A Tool for Simplifying ACL2 Definitions

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 - What the tool does
 - ► How the tool does it
 - ► Some challenges, wrinkles, bells, and whistles

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 - ... but the two tools don't share any code.
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I'll illustrate with examples. Feel free to ask questions!

WHAT THE TOOL DOES

Very simple running example for the first two sections of this talk:

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ACL2 !>(defun foo (x) (+ 1 1 x))
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FOO
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```
ACL2 !>(defun foo (x) (+ 1 1 x))

FOO

ACL2 !>(simplify-defun foo)
(DEFUN FOO$1 (X)

(DECLARE (XARGS : NORMALIZE NIL
:GUARD T
:VERIFY-GUARDS NIL))

(+ 2 X))

ACL2 !>
```

Next we explore the events generated by simplify-defun.

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We will focus mostly on how those events automate a proof that the original and simplified functions are equal.

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- ► Bird's-eye view of it all (not really readable!)
- Outline view, focusing attention on key sub-events
- Some details about key sub-events

BIRD'S-EYE VIEW OF IT ALL

```
ACL2 !>(show-simplify-defun foo)
 (PROGN
  (ENCAPSULATE NIL (SET-INHIBIT-WARNINGS "theory")
    (SET-IGNORE-OK T) (SET-IRRELEVANT-FORMALS-OK T)
    (LOCAL (INSTALL-NOT-NORMALIZED FOO))
    (DEFUN FOO$1 (X)
      (DECLARE (XARGS : NORMALIZE NIL : GUARD T : VERIFY-GUARDS NIL))
      (+2X)
    (LOCAL ; local proof details
      (DEFTHM FOO$1-BEFORE-VS-AFTER-0
                 (EQUAL (+ 1 1 X) (+ 2 X)))
        (EOUAL (FOO X) (FOO-COPY X))
        :HINTS (("Goal" :IN-THEORY '(FOO$NOT-NORMALIZED FOO-COPY-DEF)))
        :RULE-CLASSES NIL)
        (EOUAL (FOO X) (FOO$1 X))
    (DEFTHM FOO-BECOMES-FOO$1
      (EOUAL (FOO X) (FOO$1 X))
      :HINTS ...))
  (TABLE TRANSFORMATION-TABLE ...)
  (VALUE-TRIPLE '(DEFUN FOO$1 (X)
                    (DECLARE (XARGS : NORMALIZE NIL : GUARD T : VERIFY-GUARDS NIL))
                    (+ 2 X))))
ACT.2 !>
```

OUTLINE VIEW

```
(PROGN
 (ENCAPSULATE NIL
   ...; Preamble (set-ignore-ok etc.)
   (DEFUN FOO$1 (X); Simplified definition
     (DECLARE (XARGS ...))
     (+ 2 X))
   (LOCAL ; Proof of 'BECOMES' lemma
    (PROGN ...))
   (DEFTHM FOO-BECOMES-FOO$1; 'BECOMES'' lemma
     (EOUAL (FOO X) (FOO\$1 X))
    :HINTS ...))
```

OUTLINE VIEW

```
(PROGN
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   ...; Preamble (set-ignore-ok etc.)
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   (DEFTHM FOO-BECOMES-FOO$1; 'BECOMES'' lemma
     (EOUAL (FOO X) (FOO\$1 X))
     :HINTS ...)); We'll ignore the rest:
```

OUTLINE VIEW

```
(PROGN
 (ENCAPSULATE NIL
  ...; Preamble (set-ignore-ok etc.)
   (DEFUN FOO$1 (X); Simplified definition
     (DECLARE (XARGS ...))
     (+ 2 X)
   (LOCAL ; Proof of 'BECOMES' lemma
    (PROGN ...))
   (DEFTHM FOO-BECOMES-FOO$1; 'BECOMES'' lemma
     (EOUAL (FOO X) (FOO\$1 X))
    :HINTS ...)); We'll ignore the rest:
 (TABLE TRANSFORMATION-TABLE
        ...); For database (e.g., redundancy)
 (VALUE-TRIPLE; Value returned in the loop
 '(DEFUN FOO$1 (X) (DECLARE (XARGS ...)) (+ 2 X)))
```

PREAMBLE

```
(SET-INHIBIT-WARNINGS "theory")
(SET-IGNORE-OK T)
(SET-IRRELEVANT-FORMALS-OK T)
(LOCAL (INSTALL-NOT-NORMALIZED FOO))
(DEFUN FOO$1 (X); Simplified definition
  (DECLARE (XARGS ...))
  (+ 2 X)
(LOCAL ; Proof of 'BECOMES' lemma
 (PROGN ...))
(DEFTHM FOO-BECOMES-FOO$1; 'BECOMES'' lemma
  (EOUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

