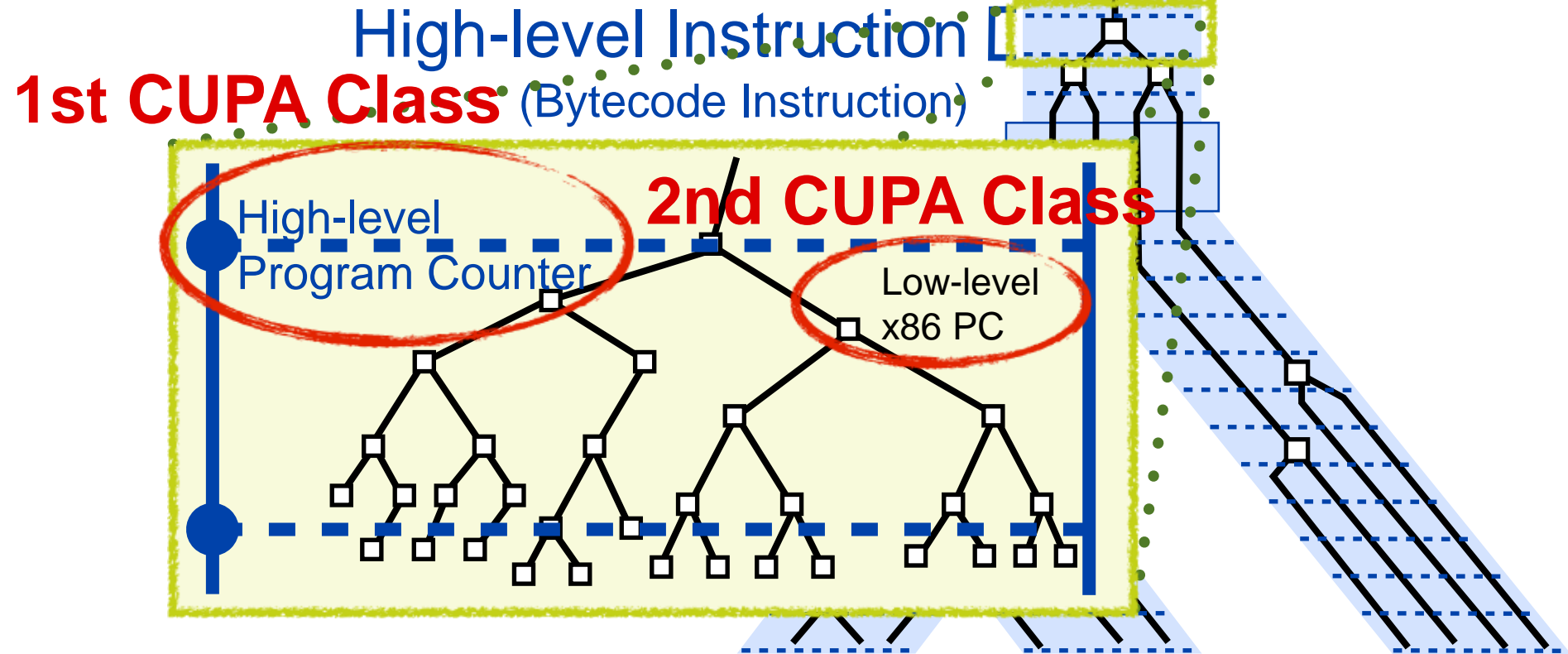
**1st CUPA Class** (Bytecode Instruction)

High-level  
Program Counter

Low-level  
x86 PC



# Partitioning High-level Paths



Reconstruct high-level execution tree

# CUPA Classes

## 1. High-level PC

- *Uniform HL instruction exploration*
- *Obtained via instrumentation*

## 2. x86 PC

- *Uniform native method exploration*
- *Approximated as the PC of fork point*

# Interpreter Loop Instrumentation

```
while (true) {
    fetch_instr(hlpc, &opcode, &params);
    switch (opcode) {
    case LOAD:
        ...
    case STORE:
        ...
    case CALL_FUNCTION:
        ...
        ...
    }
    hlpc++;
}
```



# Interpreter Loop Instrumentation

```
while (true) {
    fetch_instr(hlpc, &opcode, &params);
    chef_log_hlpc(hlpc, opcode);
    switch (opcode) {
    case LOAD:
        ...
    case STORE:
        ...
    case CALL_FUNCTION:
        ...
        ...
    }
    hlpc++;
}
```

