
CS345H: Programming Languages

Lecture 6: Parsing Algorithms

Thomas Dillig

Outline

- ▶ Extend CFGs to build parse trees

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- ▶ We will build a parser that recognizes a CFG

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- ▶ Error recovery

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Extending CFGs for program parsing

- ▶ CFGs describe the structure of a program.
- ▶ But we also need this structure in form of a tree, not just a yes/no answer
- ▶ **Insight:** We do not need all program structure, only the relevant part
- ▶ We call this an **abstract syntax tree**

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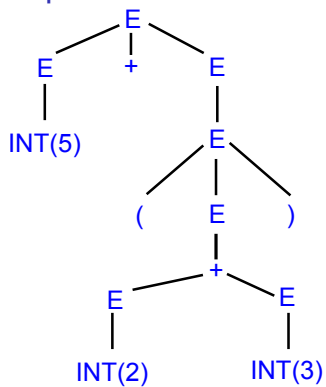
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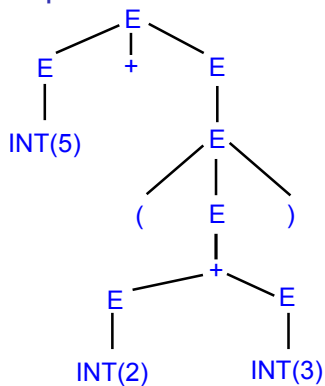
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- ▶ After lexical analysis as string of tokens:
INT(5) '+' '(' INT(2) '+' INT(3) ')'
- ▶ During parsing, we built a parse tree:

Example of Parse Tree

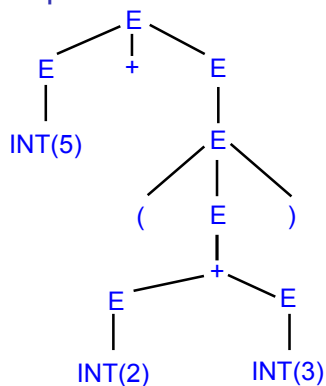


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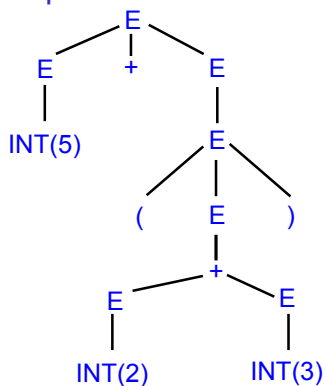
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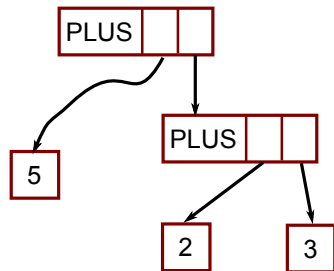
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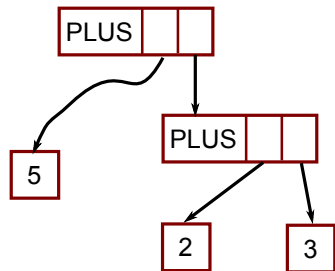


- ▶ Captures the nesting structure
- ▶ But **too much information!**
- ▶ **Example:** We do not care about the parentheses

Example of Abstract Syntax Tree

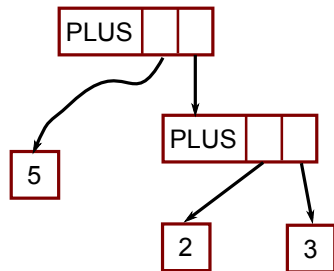


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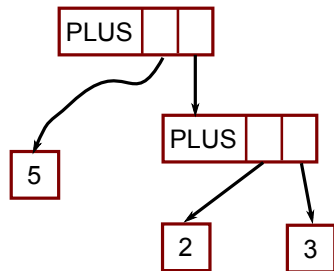
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- ▶ Also captures the nesting structure
- ▶ But **abstracts** from the concrete syntax
- ▶ More compact and easier to use

Semantic Actions to built the AST

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- ▶ Each production has a action computing its resulting attribute
- ▶ Written as: $X \rightarrow Y_1 \dots Y_n \{\text{action}\}$