SIMPLIFIED DEFINITION

The expander (books/misc/expander.lisp) provides our interface to the rewriter, to simplify the definition.

```
...; Preamble (set-ignore-ok etc.)
(DEFUN FOO$1 (X); Simplified definition
  (DECLARE (XARGS : NORMALIZE NIL
                  :GUARD T
                  :VERIFY-GUARDS NIL))
 (+ 2 X)
(LOCAL ; Proof of 'BECOMES' lemma
 (PROGN ...))
(DEFTHM FOO-BECOMES-FOO$1; 'BECOMES'' lemma
  (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

"BECOMES" LEMMA

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```
...; Preamble (set-ignore-ok etc.)
(DEFUN FOO$1 (X); Simplified definition
  (DECLARE (XARGS ...))
  (+ 2 X)
(LOCAL ; Proof of 'BECOMES' lemma
 (PROGN of_of_becomes-lemma>))
(DEFTHM FOO-BECOMES-FOO$1; redundant
  (EOUAL (FOO X) (FOO \$1 X))
  :HINTS ...))
Let's look at comes-lemma>.
```

PROOF OF "BECOMES" LEMMA (1): OVERVIEW

```
(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
 (IMPLIES (AND)
           (EQUAL (+ 1 1 X) (+ 2 X)))
 :HINTS ... :RULE-CLASSES NIL)
(ENCAPSULATE (((FOO-COPY *) => *))
  (LOCAL (DEFUN FOO-COPY (X)
           (DECLARE (XARGS : NORMALIZE NIL))
           (FOO X)))
  (DEFTHM FOO-COPY-DEF
    (EOUAL (FOO-COPY X)
           (BINARY-+ '1 (BINARY-+ '1 X)))
   :HINTS ... :RULE-CLASSES ...))
(DEFTHM FOO-IS-FOO-COPY
 (EQUAL (FOO X) (FOO-COPY X))
 :HINTS :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
 (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

PROOF OF "BECOMES" LEMMA (2)

```
(DEFCONST *FOO-RUNES*
 '((:REWRITE FOLD-CONSTS-IN-+)
    (:EXECUTABLE-COUNTERPART BINARY-+)
    (:DEFINITION SYNP)))
(DEFTHM FOO$1-BEFORE-VS-AFTER-0 ...)
(ENCAPSULATE (((FOO-COPY *) => *))
  (LOCAL ...)
  (DEFTHM FOO-COPY-DEF ...))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X))
  :HINTS :: RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

PROOF OF "BECOMES" LEMMA (3)

```
(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
  (IMPLIES (AND)
           (EOUAL (+ 1 1 X) (+ 2 X)))
 :HINTS
   (("Goal" :IN-THEORY *FOO-RUNES* :EXPAND NIL))
 :RULE-CLASSES NIL)
(ENCAPSULATE (((FOO-COPY *) => *))
  (LOCAL ...)
  (DEFTHM FOO-COPY-DEF ...))
(DEFTHM FOO-IS-FOO-COPY
  (EOUAL (FOO X) (FOO-COPY X))
 :HINTS ... :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

PROOF OF "BECOMES" LEMMA (4)

```
(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
        ... (EQUAL (+ 1 1 X) (+ 2 X)) ...)
(ENCAPSULATE (((FOO-COPY \star) => \star))
 (LOCAL (DEFUN FOO-COPY (X)
           (DECLARE (XARGS : NORMALIZE NIL))
           (FOO X)))
  (DEFTHM FOO-COPY-DEF
   (EOUAL (FOO-COPY X)
           (BINARY-+ '1 (BINARY-+ '1 X)))
   :HINTS (("Goal"
             :IN-THEORY '((:D FOO-COPY))
             :EXPAND ((FOO X)))
   :RULE-CLASSES ((:DEFINITION :INSTALL-BODY T))))
(DEFTHM FOO-IS-FOO-COPY
  (EOUAL (FOO X) (FOO-COPY X))
 :HINTS :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
 (EOUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

