## CS378

# Autonomous Multiagent Systems Spring 2004 

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The University of Texas at Austin
Week 13a: Tuesday, April 20th

## Good Afternoon, Colleagues

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- What if agents and humans act together?
- Is it irrational to be a participant in a common value auction?
- Are representative voting systems better?
- What's the best voting system?


## Logistics

- Final tournament: Thursday, May 13th, 10:30am, ACES 6.304


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- Next week's readings


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Not all possible!

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- A pairwise method
- Smith set: smallest set of candidates such that each candidate in the set preferred over each candidate not in the set
- Every candidate in the Smith set is relevant


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- 40: $\mathrm{B}>\mathrm{C}>\mathrm{A}$
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- Does that solve everything? What about cycles?


## Class Discussion

## Arpan Sura on voting systems

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Producers: production possibility sets
Variables: prices on goods

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- Braess' paradox


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- Two people bargaining, each with a preference over outcomes $O$
- Let $o^{*}$ be the selected outcome
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- One person makes offer o
- Other rejects with probaility $p(o)$ - based on offer
- If rejects, both get nothing


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- Contingencies
- Leveled commitment (price)
- Coalitions
- Formation
- Optimization within
- Payoff division


## DRDM Summary

For many agents: voting, general equilibrium, auctions
For fewer agents: auctions, contract nets, bargaining
Possible in all: coalitions

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## All self-interested, rational agents

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## So decided to auction

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- Efficient allocation (assign to whom it's worth the most)
- Promote deployment of new technologies
- Prevent monopoly (or close)
- Get some licenses to designated companies
- No political embarrassments


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Revenue an afterthought (but important in end)

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- How much information public?