} Reconstruct high-level execution tree and CFG

# Interpreter Optimizations

```
static long
string_hash(PyStringObject *a)
{
#ifdef SYMBEX_HASHES
    return 0;
#else
    register Py_ssize_t len;
    register unsigned char *p;
    register long x;

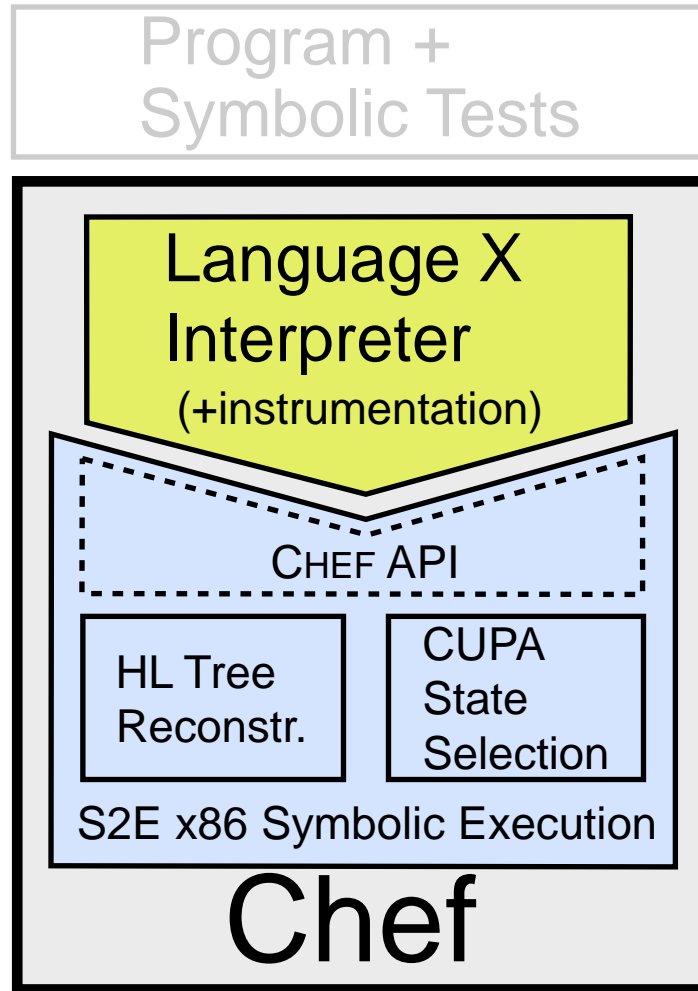
    len = Py_SIZE(a);

    p = (char *) a->ob_sval;
    x = _Py_HashSecret.prefix;
    x ^= *p << 7;
    while (--len >= 0)
        x = (1000003*x) ^ *p++;
    x ^= Py_SIZE(a);
    x ^= _Py_HashSecret.suffix;
    if (x == -1)
        x = -2;
    return x;
#endif
}
```

Hash neutralization

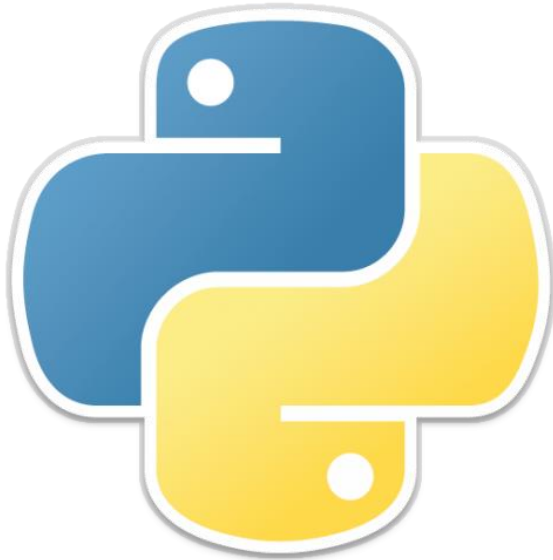
- Simple changes to interpreter source
- “Anti-optimizations” in linear performance...
- ... but exponential gains in symbolic mode