PROOF OF "BECOMES" LEMMA (5)

```
(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
        ... (EQUAL (+ 1 1 X) (+ 2 X)) ...)
(ENCAPSULATE (((FOO-COPY \star) => \star))
  (LOCAL (DEFUN FOO-COPY (X) ...))
  (DEFTHM FOO-COPY-DEF
    (EOUAL (FOO-COPY X)
           (BINARY-+ '1 (BINARY-+ '1 X)))
    :HINTS ... :RULE-CLASSES ...))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X))
 :HINTS (("Goal" :IN-THEORY
           '(FOO$NOT-NORMALIZED FOO-COPY-DEF)))
 :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)
```

PROOF OF "BECOMES" LEMMA (6)

```
(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
       ... (EQUAL (+ 1 1 X) (+ 2 X)) ...)
(ENCAPSULATE (((FOO-COPY \star) => \star))
 (LOCAL (DEFUN FOO-COPY (X) ...))
 (DEFTHM FOO-COPY-DEF
   (EOUAL (FOO-COPY X)
          (BINARY-+ '1 (BINARY-+ '1 X))) ...))
(DEFTHM FOO-IS-FOO-COPY
 (EOUAL (FOO X) (FOO-COPY X)) ...)
(DEFTHM FOO-BECOMES-FOO$1
  (EOUAL (FOO X) (FOO \$1 X))
  · HINTS
  (("Goal" ; Avoid induction in recursive case
    :BY (:FUNCTIONAL-INSTANCE FOO-IS-FOO-COPY
                                   (FOO-COPY FOO$1))
    :IN-THEORY (THEORY 'MINIMAL-THEORY))
   '(:USE (FOO$1-BEFORE-VS-AFTER-0 FOO$1))))
```

PROOF OF "BECOMES" LEMMA (7)

The value of functional instantiation is more clear for a recursive definition. Given

```
(defun bar (x)
  (if (zp x)
    (+ 1 1 (bar (+ -1 x))))
— we generate:
(DEFTHM BAR-BECOMES-BAR$1
  (EOUAL (BAR X) (BAR$1 X))
  :HINTS
  (("Goal"
    :BY (:FUNCTIONAL-INSTANCE BAR-IS-BAR-COPY
                                (BAR-COPY BAR$1))
    :IN-THEORY (THEORY 'MINIMAL-THEORY))
   '(:USE (BAR$1-BEFORE-VS-AFTER-0 BAR$1))))
```

PROOF OF "BECOMES" LEMMA (8)

The :by hint works, so the proof proceeds as follows.

Goal' : bar\$1 satisfies the definition of bar-copy

```
(EOUAL (BAR$1 X)
       (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X)))).
We augment the goal with the hypotheses provided by the : USE hint.
These hypotheses can be obtained from BAR$1-BEFORE-VS-AFTER-0 and
BAR$1. We are left with the following subgoal.
Goal''
(IMPLIES
 (AND (IMPLIES : use bar$1-before-vs-after-0
       (EOUAL (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X))))
              (IF (ZP X) 0 (+ 2 (BAR$1 (+ -1 X)))))
      (EOUAL (BAR$1 X) ; use bar$1
             (IF (ZP X) 0 (+ 2 (BAR$1 (+ -1 X)))))
 (EOUAL (BAR$1 X)
        (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X))))).
```

But we reduce the conjecture to T, by primitive type reasoning.

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SOME SOME CHALLENGES, WRINKLES, BELLS, AND WHISTLES

Next we look at a few interesting aspects of simplify-defun. We'll do the following.

- ► Consider some challenges and how they were overcome.
- ▶ Skim the documentation.
- ► Look at some of the many knobs to turn.

Let's start by looking at some challenges and their solutions.

New general features developed for MUSE are in color.

prove termination	appeal to previous function's <i>unnor-malized</i> body (install-not-normalized) and :termination-theorem
verify guards	appeal to the previous function's :guard-theorem
support	require a proof that assumptions are
assumptions	preserved on recursive calls
preserve structure	use directed-untranslate
use context	simplify and <i>flatten</i> assumptions and
	governing IF tests
suppress output	turn off warnings; return and print
	only the new definition
ease debugging	show-simplify-defun, :verbose t
control	patterns, hints,
support redundancy	use a table
automate reasoning	functional instantiation, theories,

DOCUMENTATION

Let's skim the documentation.