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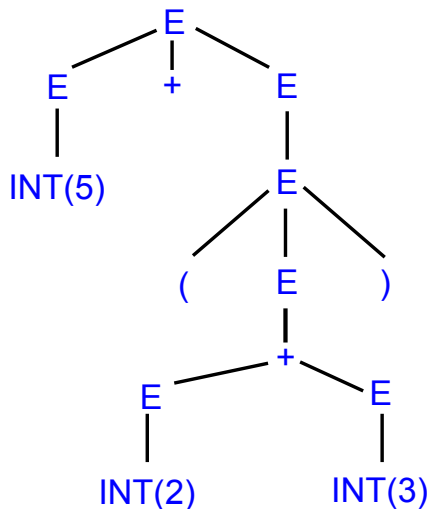
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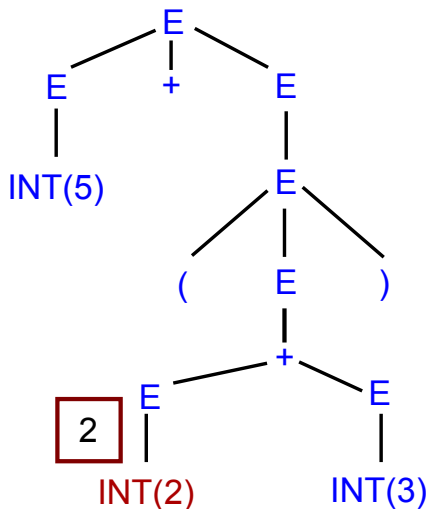
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- ▶ **Question:** What order do we need to evaluate these equations to compute a solution?
- ▶ **Answer:** Bottom-up

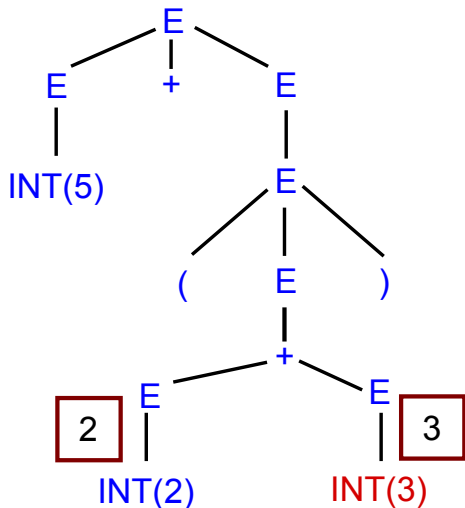
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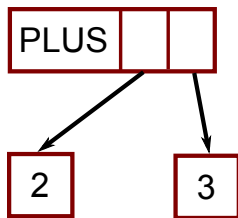
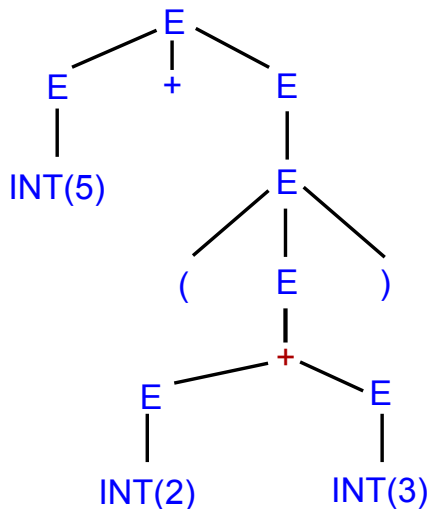
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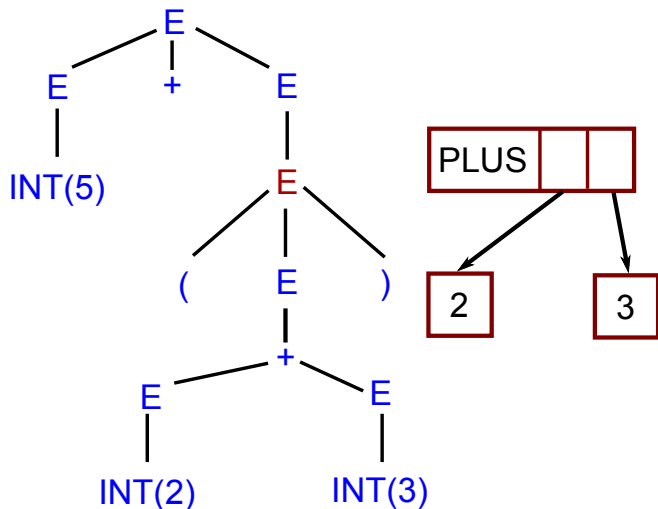
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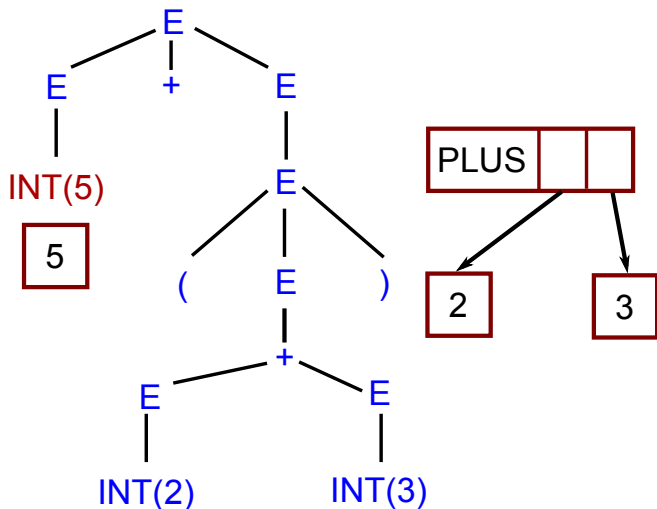
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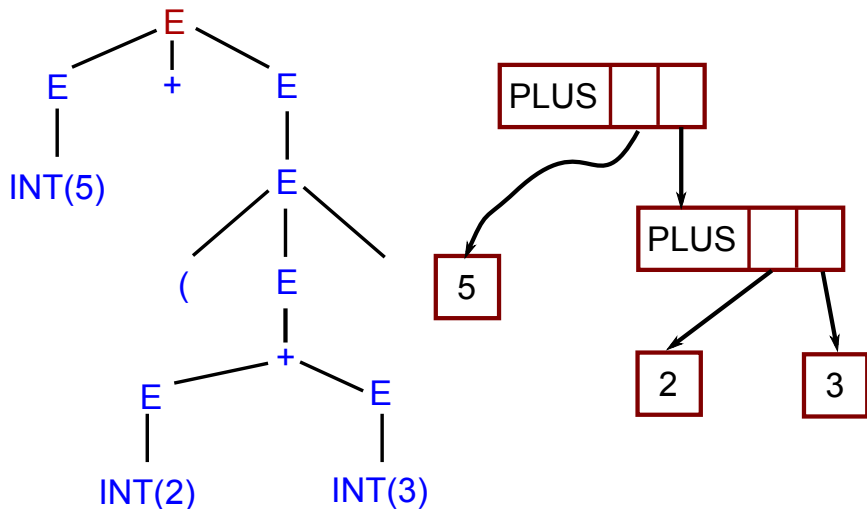
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Semantic Actions