# Chef Summary



Symbolic Execution Engine for Language X

# Chef-Prototyped Engines



Python  
5 person-days  
321 LoC



Lua  
3 person-days  
277 LoC

# Testing Python Packages

6 Popular Packages

argparse

ConfigParser

HTMLParser

simplejson

unicodcsv

xlrd

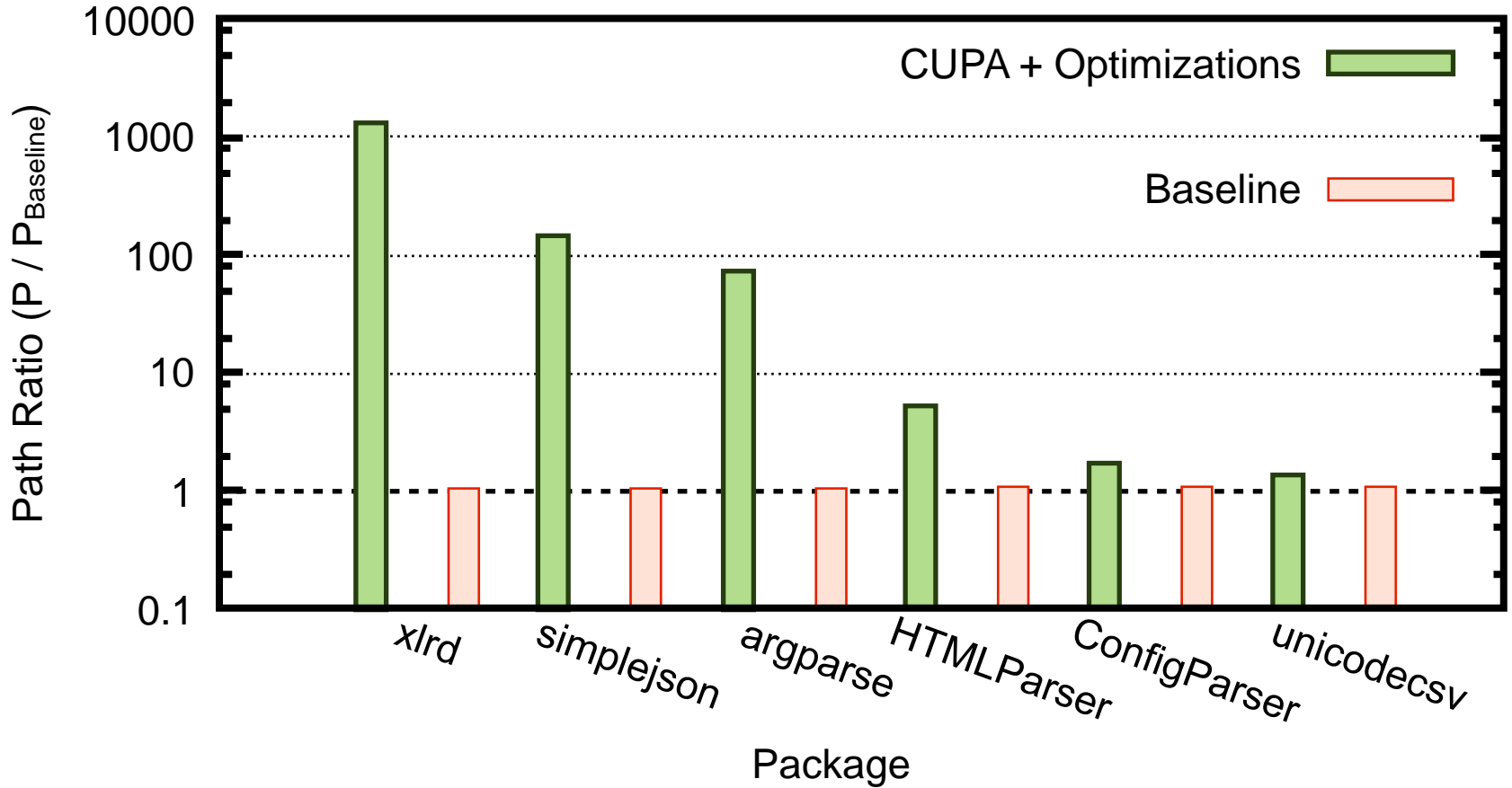
10.9K lines of Python code

30 min. / package