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Now we focus our attention on some of the many knobs to turn.

```
REUSE FOR GUARDS, MEASURES, AND THEIR PROOFS
   ACL2 !> (defun bar (x)
            (declare (xargs :quard (natp x)))
            (if (zp x) 0 (+ 1 1 (bar (+ -1 x))))
   ACL2 !>(simplify-defun bar)
    (DEFUN BAR$1 (X)
      (DECLARE
       (XARGS
        :NORMALIZE NIL
        :GUARD (NATP X)
```

(("Goal" : USE (:GUARD-THEOREM BAR)))

(IF (ZP X) 0 (+ 2 (BAR\$1 (+ -1 X))))

(("Goal": USE (:TERMINATION-THEOREM BAR)))))

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:MEASURE (ACL2-COUNT X)

:VERIFY-GUARDS T :GUARD-HINTS

:HINTS

SIMPLIFYING UNDER ASSUMPTIONS (1)

```
ACL2 !> (defun f (x)
          (declare (xargs :guard (true-listp x)))
          (if (consp x)
              (f(cdr x))
            \times))
ACL2 !>(simplify-defun f :assumptions :quard)
 (DEFUN F$1 (X)
         (DECLARE (XARGS ...))
         (IF (CONSP X) (F$1 (CDR X)) NIL))
ACL2 !>
```

SIMPLIFYING UNDER ASSUMPTIONS (1)

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ACL2 !>(simplify-defun f :assumptions :quard)
 (DEFUN F$1 (X)
         (DECLARE (XARGS ...))
         (IF (CONSP X) (F$1 (CDR X)) NIL))
ACL2 !>
```

Note that we get the same result from the following; the use of :assumptions :guard is just a handy shortcut.

```
(simplify-defun f :assumptions '((true-listp x)))
```

SIMPLIFYING UNDER ASSUMPTIONS (2)

The generated events are a bit more complicated when the keyword :assumptions is provided.

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OBTAINING PRETTY RESULTS

We use

```
books/kestrel/system/directed-untranslate.lisp:
ACL2 !>(defun f3 (x y)
  (implies (car (cons x x)) (not y)))
...
ACL2 !>
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ACL2 !>(defun f3 (x y)
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...
ACL2 !>(trace$ directed-untranslate)
  ((DIRECTED-UNTRANSLATE))
ACL2 !>
```

OBTAINING PRETTY RESULTS

ACT₁2 !>

```
We use
books/kestrel/system/directed-untranslate.lisp:
ACL2 !> (defun f3 (x y)
 (implies (car (cons x x)) (not y)))
ACL2 !>(trace$ directed-untranslate)
 ((DIRECTED-UNTRANSLATE))
ACL2 !>(simplify-defun f3)
1> (DIRECTED-UNTRANSLATE (IMPLIES (CAR (CONS X X))
                           (IMPLIES (CAR (CONS X X))
                           (IF X (IF Y 'NIL 'T) 'T)
                          NIL |current-acl2-world|)
<1 (DIRECTED-UNTRANSLATE</pre>
                          (IMPLIES X (NOT Y)))
 (DEFUN F3$1 (X Y)
         (DECLARE (XARGS ...))
         (IMPLIES X (NOT Y)))
```

SIMPLIFYING SUBTERMS

```
ACL2 !> (defun h (x)

(list (+ 1 1 x)

(and (integerp x) (+ 2 -2 x))

(+ 3 -3 x)

(+ 4 4 x)))

...
ACL2 !>
```

SIMPLIFYING SUBTERMS

```
ACL2 !> (defun h (x)
          (list (+ 1 1 x)
                 (and (integerp x) (+ 2 - 2 x))
                 (+ 3 -3 x)
                 (+ 4 4 x))
ACL2 !>(simplify-defun h
                          :simplify-body
                          (list @ (and _ @) @ _))
 (DEFUN H$1 (X)
         (DECLARE (XARGS ...))
         (LIST (+ 2 X)
                (AND (INTEGERP X) X)
                (IF (ACL2-NUMBERP X) X 0)
                (+ 4 4 X))
ACT<sub>1</sub>2 !>
```

ADDITIONAL OPTIONS FOR:

- hints, including theory control
- specifying the new function name
- providing a measure
- specifying enable status for resulting events
- ► simplifying the measure and/or guard
- controlling guard verification
- untranslating in full (instead of using directed-untranslate)

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More options may come; demand-driven!

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- specifying the new function name
- providing a measure
- specifying enable status for resulting events
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More options may come; **demand-driven!**Not discussed here, but analogous: simplify-defun-sk.

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Additional enhancements are planned, including support for mutual recursion and for transforming a non-recursive function to a recursive function.

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Its implementation (another talk?) may give clues on how to write other tools that manipulate ACL2 events.

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Additional enhancements are planned, including support for mutual recursion and for transforming a non-recursive function to a recursive function.

Its implementation (another talk?) may give clues on how to write other tools that manipulate ACL2 events.

I'm hoping that simplify-defun will be made publicly available.