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- ▶ **Next:** How to build the parser that will allow us to execute these semantic actions

Parsing

- ▶ Consider the non-ambiguous grammar for simple arithmetic expressions:

$$\begin{aligned} S &\rightarrow E \mid E + S \\ E &\rightarrow \text{int} \mid \text{int} * E \mid (S) \end{aligned}$$

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- ▶ **Idea:** Start with start symbol S and try rules for S in order, backtrack if we made the wrong choice

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S

(INT5)



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Mismatch! (is not INT
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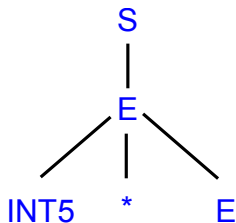
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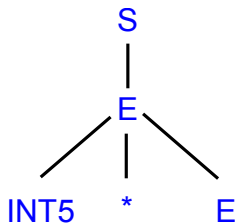


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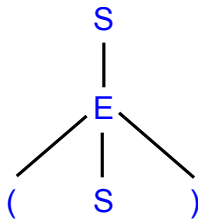
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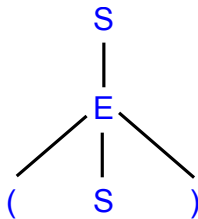


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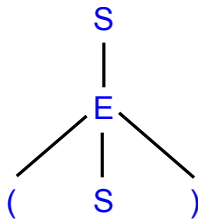
(INT5)



Match! Advance input

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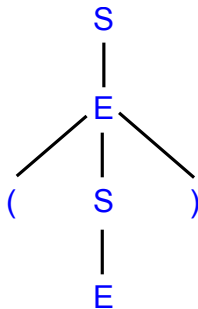


(INT5)