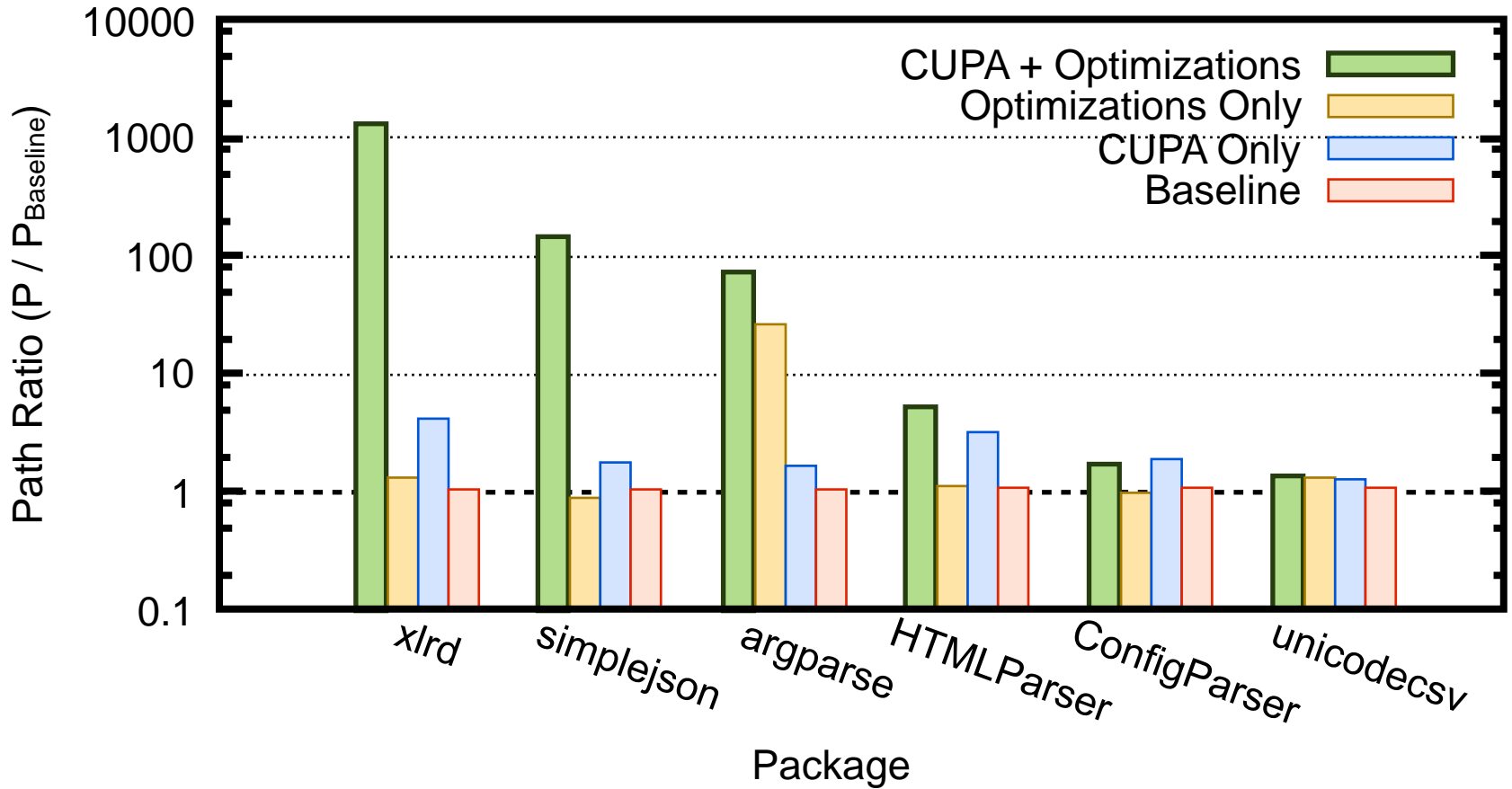
> 7,000 tests generated

4 undocumented exceptions found

# Efficiency



# Efficiency



# Symbolic Execution

- Path-wise under-approximate program analysis
  - *Mixes concrete and symbolic reasoning*
- Automatic test case-generation
- Major-challenge: path explosion
- Solutions:
  - *State merging*
  - *Domain-specific optimizations*
  - ...