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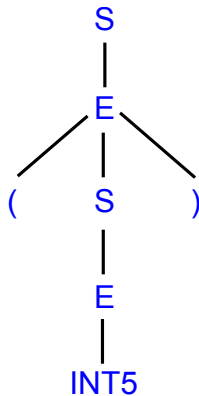
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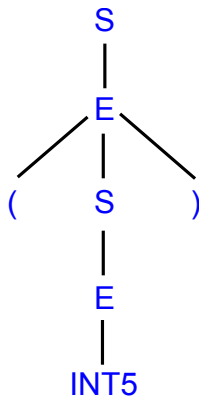


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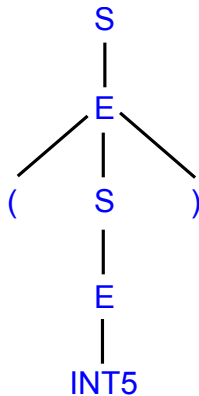


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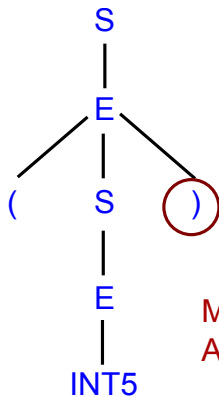
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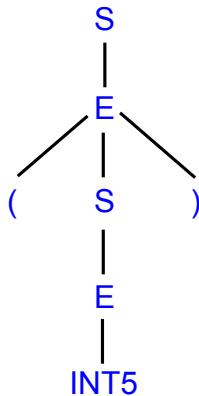


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Match!
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Parsing

$$S \rightarrow E \mid E + S$$
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Successful parse

(INT5)



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- ▶ It is easy to automate this strategy: For this assume:
 - ▶ `TOKEN` is the type of tokens
 - ▶ `next` is global pointer to array of `TOKEN`'s

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 - ▶ For the n 'th production of a non-terminal S , we will define
`bool S_n() { ... }`
 - ▶ To try all productions of a non-terminal S , we will define
`bool S() { ... }`

Recursive Descent Parsing 2

- ▶ For production $S \rightarrow E$
 `bool S_1() { return E(); }`

Recursive Descent Parsing 2

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- ▶ For all production S (with backtracking)
`bool S() {
 TOKEN* save = next;
 if(S_1() == true) return true;
 next = save;
 return S_2(); }`

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bool S() {  
    TOKEN* save = next;  
    if(S_1() == true) return true;  
    next = save;  
    return S_2(); }
```

- ▶ Or, equivalently written as

```
bool S() {  
    return ((next = save, S_1())  
           || ((next = save, S_2())) }
```


Recursive Descent Parsing 3

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bool E_2() { return TERM(INT) &&  
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```
bool E_3() { return TERM(LPAREN) && S() &&  
    TERM(RPAREN) }
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Recursive Descent Parsing 3

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bool E_2() { return TERM(INT) &&
    term(TIMES) && T(); }
bool E_3() { return TERM(LPAREN) && S() &&
    TERM(RPAREN) }
```

- ▶ For all productions in E , again with backtracking:

```
bool E() {
    TOKEN* save = next;
    return (next = save, E_1()) ||
        (next = save, E_2()) ||
        (next = save, E_3())
}
```

Complete Parser

```
bool term(TOKEN tok) { return token == *next++;}

bool S_1() { return E(); }
bool S_2() { return E() && term(PLUS) && S(); }
bool S() { return ((next = save, S_1())
    || ((next = save, S_2()) }

bool E_1() { return TERM(INT); }
bool E_2() { return TERM(INT) &&
    term(TIMES) && T(); }
bool E_3() { return TERM(LPAREN) && S() &&
    TERM(RPAREN) }
bool E() {
    TOKEN* save = next;
    return (next = save, E_1()) ||
        (next = save, E_2()) ||
        (next = save, E_3())
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- ▶ This simulates the example parse and is easy to implement by hand

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- ▶ Such grammars are called [left-recursive](#)

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- ▶ Easy to generalize this procedure slightly for non-direct left-recursion, such as

$$\begin{aligned} S &\rightarrow A\alpha \\ A &\rightarrow S\beta \mid \varepsilon \end{aligned}$$

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- ▶ In practice, you can often eliminate much backtracking by restricting the grammar

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- ▶ **Example:** GCC and G++ both use a hand-written recursive descent parser
- ▶ However, you will use the parser-generator `bison` for your homework which has some restrictions on your grammar. Read the posted manual!

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- ▶ **Question:** Why is this the case?

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